

Undrained cylindrical cavity expansion/contraction in stiff clays using a two-surface plasticity model

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Abstract

 This paper presents a semi-analytical solution of undrained cylindrical cavity expansion/contraction problem using a two-surface plasticity model for natural stiff clays from the view point of poromechanics. The present solution reduces the classical boundary problem into a group of seven first-order ordinary differential equations via an auxiliary independent variable *ξ* under undrained conditions. It strictly follows the premise of constant soil mass. Meanwhile, the solution for the constant soil volume problem is used for comparison. It shows that constant soil mass assumption is of paramount importance in developing solutions under high stress condition, while constant soil volume induces non-negligible errors in effective stress and pore pressure distributions. Based on the premise of constant soil mass, extensive parametric studies on cavity expansion/contraction are undertaken to investigate the effects of the model key parameters on the stress components distribution, excess pore pressure distribution and cavity expansion curves. The present solution could be useful while dealing with geotechnical and petroleum engineering problems involving stiff clays or soft claystones. The application in Praclay Gallery excavation in natural Boom clay well demonstrates the validity of the present solution.

 Keywords: stiff clays; cavity expansion/contraction; undrained condition; constant soil mass; elastoplasticity; poromechanics

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1. Introduction

 Cavity expansion theory has been widely applied to interpreting the results from some in situ tests such as cone penetration and pressuremeter tests, analyzing the stresses and deformations induced by wellbore drilling, gallery excavation, tunneling and pile installation. Over the past decades, various analytical and semi-analytical solutions [1-13] for cylindrical and spherical cavity expansions have been developed. With the increasing complexity of constitutive models, from elastic models, elastic perfectly plastic models to critical state models, the solutions are increasingly realistic. Among these models, original and modified Cam-clay models have gained large popularity in solving the cavity expansion and contraction problems for their capability of modelling strain hardening/softening behaviors of soils. Carter et al. [14] firstly investigated the cavity expansion problems with original Cam-clay model by means of finite element analysis. Collins and Yu [6] developed a general solution for large strain undrained cavity expansion using both original and modified Cam-clay models with and without zero initial radius assumption. Cao et al. [7], by following Collins and Yu's approach, developed a semi-analytical solution for undrained cavity using modified Cam-clay model. Mo and Yu [8], extended the original Cam-clay model to a unified state parameter model for clays and sands, then developed a novel solution for both cylindrical and spherical cavity problems. Russell and Khalili [29], using the similarity technique, investigated the cavity expansion problem in unsaturated soils by a unified bounding surface model to consider the influence of suction and moisture content. That study demonstrated there was no difficulty in solving cavity expansion problems using two-surface constitutive models. However, it should be noted that the initial stress state is assumed isotropic and the vertical stress is omitted in two stress invariants in that similarity approach [6]. Recently, Chen and Abousleiman [9-11] proposed novel semi-analytical solutions for both drained and undrained cylindrical cavity expansion/contraction problems. Their solutions removed the limitation on the initial condition of isotropic stress state and depicted a more general case of in situ situation by considering the vertical stress around the expanded/contracted cavity. Based on this versatile framework, Chen et al. [12] used the semi-analytical solution to analyze the three-dimensional strength and the anisotropic properties of soils by introducing Spatially Mobilized Plane (SMP) criterion in modified Cam-clay model. More recently, fabric and stress induced anisotropy has

 also been accounted for using anisotropic elastoplastic models like S-CLAY1 [13] and Dafalias' anisotropic bounding surface model [14]. Although various types of solutions have been proposed, most of them basically treat soil as an original or modified Cam-clay material with an associated flow rule, providing quite low accuracy in modelling heavily over-consolidated clays. In particular, 88 for highly plastic stiff clays or soft claystone, high clay contents, low void ratios, low permeability and high stress states (usually greater than 1 MPa) distinguish them from Cam-clay materials with the following basic hydro-mechanical behaviors:

 (1) Highly nonlinear behaviors are typically observed on stiff clays at heavily over-consolidated states [16]. These pre-yielding nonlinear behaviors would have significant influence on the variations of pore pressure and displacements which are described by advanced constitutive modelling for stiff clays [16, 17, 18, 22].

 (2) For highly plastic stiff clays, the yield surface is of a 'tear' shape rather than an 'elliptical' shape. An 'elliptical' shape would overestimate the failure stress on the 'dry side' but underestimate it on the 'wet side'. The yield surface shape variation would lead to misestimating the excess pore pressure under undrained conditions. On the other hand, the plastic flow direction should also be considered for the complex behavior of stiff clays.

 (3) The pore fluid governs the distribution of excess pore pressure and stress components in expanding process. In relatively low stress states (e.g. 0.1 MPa~1 MPa) under undrained conditions, the volumetric strain due to loading remains almost constant. However, for stiff clays and soft claystone at great depth (e.g. 1MPa~100MPa), the pore water would induce a slight volumetric strain itself, which can significantly influence the excess pore pressure.

 These three main differences make the existing analytical solutions [6-14] difficult to be used directly in analyzing tunneling and piezocone penetration tests in stiff clays under deep ground. On the other hand, although several two-surface plasticity (bounding/subloading surface) models have already been numerically applied into tunnel/gallery construction, e.g. the ground movement (settlement or uplift) induced by tunneling in stiff London clay[38-39] or Shanghai soft clay[37], the excess pore water pressure distribution in Boom clay[35], the characteristic of load transfer in shanghai clay during tunnel operating period[36], the corresponding novel analytical or semi-analytical solutions are still appealing. Based on the rigorous semi-analytical framework proposed by Chen and Abousleiman [9] and the premise of constant soil mass, the study extends

 the solution with a two-surface plasticity model named ACC2 [16] to consider the mechanical behavior of natural stiff clays under high stress conditions. After a brief introduction of the basic formulas, the main features and parameters of the two-surface plasticity model, it is extended to undrained conditions by incorporating the mass conservation for the liquid phase in the pore space. By using the incremental stress-strain relationship, the undrained cavity expansion/contraction problem is formulated to solve a system of first-order ordinary differential equations with two different premises, namely constant soil volume and constant soil mass, respectively. A discussion between Constant Soil Volume (CSV) and Constant Soil Mass (CSM) assumptions is included to highlight that undrained condition corresponds to a situation with constant soil mass. Further parametric studies based on four key material parameters about stress paths, stress distribution and cavity expansion/contraction curves are conducted. Lastly, as a precise and convenient tool, the present semi-analytical solution is utilized to predict the pore pressure and stress distribution along the radial distance and the supporting pressure which is required to maintain the Gallery stability in the case of Praclay Gallery in underground research facility HADES-URF built at a depth of 223m in natural Boom clay.

2. Model description

 This section gives a brief description of the two-surface plasticity model for stiff clays (e.g. natural Boom clay) named ACC2 [16]. The formulation of ACC2 model is based on the triaxial 133 conditions with three principal stresses (namely, σ'_r , σ'_θ , σ'_z in a cylindrical coordinate system):

135
$$
p' = \frac{1}{3}(\sigma_r' + \sigma_\theta' + \sigma_z')
$$
 (1)

136
$$
q = \sqrt{\frac{1}{2} \left(\left(\sigma_r' - \sigma_\theta' \right)^2 + \left(\sigma_r' - \sigma_z' \right)^2 + \left(\sigma_\theta' - \sigma_z' \right)^2 \right)}
$$
(2)

138 Fig.1 Schematic plot of two surface plasticity model ACC2: (a) *p'-q* plane; (b) *υ*-ln *p'* plane

 Fig.1 gives a schematic illustration of the two surfaces (Loading surface and Yield surface). These two surfaces are linked through a progressive hardening relationship by a positive scalar *r* in *υ*-ln *p'* plane. A smooth compression behavior is achieved via the use of two hardening variables \bar{p}'_c and *r* before the soil reaches normally consolidated states:

143
$$
r = \frac{p'}{\bar{p}'} = \frac{q}{\bar{q}} = \frac{p'_c}{\bar{p}'_c}
$$
 (3)

144 where p'_c is the actual loading yield stress on the Loading surface and \bar{p}'_c is the conventional 145 pre-consolidation pressure on the conventional Normal Compression Line.

146 Similar to the concept of bounding surface plasticity, the current stress point (*p', q*) is 147 assumed to always lie on the Loading surface which is expressed as:

148
$$
f_I(p',q,r,p'_c) = q^2 + \frac{M_f^2}{1 - k_f} \left(\frac{p'}{r\overline{p}'_c}\right)^{\frac{2}{k_f}} \left(r\overline{p}'_c\right)^2 - \frac{M_f^2 p'^2}{1 - k_f} = 0
$$
 (4)

149 where M_f is the stress ratio at the apex of the two surfaces and k_f is a parameter specifying the 150 shape of the yield surfaces. Because natural stiff clays (e.g. natural Boom clay) show a unique 151 yielding behavior, a generalized yield surface $(k_f < 2)$ is adopted in this model. While k_f varies

152 from 0.5 to 2, a tear shape surface turns into an elliptical shape more suitable to soft clays in Fig. 153 2(a). The calibrated yielding behavior of natural Boom clay shows that the closest value of k_f is 154 0.7.

155 Two internal variables, namely \bar{p}'_c and *r*, are used to control the plastic strain hardening or 156 softening behavior. A cam-clay type volumetric plastic strain isotropic hardening law for $d\bar{p}'_c$ is 157 adopted:

$$
158 \t d\overline{p}_c' = \frac{\nu}{\lambda - \kappa} \overline{p}_c' d\varepsilon_v^p \tag{5}
$$

159 where *v* is the specific volume; λ is the slope of conventional normal compression line in *v*-ln *p'* **160** plane; *κ* is the slope of reloading line in *v*-ln *p'* plane; $d\varepsilon_v^p$ is the volumetric plastic strain increment. 161

162 Meanwhile, a progressive hardening law for *dr* is introduced with a generalized plastic strain 163 to account for the contribution of both volumetric and shear plastic deformation parts. It should be noted that different strain types are considered in previous works [30, 31, 32]. Russell and Muir 164 165 Wood [28] pointed out that the inclusion of both volumetric and shear parts was of paramount importance in accurately describing soil behavior. This hardening law reads as follows: 166

167
$$
dr = \frac{\nu}{\lambda - \kappa} s (1 - r) d\varepsilon_d^p = \frac{\nu}{\lambda - \kappa} s (1 - r) (d\varepsilon_v^p + A_d d\varepsilon_s^p)
$$
(6)

168 where *s* is the key material parameter $(s > 0)$ that determines the rate at which the Loading surface 169 hardens towards the Yield surface; A_d is a material parameter $(A_d > 0)$ which controls the 170 contribution of plastic shear strain to strain hardening.

 As plotted in Fig.2(c), *s* controls the nonlinearity of the isotropic compression line in over-consolidated states in *υ*-ln *p'* plane. As *s* varies from 4 to 1000, the behavior switches from a nonlinear trend to a bi-loglinear behavior as in the modified cam-clay model. Calibrated with the test results of natural Boom clay, a value of 8 is found for *s*.

175 As plotted in Fig.2(d), parameter A_d ($A_d \ge 0$) can be obtained by fitting stress paths during 176 drained softening stages in highly over-consolidated states. Parameter *Ad* describes how the plastic 177 shear strain affects the hardening process. As *Ad* varies from 0 to 5, the nonlinearity on the 'dry 178 side' is increasingly obvious. It is noteworthy that when $A_d = 0$, the plastic shear strain does not 179 contribute to the hardening process anymore. The most suitable value of *Ad* for natural Boom clay

180 is 0.1.

 The stress dilatancy relation proposed by McDowell et al. [19] is adopted to define a non-associated flow rule for better describing the volumetric strain and excess pore pressure generation during undrained loadings for natural stiff clays. Assuming a plastic potential having the same shape as the yield surfaces but a different pair of parameters (*Mg, kg*), the stress dilatancy equation and the non-associated flow rule are expressed as follows:

186
$$
\frac{d\varepsilon_v^p}{d\varepsilon_s^p} = \frac{\frac{\partial g_1}{\partial p}}{\frac{\partial g_1}{\partial q}} = \frac{M_g^2 - \eta^2}{k_g \eta}
$$
 (7)

187
$$
d\varepsilon_v^p = \Lambda \frac{\partial g_I}{\partial p}, \quad d\varepsilon_s^p = \Lambda \frac{\partial g_I}{\partial q}
$$
 (8)

188 where η denotes the stress ratio q/p' , M_g is the critical state ratio where no further volumetric 189 strain develops and k_g controls the shape of the plastic potential and the direction of plastic flow. 190 Fig.2(b) depicts the variation of plastic flow direction (*kg*) from 0.5 to 2 in *p'-q* plane. The 191 calibrated yielding behavior of natural Boom clay shows that the closest value of *kg* is 0.9.

195 Fig.2 Variation of parameters of ACC2 model in *p'-q* plane and *υ*-ln *p'* plane: (a) *kf* varies from 0.5 196 to 2; (b) *kg* varies from 0.5 to 2; (c) *s* varies from 4 to 1000; (d) *Ad* varies from 0.1 to 5

197 With eleven material parameters (five of them are the same as MCC model), the two-surface plasticity model named ACC2, similarly to bounding surface plasticity theory, has been proposed 198 199 to consider the mechanical behavior of both normally consolidated and over-consolidated stiff clays. Five of them $(\lambda, \kappa, \bar{p}'_c, v, M_f)$ are the same as for the modified cam-clay model. *r* denotes 201 the inverse of over-consolidation ratio. Two parameters (k_f , k_g) control the shapes of the yield surface and the plastic potential surface. Two parameters (*s*, *Ad*) are used to account for a 202 203 progressive hardening mechanism in over-consolidated states. Thus, the following discussion about ACC2 model is mainly done by considering four principal parameters, namely k_f (shape of 205 yield surface), *kg* (direction of plastic flow), *s* (isotropic compression nonlinearity) and *Ad* 206 (deviatoric nonlinearity).

207

208 **3. Problem statement**

209 **3.1 Undrained cylindrical cavity expansion/contraction**

210 Fig.3 presents schematic plots of cylindrical cavity expansion/contraction problems with initial 211 radius $a_{0,0}$ in an infinite elasto-plastic soil layer under undrained conditions. As the cavity expands 212 or shrinks from initial radius $a_{0,0}$ to current radius a_0 , a failure zone would be formed in the 213 vicinity of the cavity wall. At the same time, the outside zone limited by radius $a_{x,0}$ would be 214 plastic with stress points always lying on the Loading surface. Beyond that radius, the soil is in the 215 elastic regime.

216 The radial equilibrium equation for cylindrical cavity expansion/contraction problem is 217 expressed in terms of the effective stress as:

$$
218 \qquad \frac{d\sigma'_r}{da_x} + \frac{\sigma'_r - \sigma'_\theta}{a_x} + \frac{du_w}{da_x} = 0 \tag{9}
$$

219 where σ'_r , σ'_θ are radial, tangential effective stress of any material point, respectively. u_w stands 220 for pore pressure.

$$
\overline{}
$$

223 Fig.3 Geometry of cylindrical cavity problem: (a) expansion; (b) contraction

224 Based on the compatibility condition and large deformation theory, a generalized logarithmic 225 definition of strains in Eulerian description can be adopted in all areas [6]:

$$
226 \qquad \varepsilon_r = -\ln(\frac{da_x}{da_{x0}}), \quad \varepsilon_\theta = -\ln(\frac{a_x}{a_{x0}}), \quad \varepsilon_v = -\ln(\frac{v}{v_0})
$$
\n
$$
\tag{10}
$$

227 where *ax*, *ax*⁰ are the current and initial radii of any material points, respectively. *εr*, *εθ*, *εv* are the 228 radial, tangential and volumetric strains, respectively. *υ*, *υ*⁰ are the current and initial void ratios, 229 respectively.

230 For further study, they can also be expressed in incremental form, as follows:

231
$$
d\varepsilon_r = -\frac{\partial (da_x)}{\partial a_x}, \ d\varepsilon_{\theta} = -\frac{da_x}{a_x}, \ d\varepsilon_{\psi} = -\frac{d\upsilon}{\upsilon}
$$
 (11)

232

233 **3.2 Elastoplastic analysis under undrained condition**

234 The incremental stress-strain relationship for ACC-2 model is expressed in Lagrangian description 235 (see A-17 in Appendix A):

$$
236 \qquad \begin{bmatrix} D\sigma_r' \\ D\sigma_\theta' \\ D\sigma_z' \end{bmatrix} = \begin{bmatrix} c_{rr} & c_{r\theta} & c_{rz} \\ c_{\theta r} & c_{\theta \theta} & c_{\theta z} \\ c_{zr} & c_{z\theta} & c_{zz} \end{bmatrix} \begin{bmatrix} D\varepsilon_r \\ D\varepsilon_\theta \\ D\varepsilon_z \end{bmatrix} \tag{12}
$$

where *D* denotes the differential of material points in Lagrangian description which should be 238 distinguished from *d* in Eulerian form.

Under relatively low stress and undrained conditions, most analytical and semi-analytical 239 solutions, including Chen and Abousleiman's method [9], consider the soil mixture as an 240 ₂₄₁ incompressible material with the undrained Poisson's ratio being equal to 0.5 and the volumetric strain remaining constant. The volume change of pore water due to external loading is ignored. 242 243 This is the case referred to as constant soil volume (CSV). Most reasonable analytical and 244 semi-analytical solutions for undrained cavity problems are extensively developed and applied for various geotechnical problems based on this premise [6-9, 11-15]. Appendix B depicts the 245 246 undrained solution in the form of five first-order ordinary differential equations for the 247 comparative study. However, under high stress and low porosity conditions, the real 248 compressibility of pore fluids (e. g water, oil) would exhibit a significant influence on the excess pore pressure and stress distribution along the cavity. This condition of constant soil volume can 249 250 actually be relaxed by considering that undrained conditions correspond to a situation with constant soil mass (CSM). 251

 The well-known Skempton coefficient *B*, which indicates the ratio between the change in pore pressure and the change in total applied stress in Appendix C-12, could also be used to illustrate the difference. For CSV premise, the value of *B* is always 1 in saturated conditions. This situation may be reasonable for soft clayey soils under low stress conditions (*B>*0.95), but not for stiff clays and soft claystone under high stress conditions (e.g. *B*≈0.92 for natural Boom clay [23], *B*≈0.75 to 0.84 for Callovo–Oxfordian claystone [24, 34], *B*≈0.88 for Opalinus argillite [25]). In such cases, the CSV assumption would lead to unavoidable computational errors for stress and pore pressure distributions, since the effect of pore fluids' compressibility under high stress conditions in not accounted for. Note that the compressibility of the solid particles is still neglected, since it leads to volume changes that are one order of magnitude (at least) lower than 262 the compressibility of the pore fluid.

263

264 **3.3 Undrained cavity expansion/contraction seen as constant soil mass conditions**

265 In the framework of poro-elasto-plasticity theory, pore fluid is typically regarded as a 266 compressible elastic medium with a large bulk modulus (e.g. 2.2×10^3 MPa for water, 1.6×10^3 MPa 267 for oil at room temperature 20° C and isotropic pressure 1 MPa), which is slightly sensitive to

 temperature and pressure variations [21]. The bulk modulus of pore fluid is usually dozens of times that of solid grain. For most clays, the compressibility of solid grains can be neglected (e.g. $C_s = 2.0 \times 10^{-5}$ MPa⁻¹ for Illite [33], to be compared to the water compressibility $C_w = 45.5 \times 10^{-5}$ 271 MPa⁻¹ for water). Considering infinitesimal transformation and undrained conditions (CSM), and neglecting solid grains compressibility, pore water pressure change and soil volumetric change are 273 related using Eulerian porosity *n* and pore fluid's bulk modulus $k_w (k_w=1/C_w)$ as follows:

274
$$
du_w = \frac{d\varepsilon_v - C_s dp}{\phi(C_w - C_s)} \approx \frac{d\varepsilon_v}{nC_w} = \frac{k_w d\varepsilon_v}{n}
$$
 (13)

275 It is noteworthy that Eq (13) is deduced in the framework of poromechanics by Coussy [20]. 276 More details are presented in Appendix C.

 In analyses considering CSM, the soil volumetric strain increment at any material point cannot be ignored even under undrained condition. Meanwhile, the vertical strain increment is still null in cylindrical cavity analysis (plane strain conditions). The general incremental solution for cylindrical cavity problem is expressed in Lagrangian description, as follows:

281
$$
D\varepsilon_y = -\frac{Dv}{v}, D\varepsilon_\theta = -\frac{Da_x}{a_x}, D\varepsilon_z = 0
$$
 (14)

282 An auxiliary independent variable *ξ* is chosen as the ratio of initial radial position to current 283 radial position for each specific particle. The following differentiations can be done:

284
$$
\xi = \frac{a_{x0}}{a_x}, \quad \frac{D\xi}{Da_x} = -\frac{a_{x0}}{a_x^2}, \quad \frac{D\varepsilon_{\theta}}{D\xi} = -\frac{Da_x}{a_x D\xi} = \frac{a_x}{a_{x0}} = \frac{1}{\xi}
$$
 (15)

285 Substituting Eq (15) into Eq (12), the incremental stress-strain relationship can be 286 transformed into three first-order ordinary differential equations with an unknown 287 Lagrangian-form differential $\frac{D\varepsilon_v}{D\varepsilon}$: *D* $\mathcal E$ عج(

$$
288 \qquad \frac{D\sigma'_r}{D\xi} = c_{rr} \frac{D\varepsilon_v}{D\xi} + \frac{c_{r\theta} - c_{rr}}{\xi} \tag{16}
$$

$$
289 \qquad \frac{D\sigma'_{\theta}}{D\xi} = c_{\theta r} \frac{D\varepsilon_{\nu}}{D\xi} + \frac{c_{\theta\theta} - c_{\theta r}}{\xi} \tag{17}
$$

$$
290 \qquad \frac{D\sigma_z'}{D\xi} = c_{zr} \frac{D\varepsilon_v}{D\xi} + \frac{c_{z\theta} - c_{zr}}{\xi} \tag{18}
$$

291 At the same time, the excess pore water pressure can be given in Lagrangian description:

$$
292 \t Du_w = \frac{k_w}{n} D\varepsilon_v \t (19)
$$

293 Thus:

$$
294 \qquad \frac{Du_w}{D\xi} = \frac{vk_w}{\nu - 1} \frac{D\varepsilon_v}{D\xi}
$$
\n⁽²⁰⁾

295 where *kw* is the bulk modulus of pore water, *n* is the current porosity and *υ* is current specific 296 volume.

297 In order to make the problem solvable, let us consider $\frac{D\varepsilon_v}{D\xi} = f$. Substitute Eq (16) and Eq

298 (20) into the radial equilibrium equation (9) gives:

299
$$
\left(\frac{D\sigma'_{r}}{D\xi} + \frac{D u_{w}}{D\xi}\right) \frac{d\xi}{d a_{x}} + \frac{\sigma'_{r} - \sigma'_{\theta}}{a_{x}} = 0
$$
\n(21)

300 Unlike $\frac{25}{R}$ in Eq (15), $\frac{25}{I}$ corresponds to a Eulerian description: *x D Da* عج(*x d da* $\tilde{\xi}$

301
$$
\frac{d\xi}{da_x} = \frac{\frac{da_{x0}}{da_x}a_x - a_{x0}}{a_x^2} = \frac{1}{a_x} \left(\frac{da_{x0}}{da_x} - \xi\right) = \frac{1}{a_x} \left(e^{a_x} - \xi\right)
$$
(22)

302 Integrating Eq (10), the full form of radial strain can be obtained:

303
$$
\varepsilon_r = \varepsilon_v - \varepsilon_\theta = -\ln\left(\frac{\nu}{\nu_0}\right) + \ln\left(\frac{a_x}{a_{x0}}\right) = \ln\left(\frac{\nu_0}{\nu\xi}\right)
$$
 (23)

304 Then:

$$
305 \qquad \frac{d\xi}{da_x} = \frac{1}{a_x} \left(\frac{\nu_0}{\nu \xi} - \xi \right) \tag{24}
$$

306 Making full use of Eq (16), Eq (20) and Eq (24), the radial equilibrium equation (9) turns into 307 Eq (25):

308
$$
\left(c_{rr}f + (c_{r\theta} - c_{rr})\frac{1}{\xi} + \frac{\nu k_w}{\nu - 1}f\right) \times \frac{1}{a_x} \left(\frac{\nu_0}{\nu \xi} - \xi\right) + \frac{\sigma'_r - \sigma'_\theta}{a_x} = 0
$$
 (25)

Then, an equation relating *f* to the other principal variables σ_r' , σ_θ' , $c_{r\theta}$, c_{rr} , v and ξ is obtained: 310

311
$$
f = -\frac{\xi(\sigma_r' - \sigma_\theta') + \left(\frac{v_0}{v\xi} - \xi\right)(c_{r\theta} - c_{rr})}{\left(\frac{v_0}{v} - \xi^2\right)\left(c_{rr} + \frac{vk_w}{v - 1}\right)}
$$
(26)

312 The previous four first-order ordinary differential equations are finally reduced into a full 313 explicit form with respect to the auxiliary independent variable *ξ*:

$$
314 \qquad \frac{D\sigma'_r}{D\xi} = c_{rr}f + \frac{c_{r\theta} - c_r}{\xi} \tag{27}
$$

$$
315 \qquad \frac{D\sigma_{\theta}'}{D\xi} = c_{\theta r}f + \frac{c_{\theta \theta} - c_{\theta r}}{\xi} \tag{28}
$$

$$
316 \qquad \frac{D\sigma_z'}{D\xi} = c_{zr}f + \frac{c_{z\theta} - c_{zr}}{\xi} \tag{29}
$$

$$
317 \qquad \frac{Du_w}{D\xi} = \frac{vk_w}{\nu - 1} f \tag{30}
$$

The other three variables, namely specific volume *v*, pre-consolidation pressure \bar{p}'_c and p_{319} positive scalar r are also included in the differential equations through equation (26):

$$
320 \qquad \frac{Dv}{D\xi} = -vf \tag{31}
$$

321
$$
\frac{D\varepsilon_v^p}{D\xi} = \frac{D\varepsilon_v}{D\xi} - \frac{D\varepsilon_v^e}{D\xi} = f - \frac{\kappa}{\nu(\sigma_r' + \sigma_\theta' + \sigma_z')} \left(\frac{D\sigma_r'}{D\xi} + \frac{D\sigma_\theta'}{D\xi} + \frac{D\sigma_z'}{D\xi}\right)
$$
(32)

322
$$
\frac{D\varepsilon_s^p}{D\xi} = \frac{D\varepsilon_s^p}{D\varepsilon_v^p} \frac{D\varepsilon_v^p}{D\xi} = \frac{k_g \eta}{M_g^2 - \eta^2} \left[f - \frac{\kappa}{\nu(\sigma_r' + \sigma_\theta' + \sigma_z')} \left(\frac{D\sigma_r'}{D\xi} + \frac{D\sigma_\theta'}{D\xi} + \frac{D\sigma_z'}{D\xi} \right) \right]
$$
(33)

323
$$
\frac{D\overline{p}_c'}{D\xi} = \frac{v}{\lambda - \kappa} \overline{p}_c' \frac{D\varepsilon_v^p}{D\xi} = \frac{v}{\lambda - \kappa} \overline{p}_c' \left[f - \frac{\kappa}{v(\sigma_r' + \sigma_\theta' + \sigma_z')} \left((c_r + c_{\theta r} + c_{zr}) \left(f - \frac{1}{\xi} \right) + \frac{c_{r\theta} + c_{\theta\theta} + c_{z\theta}}{\xi} \right) \right]
$$
(34)

$$
\frac{Dr}{D\xi} = \frac{v}{\lambda - \kappa} s(1 - r) \left(\frac{D\varepsilon_v^p}{D\xi} + A_d \frac{D\varepsilon_s^p}{D\xi} \right)
$$
\n
$$
= \frac{v}{\lambda - \kappa} s(1 - r) \left(1 + A_d \frac{k_g \eta}{M_g^2 - \eta^2} \right) \left[f - \frac{\kappa}{v(\sigma_r' + \sigma_\theta' + \sigma_z')} \left((c_{rr} + c_{\theta r} + c_{zr}) \left(f - \frac{1}{\xi} \right) + \frac{c_{r\theta} + c_{\theta\theta} + c_{z\theta}}{\xi} \right) \right]^{(35)}
$$

325 At this stage, based on the premise of CSM, the cylindrical cavity expansion/contraction 326 problem under undrained conditions is finally reduced to seven ordinary differential equations (Eq 327 (27), Eq (28), Eq (29), Eq (30), Eq (31), Eq (34), Eq (35)). These equations can be solved as an 328 initial boundary value problem with *ξ* starting from 1. It is worth noting that these ordinary 329 differential equations which are expressed in terms of *ξ* should finally be converted to the radius 330 position a_x . From equation (24), it is obtained:

$$
331 \qquad \frac{da_x}{a_x} = \frac{d\xi}{\frac{v_0}{v\xi} - \xi} \tag{36}
$$

332 Integrating the above equation, the following formula is obtained:

333
$$
\frac{a_x}{a_0} = \exp\left(\int_{\xi(a_0)}^{\xi} \frac{d\xi}{\frac{v_0}{v\xi} - \xi}\right)
$$
 (37)

334

335 **3.4 Initial condition**

336 The classical undrained cylindrical cavity expansion/contraction problem is eventually solved 337 using these seven first-order ordinary differential equations with the corresponding initial stress 338 conditions. These stress conditions are initially defined as:

339
$$
\sigma'_r(a_{x0}) = \sigma'_{r0}
$$
, $\sigma'_\theta(a_{x0}) = \sigma'_{\theta0}$, $\sigma'_z(a_{x0}) = \sigma'_{z0}$, $u_w(a_{x0}) = u_{w0}$, $v(a_{x0}) = v_0$, $p'_c(a_{x0}) = p'_{c0}$,
\n340 $r(a_{x0}) = r_0$

341 **4. Results and discussion**

 In this section, the results obtained from the semi-analytical solution are presented for the cylindrical cavity expansion/contraction in soils under undrained conditions. The original 11 material parameters of ACC2 model are calibrated and chosen by fitting the laboratory test (isotropic compression, drained triaxial compression) results for natural Boom Clay according to Hong et al. [16] (Table 1 and Table 2): *υs* (void ratio in critical state at isotropic stress of 1 MPa) = 1.84, *λ* (slope of normal consolidation line in *υ*-ln *p'* plane) = 0.18, *κ* (slope of unloading line in *v*-ln *p'* plane) = 0.02, M_g (critical state ratio) = 0.67, M_f (stress ratio at apex of yield surface) = 0.67, \bar{p}'_c (pre-consolidated pressure) = 6 MPa. The Poisson ratio *v* is assumed to be 0.3. It should be noted that the calibration process could be improved by an appropriate genetic algorithm which has been studied in previous literatures [40-45].

 The undrained shear strength *su* is calculated based on the premise of constant soil volume (Wood, 1990):

354
$$
S_u = \frac{1}{\sqrt{3}} M_g e^{(\nu_s - \nu_0)/\lambda}
$$
 (38)

 As mentioned previously, under undrained loading process, the soil sample at low void ratio and under high stress would also induce a slight volumetric strain increment which explains the variation of pore pressure. The *su* assumed here is only for the nondimensionalization purpose.

 This section firstly highlights the effect of the compressibility of pore fluid and the importance of solving the cavity expansion problem using poro-elasto-plasticity under various stress conditions. Representative comparisons are given in Fig. 4-6 between the results for normally consolidated soils based on constant soil volume (CSV) and constant soil mass (CSM) conditions at isotropic effective stresses of 2 MPa, 10 MPa, 50 MPa, respectively. The soil mass is fully saturated with pore water. Moreover, a full range of isotropic stresses from 0.1 MPa to 100 MPa is considered to assess the relative errors between these two assumptions under cavity 365 expansion condition $(a_0/a_{0.0} = 2)$. Isoerror maps computed for stress components are plotted in Fig. 7.

 Then, based on CSM premises, parametric studies of cavity expansion at normal consolidated 368 stress state $(r=1)$ and highly over-consolidated stress state $(r=2.9)$ using ACC2 model are conducted. It aims at illustrating the advantages brought by the use of this sophisticated model, when compared to simple models like MCC, for which analytical solutions for the same problem already exist.

372 (1) ACC2 model with different values of yield shape parameter k_f (0.5 to 2) as Case 4 and plastic 373 flow direction parameter k_g (0.5 to 2) as Case 5 at normally consolidated stress state $(r_0=1)$ is applied to investigate the effect of the shape of yield surface (the yielding behavior) and the shape of plastic potential surface (the direction of plastic flow).

 (2) ACC2 model with isotropic compression non-linearity parameter *s* (4 to 1000) as Case 6 and 377 deviatoric non-linearity parameter A_d (0.1 to 5) as Case 7 is applied to investigate the effect of the 378 nonlinearity at a highly over-consolidated stress state $(r_0=2.9)$.

380 **4.1 Comparison between CSV and CSM conditions**

387 points reach the plastic state to some extent.

381 The results obtained using CSV and CSM assumptions at three isotropic effective stress states 382 (*p'*=2, 10, 50 MPa) are compared in Fig. 4 as Case 1, Fig. 5 as Case 2 and Fig. 6 as Case 3. The 383 soil is initially assumed to be at normally consolidated and isotropic stress state (*r*=1), then rapidly 384 expanded to a certain cavity radius $(a_0/a_{0.0} = 2)$ without considering the rate and seepage effect. 385 During the expanding process, a critical state zone where the stress state at any point satisfies 386 *q*=*Mgp'* would be formed in vicinity of the cavity. Outside the critical state zone, all material

 There is a clear difference between CSV and CSM in stress and excess pore pressure 389 distributions along the radius distance in Fig. 4-6. From the normalized effective stress (σ'_r / s_u , $390 \sigma'_{\theta}/s_u$, σ'_z/s_u) distributions along the radius distance corresponding to the cavity radius ratio of *a*₀/*a*_{0,0} = 2 in Fig. 4(a), Fig. 5(a) and Fig. 6(a), the expanding results obtained based on CSM appear to be slightly larger than those based on CSV at each corresponding point. The opposite 393 phenomenon could be observed in the normalized excess pore pressure $\Delta u_w/s_u$ and stress ratio η distributions along the radius distance in Fig. 4(b), Fig. 5(b) and Fig. 6(b). Meanwhile, the range of critical state zone (see CP boundary) for CSM is shorter than for CSV. The CP boundary corresponds to the boundary between critical state zone and plastic zone. It can be determined by 397 the evolution of current stress ratio ($n=q/p'$) along normalized radial distance. With the increase of initial isotropic stress, the difference between CSV and CSM becomes more and more obvious.

400 would influence the excess pore pressure and principal effective stress distributions. This confirms 401 the necessity of considering the compressibility of pore fluid under high stress conditions.

399 Through the comparison between the two cases, it can be concluded that the premise of CSV

403 Fig. 4 Undrained cavity expansion at normally consolidated and isotropic stress state (*p'*= 2 MPa):

407 Fig. 5 Undrained cavity expansion at normally consolidated and isotropic stress state (*p'*= 10 MPa): 408 (a) normalized principal stress distributions; (b) normalized excess pore pressure and stress ratio 409 distribution

411 Fig. 6 Undrained cavity expansion at normally consolidated and isotropic stress state (*p'*= 50 MPa): 412 (a) normalized principal stress distributions; (b) normalized excess pore pressure and stress ratio 413 distribution

414

415 In order to estimate the relative errors based on the two premises, a full range of isotropic 416 stress from 0.1 MPa to 100 MPa is considered in cavity expansion process. The relative errors (*Re*) 417 for three principal stresses and pore pressure are defined as: $Re = |V_{CSM} - V_{CSV}|/|V_{CSM}|$. In the 418 formula, *VCSM*, *VCSV* represent the corresponding results of each material point based on CSM and 419 CSV, respectively.

423 Fig. 7 Isoerror maps plotted for constant soil mass (CSM) and constant soil volume (CSV): (a) 424 radial effective stress; (b) tangential effective stress; (c) vertical effective stress; (d) excess pore 425 pressure

426 Figs. 7(a)-(c) plot isoerror maps for the three principal effective stress distributions from a_x/a_0 $427 = 1$ to $a_x/a_0 = 10$ in mean effective stress range from 0.1 MPa to 100 MPa when the cavity expands 428 to $a_0/a_{0,0} = 2$. Case 1 of $p'=2$ MPa, case 2 of $p'=10$ MPa, case 3 of $p'=50$ MPa are specially pointed out. In the range from 0.1 MPa to 1 MPa (low stress conditions), the value of *Re* is less than 1%, suggesting that both cases (CSM, CSV) would get reliable results in principal stress distributions. However, when the isotropic stress is larger than 10 MPa (relatively high stress conditions), the value of *Re* would increase rapidly. Meanwhile, the *Re* value for excess pore pressure distribution in Fig. 7(d) is much more sensitive to pressure change than the effective stress distribution at both low and high stress conditions.

438 **4.2 Results with variations of yield surface parameter**

439 A parametric study of cavity expansion is presented as Case 4 with variable k_f and fixed k_g (k_g = 440 0.9) for *r*=1 (normally consolidated state) based on CSM. Four different values of *kf* (0.5, 0.7, 0.9, 441 2), representing tear shape to elliptical shape, are considered to investigate the impact of the shape 442 of yield surface on the stress and pore pressure distributions around the cavity.

 Fig. 8(a) shows the effective stress paths normalized by the undrained shear strength *su* from *a*₀/a_{0,0} = 1 to $a_0/a_{0,0} = 2$ at the cavity wall. With the change of k_f from 0.5 to 2, the shape of yield surface varies and the intersection with the critical state line decreases. Figs. 8(b), 8(d) depict the 446 normalized effective stresses $(\sigma'_r / s_u, \sigma'_\theta / s_u, \sigma'_z / s_u)$ and pore pressure $\Delta u_w / s_u$ distributions 447 along radius position. The radius position a_x is normalized by cavity radius a_0 and plotted in the scale of logarithm. It can be seen that in the vicinity of cavity wall the three principal stresses remain almost unchanged, indicating that the soil in this range has reached the critical state.

 Further investigation on the shape variation of yield surface shows that positive increment of *kf* would sharply decrease the values of the three principal stresses in the critical state range (Fig. 8(a)), but have negligible effects on the location of CP boundary. Fig. 8(c) presents the cylindrical 453 cavity expansion curve from $a_0/a_{0,0} = 1$ to $a_0/a_{0,0} = 10$ at the cavity wall. The cavity pressure and excess pore pressure increase rapidly to a limit and then stay constant with cavity expanding. With the change of *kf* from 0.5 to 2, the present solution predicts a decreasing cavity pressure and excess pore pressure limit around cavity wall. In Fig. 8(d), the normalized excess pore pressure would decrease monotonously along the radial distance. In the vicinity of the cavity wall, the stress point 458 would reaches the critical state where three principal stresses $(\sigma_r', \sigma_\theta', \sigma_z')$ remain almost

459 constant
$$
\left(\frac{d\sigma'_r}{da_x} = \frac{d\sigma'_\theta}{da_x} = \frac{d\sigma'_z}{da_x} = 0\right)
$$
 and the radial balance equation $\left(\frac{d\sigma'_r}{da_x} + \frac{\sigma'_r - \sigma'_\theta}{a_x} + \frac{du_w}{da_x} = 0\right)$

460 would reduce into $\frac{G_{rc} - G_{\theta c}}{r} + \frac{du_w}{l} = 0$. σ'_{rc} , $\sigma'_{\theta c}$ is the corresponding radial, tangential 461 effective stress at the critial state zone, respectively. So the solution of pore water pressure at this 462 zone would be $u_w = -(\sigma'_m - \sigma'_m) \ln a_x + C(C$ is a constant). For the case of cavity expansion, 463 σ'_{rc} is larger than $\sigma'_{\theta c}$ and the excess pore pressure would decrease in the vicinity of the cavity 464 wall (critical state zone). Meanwhile, under normal consolidated state, the stress would directly x \mathcal{U}_{x} *du* $\frac{\sigma'_{rc} - \sigma'_{\theta c}}{a_r} + \frac{du_w}{da_r} = 0$. σ'_{rc} , $\sigma'_{\theta c}$

465 turn into shear contraction state before reaching the cirtical state line. So the excess pore pressure

466 would directly decrease from CP boundary to $a_x/a_0 = 100$.

469 Fig. 8 Undrained cavity expansion results with change of *kf* from 0.5 to 2: (a) normalized stress 470 paths at cavity wall; (b) normalized principal stress distributions; (c) normalized cavity expansion 471 curve; (d) normalized excess pore pressure distribution

472

473 **4.3 Results with variations of plastic potential surface parameter**

474 A parametric study is presented as Case 5 with variable k_g and fixed k_f (k_f = 0.7) for $r=1$ and \bar{p}_c 475 (normally consolidated state) to investigate the impact of the direction of plastic flow on the stress 476 and pore pressure distributions around the cavity.

 From the same initial stress state, the four effective stress paths with different *kg* values (0.5, 478 0.7, 0.9, 2) normalized by the undrained shear strength s_u from $a_0/a_{0,0} = 1$ to $a_0/a_{0,0} = 2$ at the cavity wall are found to be almost overlapped in Fig. 9(a). This suggests that *kg* merely control the direction of plastic flow and portion of shear plastic strain in loading process. Fig. 9(b), 9(d) 481 depict the normalized effective stresses $(\sigma'_r / s_u, \sigma'_\theta / s_u, \sigma'_z / s_u)$ and pore pressure $\Delta u_w / s_u$ distributions with the variation of *kg*. The effective stresses in the vicinity of cavity wall typically remain constant. As opposed to changes of *kf*, the direction variation of plastic flow shows that an 484 positive increment of k_g induces more deviatoric plastic strains, leading to a sharp decrease of the 485 radius of critical state zone, but has negligible effects on the critical values of the three principal 486 stresses in the critical state zone. It also shows a slight reduction of excess pore pressure around 487 the cavity wall when an increasing plastic shear strain portion is produced.

490 Fig. 9 Undrained cavity expansion results with the variation of *kg* from 0.5 to 2: (a) normalized 491 stress paths at cavity wall; (b) normalized principal stress distributions; (c) normalized cavity 492 expansion curve; (d) normalized excess pore pressure distribution

493

494 **4.4 Results with variations of isotropic nonlinear parameter**

 In highly over-consolidated states, stiff clays typically exhibit a non-linear behavior under loading process without pure elastic deformations. A parametric study of cavity expansion in over-consolidated states with different isotropic nonlinear parameter *s* (4, 8, 20, 1000) is presented as Case 6. Note that *s* controls the evolution rate of Loading surface in approaching Yield surface, namely the nonlinearity of isotropic compression from over-consolidated state to normally consolidated state. A smaller *s* represents a clear nonlinearity of isotropic loading in *υ*-ln *p'* plane, while a larger *s* means that the compression line in *υ*-ln *p'* plane is closer to bi-linearity.

502 The expanding cavity is defined by an initial in-situ stress of σ'_{r} =1.91 MPa, σ'_{θ} =1.91 MPa 503 and $\sigma_z' = 2.25 \text{ MPa}$ with a pre-consolidation pressure of $\bar{p}_c' = 6 \text{ MPa}$ and over-consolidation ratio of *r*=2.9 as listed in Table.2. Figs. 10(a)-(d) depict the normalized effective stress paths at cavity wall, normalized cavity expansion curves, the normalized effective stresses and excess pore 506 pressure distributions with change of *s*. Under the expanding process from $a_0/a_{0,0} = 1$ to $a_0/a_{0,0} = 2$, the normalized effective stresses follow different stress paths with *s* varying from 4 to 1000 in Fig. 10(a). The direction of arrow means the increasing trend of *s*. When *s* reaches the value of 1000, the initial mechanical behavior is more elastic which explains the stress path being upward at the beginning of undrained loading process.

 In Fig. 10(b), the range of critical state zone is sharply dependent on *s*. But the critical values of normalized effective stresses are independent of *s*. It is worth noting that with the decreasing of *s* (the increasing nonlinearity of isotropic compression), the radius of critical state zone would decrease to zero where no pure critical state zone exists. With the increasing of *s* (the decreasing nonlinearity of isotropic compression), the radius of critical state zone would increase to a limit where no further critical state zone develops. For an extremely large value of *s* (e.g. 1000), the analytical results are similar to the case of over-consolidated states expressed in modified cam-clay model [9]. Meanwhile, the increase in nonlinearity of isotropic compression would eventually results in the decrease of effective stress in plastic zone.

 In Figs. $10(c)$ -(d), the normalized wall pressure at cavity wall is positive, in agreement with the value of *s*. A sophisticated phenomenon is observed on the normalized excess pore pressure. At the beginning of expanding process, the normalized excess pore pressure would firstly increase, decrease and then increase to a limited value. With the increasing of *s*, the increasing and 524 decreasing phenomenon would be more obvious. At the expanded cavity of $a_0/a_{0.0} = 2$, the normalized excess pore pressure at cavity wall would increase to a limit value with increasing *s*. In the critical state zone, the normalized excess pore pressure would decrease along the normalized radial distance. Unlike the results by modified cam-clay model [9], a 'second peak' of normalized excess pore pressure is observed, which is owing to the soil's shear dilatancy behavior under 529 highly over-consolidated states. From $a_x/a_0 = 100$ to the 'second peak', the excess pore pressure would increase (shear contraction); from the 'second peak' to the CP boundary, the excess pore pressure would decrease (shear dilatancy) and the value of excess pore pressure would be $-(\sigma_{rc}^{\prime} - \sigma_{\theta c}^{\prime})\ln a_x + C(C \text{ is a constant})$ in the range of critical state zone. The position of the 533 'second peak' is also consistent with the value of *s*. In the far end of expanded cavity, excess pore

534 pressure would vanish.

537 Fig. 10 Undrained cavity expansion results with different values of *s* from 4 to 1000: (a) 538 normalized stress paths at cavity wall; (b) normalized principal stress distributions; (c) normalized 539 cavity expansion curve; (d) normalized excess pore pressure distribution

540

541 **4.5 Results with the variations of deviatoric nonlinear parameter**

 In over-consolidated states, parameter *Ad* describes how the plastic shear strain affects the hardening process. It can be calibrated from the stress paths under high over-consolidated states in undrained conditions. A parametric study of cavity expansion in over-consolidated states with different values of deviatoric nonlinear parameter *Ad* (0.1, 0.5, 1, 5) is presented as Case 7.

546 An in-situ stress of $\sigma_r' = 1.91$ MPa, $\sigma_\theta' = 1.91$ MPa and $\sigma_z' = 2.25$ MPa with a 547 pre-consolidation pressure of $\bar{p}_c^{\prime} = 6$ MPa and over-consolidation ratio of $r=2.9$ is considered to 548 evaluate the impact of A_d on the stress and pore pressure distributions around the cavity.

551 Fig. 11 Undrained cavity expansion results with different values of *Ad* from 0.1 to 5: (a) 552 normalized stress paths at cavity wall; (b) normalized principal stress distributions; (c) normalized 553 cavity expansion curve; (d) normalized excess pore pressure distribution

 Figs. 11(a)-(d) depict the results with different *Ad* values. Similar to nonlinear parameter *s*, the radius of critical state zone is sharply dependent on *Ad*. But the critical values of normalized effective stress are independent of *Ad*. With the decreasing of *Ad*, the radius of critical state zone 557 would decrease to zero where no pure critical state zone exists. At the expanded cavity of $a_0/a_{0,0}$ = 2, the normalized excess pore pressure at the cavity wall and the range of critical state zone would increase with increasing *Ad*. One should also note that the increasing of *Ad* means the increasing portion of plastic shear strain and the decreasing portion of plastic volumetric strain in hardening process. With the increasing of *Ad*, the stress path would be more likely upward at the beginning of undrained loading process. In Fig. 11(d), a 'second peak' of normalized excess pore pressure is also observed and the peak gradually vanish with the increasing of *Ad*.

564

565 **5. Application to Praclay Gallery excavation**

566 This section examines the application of the present solution into the excavation of Praclay 567 Gallery in underground research facility HADES-URF built at a depth of 223m in natural Boom

 clay and located in Mol, Belgium [26, 27]. The natural Boom clay is a deposit of over-consolidated stiff clay which have been specifically investigated in the previous studies [16]. Meanwhile, the natural Boom clay is initially considered as homogeneous, at an isotropic effective stress of 2.3 MPa and fully saturated with an initial pore pressure of 2.2 MPa.

 Praclay Gallery is excavated 45 meters long in horizontal plane, so it is regarded as a plane strain problem as plotted in Fig. 12. The inner radius of Praclay Gallery and the thickness of the concrete liner is equal to 0.95 m, 0.3m, respectively. During the construction of Praclay Gallery, a total over-excavation of 0.06m is applied. Since it is finished in a short period (less than 1 day) 576 and the intrinsic permeability of natural Boom clay is extremely low $(2\sim4\times10^{-19} \text{ m}^2)$, the excavation of Praclay Gallery can also be regarded as an undrained cavity contraction process.

Fig. 12 Excavation plane of Praclay Gallery in natural Boom clay

 Fig. 13(a) presents the analytical results by cavity contraction and the test values from four pore pressure transducers placed at different nominal radial distances from the center of Praclay Gallery [26]. It shows that the present solution could basically describe the pore pressure distribution along radial distances. In the vicinity of cavity wall, pore pressure would reduce with 585 radial distance decreasing. Then a peak value shows up around the radial distance of $5{\sim}10$ m. After that peak, the pore pressure would gradually reduce to its normal value of 2.2 MPa.

 Fig. 13(b) depicts three principal stress distributions along radial distance by the solution of cavity contraction. It shows that the vicinity of cavity wall has not reached the critical state yet. The effective stress path of point A in Fig. 13(c) can also be preferential for studying the stress states around the contracting wall.

In the cavity contraction curve (Fig. 13(d)), the wall pressure at Praclay Gallery would

 gradually reduce with the increasing radial strain. In the present case, the radial strain is equal to 4.58% (radial displacement is 0.06m) and a wall pressure of 1.93 MPa is formed. However, when the radial strain reaches 21%, the wall pressure would be zero. It indicates that no more supporting pressure needs to be added on the cavity wall.

> 3.0 3.5

 $\sigma_{\scriptscriptstyle \! s}$

Effective stress /MPa Pore pressure /MPa Effective stress /MPa 2.0 2.5 1.5 $\frac{5}{2}$ $\frac{5}{2}$ $\frac{5}{2}$ $\frac{1}{2}$ $\frac{5}{2}$ $\frac{5}{2}$ ¢ 2.0 σ 1.0 1.5 0.5 Test Data[26] ¢ Analytical ^s *r* Analytical 0.0
20
40
60
80
100

20
Radial distance /m 1.0 $\begin{array}{c|c|c|c|c|c} \n1.0 & 10 & 100 \n\end{array}$

Normalized radial distance a_x/a_0 3 wall pressure at Praclay Gallery /MPa wall pressure at Praclay Gallery /MPa Analytical 4 Deviatoric stress /MPa \overline{c} 2 Eff ecc Path 2 $\sigma_{\scriptscriptstyle a}$ 597 $\frac{1}{2}$ $\frac{1$ 1 0 Current radial strain: 4.58% Maximum radial strain: 21% -2

0.00 0.05 0.10 0.15 0.20 0.25

Radial strain $\begin{array}{ccccccc}\n0 & 1 & 2 & 3 & 4 & 5 \\
0 & 1 & 2 & 3 & 4 & 5\n\end{array}$

Mean stress /MPa

598 Fig. 13 The excavation of Praclay Gallery: (a) pore pressure distribution along radial distance; (b) 599 principal effective stress distributions along normalized radial distance; (c) total and effective 600 stress paths of Point A; (d) cavity contraction curve

601

602 **6. Conclusion**

2.5 3.0

Peak

w u

 This paper presents a semi-analytical solution for undrained cylindrical cavity expansion/contraction problems using a two-surface plasticity model, which can well reproduce the yielding behaviors, unassociated plastic flowing directions and high nonlinearity of stiff clays. To develop the new solution, the premise of constant soil mass based on poromechanics is recalled. A set of seven governing differential equations is obtained and solved as an initial boundary value problem with an auxiliary independent variable *ξ*. The new solution based on constant soil mass is then compared with the one based on constant soil volume, showing its relevance under high stress conditions. Then, based on the constant soil mass premise, the variations of yield surface parameter, plastic flow direction parameter, isotropic nonlinear parameter and deviatoric nonlinear

 parameter are investigated in a parametric study focusing on the stress paths, stress and excess pore pressure distributions and cavity expansion/contraction curves. The results obtained allows the following conclusion to be drawn:

 (1) The premise of constant soil mass is important in solving cavity expansion/contraction problems especially under high stress, low porosity and multi-fluid situations. Indeed, under relatively low stress conditions (e.g. *p'<*1 MPa), the solutions based on constant soil mass and constant soil volume are found to be similar. However, with the increasing of stress, the compressibility of pore fluid becomes crucial and the volumetric strain could be no longer regarded as constant. The premise of constant soil mass become preferential.

621 (2) In normally consolidated states, the shape variation of yield surface (k_f) would change the three principal stresses in critical state zone but have no effect on the range of critical state zone. On the contrary, the variation of plastic flow direction (*kg*) would change the range of critical state zone but have no effect on the three principal stresses in the critical state zone.

 (3) The high nonlinearity means no pure elastic zones in over-consolidated states. The decreasing of both nonlinearity parameter *s* and *Ad* decreases the range of critical state zone even to zero where no pure critical state zone exists. Meanwhile, a 'second peak' value of normalized excess pore pressure along cavity radius is observed and the peak would gradually approach the cavity wall with the decreasing of *s* and *Ad*.

 (4) The present semi-analytical solution can be directly applied to explore the pore pressure, stress distributions and wall pressure around the expanding/contracting cavity (e.g. Praclay Gallery excavation).

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640 **Appendix A**

641 The effective stress and total strain increments are defined with three principal components in a

642 cylindrical coordinate system:

$$
\mathbf{d}\mathbf{\sigma}' = \begin{bmatrix} d\sigma'_r & d\sigma'_\theta & d\sigma'_z \end{bmatrix}^T
$$
 (A - 1)

$$
\mathbf{d}\mathbf{\varepsilon} = \begin{bmatrix} d\varepsilon_r & d\varepsilon_\theta & d\varepsilon_z \end{bmatrix}^T
$$
 (A - 2)

645 The total strain increment is split into elastic and plastic parts:

$$
646 \qquad d\epsilon = d\epsilon^e + d\epsilon^p \tag{A-3}
$$

$$
\mathbf{d}\mathbf{\varepsilon}^{\mathbf{e}} = \left[d\varepsilon_r^e \quad d\varepsilon_\theta^e \quad d\varepsilon_z^e \right]^T \tag{A-4}
$$

$$
\mathbf{d}\boldsymbol{\varepsilon}^{\mathbf{p}} = \begin{bmatrix} d\varepsilon_r^p & d\varepsilon_\theta^p & d\varepsilon_z^p \end{bmatrix}^T
$$
 (A - 5)

$$
\mathbf{a} = \begin{bmatrix} a_r & a_{\theta} & a_z \end{bmatrix}^T \tag{A - 6}
$$

650
$$
a_r = \frac{\partial f_1}{\partial \sigma'_r} = \frac{M_f^2}{3(1 - k_f)} \left(\frac{2}{k_f} p^{r^2 - 1} (rp'_c)^{2 - \frac{2}{k_f}} - 2p' \right) + 6(\sigma'_r - p')
$$
(A - 7)

651
$$
a_{\theta} = \frac{\partial f_{I}}{\partial \sigma_{\theta}'} = \frac{M_{f}^{2}}{3(1 - k_{f})} \left(\frac{2}{k_{f}} p^{r \frac{2}{k_{f}} - 1} (rp_{c}')^{2 - \frac{2}{k_{f}}} - 2p' \right) + 6(\sigma_{\theta}' - p') \tag{A-8}
$$

652
$$
a_z = \frac{\partial f_1}{\partial \sigma'_z} = \frac{M_f^2}{3(1 - k_f)} \left(\frac{2}{k_f} p'^{\frac{2}{k_f}-1} (rp'_c)^{2-\frac{2}{k_f}} - 2p' \right) + 6(\sigma'_z - p') \tag{A-9}
$$

$$
\mathbf{b} = \begin{bmatrix} b_r & b_\theta & b_z \end{bmatrix}^T \tag{A-10}
$$

654
$$
b_r = \left(\frac{\partial g}{\partial p'}\middle/ \frac{\partial g}{\partial q} \times \frac{\partial p'}{\partial \sigma_r'} + \frac{\partial q}{\partial \sigma_r'}\right) \times k_g \eta = \frac{1}{3} \left(M_g^2 - \eta^2\right) + \frac{3}{q} k_g \eta \left(\sigma_r' - p'\right)
$$
(A-11)

655
$$
b_{\theta} = \left(\frac{\partial g}{\partial p'}\middle/ \frac{\partial g}{\partial q} \times \frac{\partial p'}{\partial \sigma_{\theta}'} + \frac{\partial q}{\partial \sigma_{\theta}'}\right) \times k_g \eta = \frac{1}{3} \left(M_g^2 - \eta^2\right) + \frac{3}{q} k_g \eta \left(\sigma_{\theta} - p'\right)
$$
(A - 12)

656
$$
b_z = \left(\frac{\partial g}{\partial p'}\middle/ \frac{\partial g}{\partial q} \times \frac{\partial p'}{\partial \sigma_z'} + \frac{\partial q}{\partial \sigma_z'}\right) \times k_g \eta = \frac{1}{3} \left(M_g^2 - \eta^2\right) + \frac{3}{q} k_g \eta \left(\sigma_z' - p'\right)
$$
(A - 13)

$$
h = -\frac{\partial f}{\partial p'_c} \frac{\partial p'_c}{\partial \varepsilon_r^p} \frac{\partial g}{\partial p'} - \frac{\partial f}{\partial r} \left(\frac{\partial r}{\partial \varepsilon_r^p} \frac{\partial g}{\partial p'} + \frac{\partial r}{\partial \varepsilon_r^p} \frac{\partial g}{\partial q} \right)
$$

\n
$$
= \frac{\partial f}{\partial p'_c} \frac{v_0}{\lambda - \kappa} \left(M_g^2 - \eta^2 \right) + \frac{\partial f}{\partial r} \frac{v_0}{\lambda - \kappa} s (1 - r) \left(\left(M_g^2 - \eta^2 \right) + A_d k_g \eta \right)
$$
 (A - 14)

658
$$
\frac{\partial f}{\partial p'_c} = \frac{M_f^2}{1 - k_f} p'^{\frac{2}{k_f}} \left(2 - \frac{2}{k_f}\right) p'_c^{\frac{1 - \frac{2}{k_f}}{k_f}} r^{\frac{-\frac{2}{k_f}}{k_f}} \tag{A-15}
$$

659
$$
\frac{\partial f}{\partial r} = \frac{M_f^2}{1 - k_f} p^{r \frac{2}{k_f}} \left(2 - \frac{2}{k_f} \right) r^{1 - \frac{2}{k_f}} p_c^{r^2 - \frac{2}{k_f}}
$$
(A - 16)

$$
660 \t d\sigma' = \mathbf{D}_{ep} d\mathbf{\varepsilon} = \left(\mathbf{D}_{e} - \frac{\mathbf{D}_{e} b\boldsymbol{\alpha}^{T} \mathbf{D}_{e}}{\boldsymbol{\alpha}^{T} \mathbf{D}_{e} b + h}\right) d\mathbf{\varepsilon}
$$
 (A - 17)

661
$$
\mathbf{D}_{e} = \frac{3K}{1+v} \begin{bmatrix} 1-v & v & v \\ v & 1-v & v \\ v & v & 1-v \end{bmatrix}
$$
 (A - 18)

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676 **Appendix B**

677 In the constant soil volume assumption where pore water is regarded as an incompressible fluid, 678 the undrained cylindrical cavity expansion/contraction problem is a simple plane strain 679 deformation problem with five first-order ordinary differential equations for all material points, 680 namely:

$$
681 \qquad \frac{D\sigma_r'}{Da_x} = \frac{c_{rr} - c_{r\theta}}{a_x} \tag{B-1}
$$

$$
682 \qquad \frac{D\sigma_{\theta}'}{Da_{x}} = \frac{c_{\theta r} - c_{\theta \theta}}{a_{x}} \tag{B-2}
$$

$$
683 \qquad \frac{D\sigma_z'}{Da_x} = \frac{c_{zr} - c_{z\theta}}{a_x} \tag{B-3}
$$

684
$$
\frac{Dp'_{c}}{Da_{x}} = -\frac{\kappa p'_{c}}{\lambda - \kappa} \frac{c_{rr} + c_{\theta r} + c_{zr} - c_{r\theta} - c_{\theta \theta} - c_{z\theta}}{a_{x} (\sigma'_{r} + \sigma'_{\theta} + \sigma'_{z})}
$$
(B - 4)

685
$$
\frac{Dr}{Da_x} = -\frac{\kappa}{\lambda - \kappa} s (1 - r) \left(1 + \frac{A_d k_g \eta}{M_g^2 - \eta^2} \right) \frac{c_{rr} + c_{\theta r} + c_{zr} - c_{r\theta} - c_{\theta \theta} - c_{z\theta}}{a_x (\sigma_r' + \sigma_\theta' + \sigma_z')}
$$
(B - 5)

686 where D/Da_x denotes the material derivative taken along the particle motion path (Lagrangian 687 description), and *η* denotes the current stress ratio *q*/*p'*.

688 Meanwhile, the constant soil volume assumption would induce a constraint following the equation

689 regarding the current position of any material point a_x and the expanded cavity radius a_0 :

690
$$
a_x^2 - a_{x0}^2 = a_0^2 - a_{00}^2
$$
 (B - 6)

691 where a_{x0} is the initial position of the material point and a_{00} is the initial cavity radius.

692 The distribution of pore water pressure $u_w(a_x)$ can be obtained by integrating the radial equilibrium 693 equation:

694
$$
u_w(a_x) = \sigma'_{r0} + u_{w0} - \sigma'_{r}(a_x) - \int_{-\infty}^{a_x} \frac{\sigma'_{r} - \sigma'_{\theta}}{a_x} da_x
$$
 (B - 7)

695

696

698 **Appendix C**

699 In isotropic stress state, the total mean stress change (dp) and lagrangian porosity change $(\frac{d\phi}{})$

700 can be expressed by changes of volumetric strain (*dεv*) and pore water pressure (*duw*), as follows:

$$
701 \t dp = \frac{1}{C_d} d\varepsilon_v + b du_w \t (C - 1)
$$

$$
702 \t d\phi = -bd\varepsilon_v - \frac{1}{N}du_w \t\t (C-2)
$$

703 with the Maxwell's symmetry condition given by:

$$
704 \qquad b = \left(\frac{\partial p}{\partial u_w}\right)_{\varepsilon_v} = -\left(\frac{\partial \phi}{\partial \varepsilon_v}\right)_{u_w} \tag{C-3}
$$

705 The volumetric compressibility of soil skeleton C_d , the Biot coefficient *b* appearing in Eq (C - 1) 706 are defined as:

707
$$
\frac{1}{C_d} = \left(\frac{\partial p}{\partial \varepsilon_v}\right)_{u_w}, b = \left(\frac{\partial p}{\partial u_w}\right)_{\varepsilon_v}
$$
 (C - 4)

708 The Biot coefficient *b*, Biot modulus *N* appearing in Eq (C - 2) are defined as:

$$
709 \qquad b = -\left(\frac{\partial \phi}{\partial \varepsilon_v}\right)_{u_w}, \frac{1}{N} = -\left(\frac{\partial \phi}{\partial u_w}\right)_{\varepsilon_v}
$$
 (C - 5)

710 Eqs (C - 4, C - 5) are partial differential equations and the subscripts indicate that the 711 corresponding variables are kept constant.

712 Considering the relations between the skeleton and mineral solid properties, the compatibility 713 relations can be obtained:

714
$$
b = I - \frac{C_s}{C_d}, \frac{I}{N} = (\phi - b)C_s
$$
 (C - 6)

715 where *Cs* is the volumetric compressibility coefficient of mineral solid.

716 In a fully saturated porous medium, the current fluid mass (*mw*) per unit volume can be expressed 717 as:

$$
718 \qquad m_{w} = \rho_{w} \phi \tag{C-7}
$$

719 Differentiating Eq (C - 7) gives:

$$
720 \qquad \frac{dm_w}{\rho_w} = d\phi + \phi \frac{d\rho_w}{\rho_w} \tag{C-8}
$$

721 The change of fluid density reads as follows:

$$
722 \qquad \frac{d\rho_w}{\rho_w} = C_w du_w \tag{C-9}
$$

723 where C_w is the volumetric compressibility of pore fluid.

724 From Eqs $(C - 1, C - 2, C - 6, C - 8, C - 9)$, the following equation can be obtained:

725
$$
\frac{dm_w}{\rho_w} = -(C_d - C_s)dp - ((\phi C_s - \phi C_w) - (C_d - C_s))du_w
$$
 (C - 10)

726 In undrained conditions, the mass of the fluid phase is constant and $dm_w = 0$ holds. Thus, the 727 expressions for incremental pore water pressure can be obtained:

728
$$
du_w = \frac{C_d - C_s}{C_d - C_s + \phi(C_w - C_s)} dp = \frac{d\varepsilon_v - C_s dp}{\phi(C_w - C_s)}
$$
(C - 11)

729 The well-known Skempton coefficient *B* which indicates the ratio between pore pressure 730 increment and total isotropic stress increment is thus given by:

731
$$
B = \frac{C_d - C_s}{C_d - C_s + \phi(C_w - C_s)}
$$
(C - 12)

732 The compressibility of pore fluid is usually dozens of times that of solid grain. For most clays, the 733 compressibility of solid grains can be neglected $(C_s \approx 0)$. With infinitesimal transformation, Eq (C) 734 - 11) can be written using Eulerian porosity *n* and pore fluid's bulk modulus k_w (k_w =1/ C_w).

735
$$
du_w = \frac{d\varepsilon_v - C_s dp}{\phi(C_w - C_s)} \approx \frac{d\varepsilon_v}{nC_w} = \frac{k_w d\varepsilon_v}{n}
$$
 (C - 13)

Data availability statement

- The data used to support the findings of this study are available from the corresponding author
- upon reasonable request.

References

- [1] Vesic A S. Expansion of cavities in infinite soil mass[J]. Journal of Soil Mechanics & Foundations Div, 1972, 98(sm3).
- [2] Carter J P, Booker J R, Yeung S. Cavity expansion in frictional cohesive soils[J]. Géotechnique,
- 1986, 36 (3): 349-358.
- [3] Yu H S, Houlsby G T. Finite cavity expansion in dilatant soils: loading analysis[J]. Géotechnique, 1991, 41(2): 173-183.
- [4] Yu H S. Cavity Expansion Methods in Geomechanics[M]. Dordrecht, the Netherlands: Kluwer Academic Publishers, 2000.
- [5] Palmer A C, Mitchell R J. Plane-strain expansion of a cylindrical cavity in clay. Stress-strain
- behaviour of soils[C]. Proceedings of the Roscoe memorial symposium. Foulis, 1971: 588-599.
- [6] Collins I F, Yu H S. Undrained cavity expansions in critical state soils[J]. International journal
- for numerical and analytical methods in geomechanics, 1996, 20(7): 489-516.
- [7] Cao L F, Teh C I, Chang M F. Undrained cavity expansion in modified Cam clay[J]. Géotechnique, 2001, 51(4): 323-34.
- [8] Mo P Q, Yu H S. Undrained cavity expansion analysis with a unified state parameter model for clay and sand[J]. Géotechnique, 2017, 67(6): 503-515.
- [9] Chen S L, Abousleiman Y N. Exact undrained elasto-plastic solution for cylindrical cavity expansion in modified Cam Clay soil[J]. Géotechnique, 2012, 62(5): 447.
- [10] Chen S L, Abousleiman Y N. Exact drained solution for cylindrical cavity expansion in modified Cam Clay soil[J]. Géotechnique, 2013, 63(6): 510.
- [11] Chen S L, Abousleiman Y N. Drained and undrained analyses of cylindrical cavity contractions by Bounding Surface plasticity[J]. Canadian Geotechnical Journal, 2016: cgj-2015-0605.
- [12] Chen H, Li L, Li J, Wang H. Stress transform method to undrained and drained expansion of
- a cylindrical cavity in anisotropic modified cam-clay soils[J]. Computers and Geotechnics, 2019, 106: 128-142.
- [13] Sivasithamparam N, Castro J. Undrained expansion of a cylindrical cavity in clays with fabric anisotropy: theoretical solution[J]. Acta Geotechnica, 2018, 13(3): 729-746.
- [14] Chen S L, Liu K. Undrained cylindrical cavity expansion in anisotropic critical state soils[J]. Géotechnique, 2018, 69(3): 189-202.
- [15] Carter J P, Randolph M F, Wroth C P. Stress and pore pressure changes in clay during and after the expansion of a cylindrical cavity[J]. International Journal for Numerical and Analytical Methods in Geomechanics, 1979, 3(4): 305-322.
- [16] Hong P Y, Pereira J M, Tang A M, Cui Y J. A two-surface plasticity model for stiff clay[J].
- Acta Geotechnica, 2016, 11(4): 871-885.
- [17] Avgerinos V, Potts D M, Standing J R. The use of kinematic hardening models for predicting
- tunnelling-induced ground movements in London clay[J]. Géotechnique, 2015, 66(2): 106-120.
- [18] Avgerinos V, Potts D M, Standing J. The use of kinematic hardening models for predicting
- tunnelling-induced ground movements in London clay[J]. Géotechnique, 2016, 66(2): 106-120.
- [19] McDowell GR, Hau KW. A generalised Modified Cam clay model for clay and sand
- incorporating kinematic hardening and bounding surface plasticity. Granular Matter 2004;6:11-6.
- [20] Coussy O. Poromechanics. John Wiley & Sons Inc, 2004.
- [21] Spang B. Excel add-in for properties of water and steam in SI-units[J]. Water97_v13. xla. Hamburg, 2002.
- [22] Barnichon J D. Contribution of the bounding surface plasticity to the simulation of gallery excavation in plastic clays[J]. Engineering geology, 2002, 64(2-3): 217-231.
- [23] Cui Y J, Le T T, Tang A M, et al. Investigating the time-dependent behaviour of Boom clay under thermomechanical loading[J]. Géotechnique, 2009, 59(4): 319-329.
- [24] Mohajerani M, Delage P, Sulem J, et al. The thermal volume changes of the
- Callovo-Oxfordian claystone[J]. Rock mechanics and rock engineering, 2014, 47(1): 131-142.
- [25] Monfared M, Delage P, Sulem J, et al. A new hollow cylinder triaxial cell to study the behavior of geo-materials with low permeability[J]. International Journal of Rock Mechanics and Mining Sciences, 2011, 48(4): 637-649.
- [26] Van Marcke Ph, Li X L, Bastaens W; Verstricht J et al. The design and installation of the PRACLAY in-situ experiment[R]. Kessel-Lo: Peter De Preter,2013.
- [27] Charlier R, Chambon R, Collin F, Dizier A, Fauriel S, François B, Fokkens J, Garitte B, Gens
- A, Gerard P, et al. Timodaz report: Deliverable d13–simulation of lab and in situ tests[R]. 2010.
- [28] Russell A R, Muir Wood D. A comparison of critical state models for sand under conditions of axial symmetry[J]. Géotechnique, 2010, 60(2): 133-140.
- [29] Russell A R, Khalili N. On the problem of cavity expansion in unsaturated soils[J]. Computational mechanics, 2006, 37(4): 311-330.
- [30] Borja R I, Lin C H, Montáns F J. Cam-Clay plasticity, Part IV: Implicit integration of anisotropic bounding surface model with nonlinear hyperelasticity and ellipsoidal loading function[J]. Computer Methods in Applied Mechanics and Engineering, 2001, 190(26– 27):3293-3323.
- 806 [31] Rouainia M, Wood D M. A kinematic hardening constitutive model for natural clays with loss of structure[J]. Géotechnique, 2000, 50(2):153-164.
- [32] Hong P Y, Pereira J M, Cui Y J, et al. An elastoplastic model with combined isotropic–
- 809 kinematic hardening to predict the cyclic behavior of stiff clays[J]. Computers and Geotechnics, 2014, 62(oct.):193-202.
- 811 [33] McTigue, D. F. Thermoelastic response of fluid saturated porous rock[J]. Journal of Geophysical Research Atmospheres, 1986, 91(B9):9533-9542.
- [34] Mohajerani M, Delage P, Monfared M, et al. Oedometric compression and swelling
- behaviour of the Callovo-Oxfordia, argillite[J]. International Journal of Rock Mechanics &
- Mining Sciences, 2011, 48(4):606-615.
- 816 [35] Barnichon J D. Contribution of the bounding surface plasticity to the simulation of gallery excavation in plastic clays[J]. Engineering Geology, 2002, 64(2-3):217-231.
- [36] Yang J, Yin Z Y, Liu X F, et al. Numerical analysis for the role of soil properties to the load
- transfer in clay foundation due to the traffic load of the metro tunnel[J]. Transportation Geotechnics, 2020, 23:100336.
- 821 [37] Bian X, Hong Z S, Ding J W. Evaluating the effect of soil structure on the ground response
- 822 during shield tunnelling in Shanghai soft clay[J]. Tunnelling and Underground Space Technology
- incorporating Trenchless Technology Research, 2016, 58(sep.):120-132.
- 824 [38] Avgerinos V, Potts D M, Standing J R. The use of kinematic hardening models for predicting
- tunnelling-induced ground movements in London Clay[J]. Géotechnique, 2016, 66(2):1-15.
- [39] González N A, Rouainia M, Arroyo M, et al. Analysis of tunnel excavation in London Clay
- incorporating soil structure[J]. Géotechnique, 2012, 62(12):1095-1109.
- [40] Levasseur S, Y Malécot, Boulon M, et al. Soil parameter identification using a genetic
- algorithm[J]. International Journal for Numerical & Analytical Methods in Geomechanics, 2010, 32(2):189-213.
- [41] Jin Y F, Yin Z Y, Shen S L, et al. A new hybrid real-coded genetic algorithm and its
- 832 application to parameters identification of soils[J]. Inverse Problems in Science & Engineering,
- 2016:1-24.
- [42] Yin Z Y, Jin Y F, Shen S L, et al. An efficient optimization method for identifying parameters
- 835 of soft structured clay by an enhanced genetic algorithm and elastic–viscoplastic model[J]. Acta Geotechnica, 2016:1-19.
- [43] Jin Y F, Yin Z Y, Shen S L, et al. Investigation into MOGA for identifying parameters of a
- critical-state-based sand model and parameters correlation by factor analysis[J]. Acta Geotechnica, 2015, 454(5):1-15.
- 840 [44] Yin Z Y, Jin Y F, Shen S L, et al. Optimization techniques for identifying soil parameters in geotechnical engineering: Comparative study and enhancement[J]. International Journal for Numerical and Analytical Methods in Geomechanics, 2018, 42(1).
- [45] Jin Y F, Yin Z Y, Shen S L, et al. Selection of sand models and identification of parameters using an enhanced genetic algorithm[J]. International Journal for Numerical and Analytical Methods in Geomechanics, 2016, 40(8):1219-1240.
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л	к	$\mathcal V$	\overline{p}'_c : MPa	M_f	k_f
$0.18\,$	0.02	0.3	b	0.67	0.7
M_{g}	k_{g}	r_0	\boldsymbol{S}	A_d	
0.67	0.9		8	0.1	

Table 1. The selected parameters of ACC2 model for natural Boom clay

Case	OCR	σ' : MPa	σ'_θ : MPa	$\sigma'_{\overline{z}}$: MPa	k_f	k_{g}	S	A_d	r_0	\overline{p}' : MPa	K_0	v_0	s_u : MPa
	$\mathbf{1}$	$\overline{2}$	$\overline{2}$	$\overline{2}$	0.7	0.9	8	0.1	1	2	$\mathbf{1}$	1.76	0.60
2	$\mathbf{1}$	10	10	10	0.7	0.9	8	0.1	1	10	1	1.47	2.95
3	$\mathbf{1}$	50	50	50	0.7	0.9	8	0.1	1	50	$\mathbf{1}$	1.19	14.29
$\overline{4}$	$\mathbf{1}$	5.1	5.1	6	\ast	0.9	8	0.1	-1	\ast	0.85 1.59		1.55
5	$\mathbf{1}$	5.1	5.1	6	0.7	\ast	8	0.1	1	5.51	0.85	1.59	1.55
6	2.9	1.91	1.91	2.25	0.7	0.9	\ast	0.1	0.34	6	0.85	1.61	1.39
$7\overline{ }$	2.9	1.91	1.91	2.25	0.7	0.9	8	\ast	0.34	6	0.85	1.61	1.39

Table 2. Summary of material properties of natural Boom clay

v_s=1.84, *M_g*=0.67, '^{*} means different values are taken.