

A fatigue model for track-bed materials with consideration of the effect of coarse grain content

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Abstract

Previous studies showed that the permanent strain of interlayer soil in the French conventional railway substructure is highly dependent on the volumetric coarse grain 24 content f_v (volumetric ratio of coarse grain to total sample). This study developed a fatigue 25 model allowing the effects of coarse grain content f_v , stress state and number of loading cycles *N* on permanent strain to be accounted for. Data from the multi-stage loading cyclic tests of interlayer soil conducted at six different *f*v values (0%, 5%, 10%, 20%, 35% and 45%) and five different maximum deviator stress ∆*q*max values (10 kPa, 15 kPa, 20 kPa, 25 kPa and 30 kPa) were reviewed and used for this purpose. The model parameters were 30 determined by fitting the results from the tests at $f_v = 0\%$, 5% and 35%. In order to validate the proposed fatigue model, the determined model parameters were then used to simulate the 32 tests at $f_v = 10\%$, 20% and 45%. The results obtained showed that the proposed model can well describe the permanent strain after a certain number of loading cycles, in the case of plastic shakedown.

Keywords: coarse grain content; permanent strain; fatigue model; cyclic triaxial tests; soil fabric

1 INTRODUCTION

Under the effect of long-term train circulation in the French conventional railway track, a new layer named interlayer was created, mainly by interpenetration of ballast and subgrade. Considering the high bearing capacity of the interlayer material corresponding to a mixture of ballast grains and fine soils, which was characterized by its high dry density of 2.4 Mg/m^3 (Trinh 2011), the French railway company (SNCF) decided to keep it as part of substructure in the national track renewal program. Field investigation showed that the proportion of ballast grains decreased over depth. Roughly, the interlayer could be divided into upper part which is dominated by ballast grains and lower part which is dominated by fine soils (Trinh et al. 2012). For the upper part, the effects of fine content and water contents on permanent strain were studied by Trinh et al. (2012), Cui et al. (2013), Duong et al. (2013, 2014, 2016) and Lamas-Lopez et al. (2014, 2016) by performing monotonic and cyclic triaxial tests. The results showed that the higher the water content, the larger the permanent strain. At saturated state, the higher the fine content, the larger the permanent strain. On the contrary, at unsaturated state, the higher the fine content, the lower the permanent strain due to the contribution of suction generated inside the fines. Wang et al. (2018a, 2018b, 2018c) further 54 investigated the effect of volumetric coarse grain content f_v (volumetric ratio of coarse grain to total sample) on permanent strain using micro-ballast. A characteristic volumetric coarse grain content *f*v-cha was identified, below which the permanent strain decreased rapidly, and beyond which the permanent strain decreased relatively slowly. X-ray micro-tomography observation showed that the former case corresponded to a fine-matrix dominated structure, while the latter case corresponded to a coarse grain skeleton structure. Thus, it can be

deduced that the permanent deformation of interlayer soil increases over depth due to the 61 decreasing coarse grain content f_v . From a practical point of view, it is important to develop a 62 model, allowing the effect of f_v on permanent strain to be accounted for.

A few attempts have been made to describe the permanent strain with different factors such as number of loading cycles *N*, stress state, soil physical state (water content and dry density), etc. Based on experimental results, Barksdale (1972), Sweere (1990) and Hornych (1993) developed various empirical approaches to describe the effect of *N* on permanent strain, among which the model proposed by Hornych (1993) was validated by a large number of tests and was adopted in French standard (AFNOR 1995). In general, these models were developed based on cyclic tests subjected to a single-stage loading, which required a large number of tests for the determination of parameters. To reduce the number of tests and also the experimental dispersion related to samples variability, multi-stage loading was generally recommended. Gidel et al. (2001) applied multi-stage loading on unbound granular material, and found that the permanent strain increased significantly when the deviator stress exceeded the past maximum value. Based on the results obtained, Gidel et al. (2001) developed a model of permanent strain, accounting for both *N* and stress state. To investigate the effect of water content on permanent strain of fouled ballast, Trinh et al. (2012) performed multi-stage loading cyclic tests at various water contents. Based on the results obtained, a fatigue model considering the effects of water content, *N* and stress state was developed. More recently, Jing et al. (2018) proposed an approach to describe the permanent strain of granular materials in low-traffic pavements, taking the effects of fine content, water content, *N* and stress state into account. To the authors' knowledge, for the 82 interlayer soil of railway substructure, the effect of coarse grain content f_v on permanent strain has not been taken into account.

This study aims at developing a model of permanent strain for interlayer soil, accounting for the effects of number of loading cycles *N*, stress state and coarse grains content *f*v. Firstly, based on the multi-stage loading cyclic test results obtained by Wang et al. (2018c), a general form of the model accounting for *N*, ∆*q*max and *f*v was proposed. The model parameters were determined based on a part of cyclic tests from Wang et al. (2018c). In order to evaluate the performance of the proposed model, other tests were simulated using the parameters determined previously. The advantage and limitation of the model were also discussed.

2 MODELLING OF PERMANENT STRAIN

2.1 Review of multi-stage loading cyclic tests

Multi-stage loading cyclic tests were conducted on interlayer soil by Wang et al. (2018c). A material simulating the interlayer soil was reconstituted by mixing fines with micro-ballast at six different *f*v values (0%, 5%, 10%, 20%, 35% and 45%). The samples were prepared by dynamic compaction by keeping the fine soils inside the mixture at optimum water content $w_{opt} = 13.7\%$ and maximum dry density $\rho_{dmax-f} = 1.82 \text{ Mg/m}^3$, so that the suction developed inside the fines was expected to be similar for all samples. The effect of coarse grain content *f*v on permanent strain was investigated through cyclic triaxial tests and the results are shown in Fig. 1, with five different maximum deviator stress ∆*q*max values (10 kPa, 15 kPa, 20 kPa, 25 kPa and 30 kPa) and 90000 loading cycles for each ∆*q*max. It appears that the permanent 104 strain increased with the increasing loading cycles *N* and tended to stabilize at the end of 105 each loading stage for a given f_v value.

106 To visualize the soil fabric with different f_v values, X-ray μ CT scans were performed 107 on as-compacted samples at six different f_v values (Fig. 2). It is observed that with the 108 increase of f_v from 0% to 10%, the soil fabric was dominated by the fine soils, with coarse 109 grains floating in it. At $f_v = 20\%$, the contacts between aggregates started to develop, forming 110 local coarse grain skeletons by location. On the contrary, at $f_v = 35\%$ and 45%, the coarse 111 grains were in contact with each other, forming a global fabric of grain skeleton with fine 112 soils situated among grains. Thus, with the increase of f_v from 0% to 45%, the soil fabric 113 varies from a fine soils dominated structure to a coarse grain dominated structure.

114 **2.2 Development of a fatigue model**

Table 1 shows three widely applied fatigue models, with *N* by Hornych (1993), with *N* and ∆???????? by Gidel et al. (2001), with *N* and ∆???????? and *w* by Trinh et al. (2012), allowing the assessment of permanent strain produced under the effect of different variables. As this 118 study focuses on the modelling of the effect of f_v on permanent strain based on the cyclic test results obtained by Wang et al. (2018c) under constant water content condition, the effect of water content was not taken into account. Data from cyclic tests et different *f*v values and at various water content *w* values are needed to generalize the study to water content effect. 122 Most likely, the coupled effect of $f_v w$ should be considered in that case. Table 1 shows that the effects of *N* and other variables are separated to different terms (Gidel et al. 2001; Trinh 124 et al. 2012). Similarly, in this study, the proposed function *k* (????, Δ ??????????) is a term related 125 to the effects of f_v and Δq_{max} , while h (??) is a term related to *N*. The general form of this model is established as follows:

127
$$
\varepsilon_1^p(f_\nu, \Delta q_{max}, N) = k(f_\nu, \Delta q_{max}) \cdot h(N) \tag{1}
$$

128 where ε_1^p is the permanent strain, Δq_{max} is the deviator stress level.

129 To develop the model, the first step is to determine the form of $h(N)$. Adopting the 130 fatigue model *f* (*N*) proposed by Hornych (1993) for this purpose (Eq. (2)):

131
$$
f(N) = \varepsilon_1^{p*}(N) = \varepsilon_1^p(N) - \varepsilon_1^p(100) = A \cdot [1 - (\frac{N}{100})^{-B}]
$$
 (for *N* > 100 cycles) (2)

132 where ε_1^{p*} is the permanent strain after 100 cycles, parameter *A* represents the final 133 stabilized maximum permanent strain, parameter *B* controls the evolution of permanent 134 strain with increasing loading cycles *N*.

In order to consider the effect of ∆*q*max, Eq. (2) is modified to Eq. (3). This modification is motivated by the change of physical meaning of parameter *A* while accounting for ∆*q*max. As shown in Table 1, in the model of Hornych (1993), parameter *A* represents the stabilized maximum permanent strain. However, in the model considering *N* and ∆*q*max (Gidel et al. 139 (2001), Trinh et al. (2012)), parameter α is used. The value of this parameter is close to '1' $(a = 1.32$ in Gidel et al. (2001); $a = 0.76$ in Trinh et al. (2012)) and it definitely does not represent the maximum permanent strain.

142
$$
h(N) = a \cdot [1 - (\frac{N}{100})^{-B}]
$$
 (for $N > 100$ cycles) (3)

143 where B is a parameter.

144 After substituting Eq. (3) into Eq. (1), the fatigue model $\varepsilon_1^p(f_v, \Delta q_{max}, N)$ reads:

145
$$
\varepsilon_1^p(f_v, \Delta q_{max}, N) = k(f_v, \Delta q_{max}) \cdot a \cdot [1 - (\frac{N}{100})^{-B}] \text{ (for } N > 100 \text{ cycles)} \quad (4)
$$

7 146 Comparison between Eq. (4) and Eq. (2) shows that parameter '*A*' in Eq. (2) corresponds to 147 $\hat{i}k(f_v, \Delta q_{max}) \cdot a'$ in Eq. (4). Since parameter 'a' is close to unity, the physical meaning is 148 the same for ' $k(f_v, \Delta q_{max})$ ' and parameter '*A*'. Different from '*A*' representing the 149 maximum permanent strain (end-stage permanent strain), ' $k(f_\nu, \Delta q_{max})$ ' represents the 150 end-stage permanent strains at various loading levels ∆????????? for each *f*_v..

151 Prior to determining the form of $k(f_v, \Delta q_{max})$ in Eq. (4), the effects of coarse grain 152 content *f*v and deviator stress ∆*q*max on permanent strain need to be clarified. Fig. 3 shows the 153 variations of end-stage permanent strain ε_1^p as a function of coarse grain content f_v for 154 different Δq_{max} values. Note that the end-stage permanent strain ε_1^p was determined by a 155 method proposed by Gidel et al. (2001), which was later applied by Lamas-Lopez (2016) 156 and Wang et al. (2018c). The details of determination of that could be found in Wang et al. 157 (2018c). It is worth noting that, based on the results obtained by this method, the value of 158 end-stage permanent strain ε_1^p corresponds to that of maximum permanent strain at a given 159 *f*v and ∆*q*max values (Figure 3). It appears that a polynomial expression can be used to well describe their relationship. Fig.4 depicts the variations of the end-stage permanent strain ε_1^p 160 161 with ∆*q*max. Interestingly, a linear relationship is identified for all *f*v values. Thus, the 162 expression of $k(f_v, \Delta q_{max})$ can be formulated as follows:

163
$$
k(f_v, \Delta q_{max}) = \varepsilon_1^{p_0} \cdot [f_v^2 + bf_v + c] \cdot (\frac{\Delta q_{max}}{P_a} + d)
$$
 (5)

164 where $\varepsilon_1^{p_0}$, *b*, *c*, *d* are parameters, and P_a is atmospheric pressure, taken equal to 100 kPa.

165 In the model proposed by Trinh et al. (2012) (Table 1), a power relation was adopted to 166 relate the end-stage permanent strain to ∆*q*max at various water contents as follows:

167
$$
t(w, \Delta q_{max}) = \varepsilon_1^{p_0} \cdot (w + a_1) \cdot \left(\frac{\Delta q_{max}}{P_a}\right)^{\alpha}
$$
 (6)

168 where $\varepsilon_1^{p_0}$, a_1 and α are parameters, and $P_a = 100$ kPa.

169 A power relationship was obtained by Trinh et al. (2012) between the end-stage 170 permanent strain ε_1^p and Δq_{max} for three different water contents $w = 4\%$, 6% and 12% 171 (corresponding to $S_r = 32\%$, 48% and 100%, respectively). In the case of constant water 172 content considered in this study ($w_{opt-f} = 13.7\%$), a linear relationship is obtained with $\alpha = 1$. 173 Further examination reveals that the linear relationship is also valid when the soil is 174 unsaturated ($w = 4\%$ and $6\%)$ in the case of Trinh et al. (2012), as shown in Fig. 5. 175 After substituting Eq. (5) into Eq. (4), the fatigue model $\varepsilon_1^p(f_v, \Delta q_{max}, N)$ accounting 176 for the effect of coarse grain content *f*v, maximum deviator stress ∆*q*max and the number of

177 loading cycles *N* is obtained:

178
$$
\varepsilon_1^p(f_v, \Delta q_{max}, N) = \varepsilon_1^{p_0} \cdot [f_v^2 + bf_v + c] \cdot (\frac{\Delta q_{max}}{P_a} + d) \cdot a \cdot [1 - (\frac{N}{100})^{-B}]
$$

179 (for *N* > 100 cycles) (7)

180 where $\varepsilon_1^{p_0}$, *b*, *c*, *d*, *a* and *B* are parameters, and P_a =100 kPa.

181

182 **3 DETERMINATION OF MODEL PARAMETERS**

183 Wang et al. (2018c) investigated the effect of coarse grain content f_v on permanent strain 184 with six different *f*v values (0%, 5%, 10%, 20%, 35% and 45%). The measured data from the 185 tests at $f_v = 0\%$, 5%, 35% are used to determine the model parameters, with the following 186 two steps:

187 The first step is to determine four parameters $\varepsilon_1^{p_0}$, *b*, *c* and *d* by fitting Eq. (5) to the end-188 stage permanent strains ε_1^p at $f_v = 0\%$, 5%, 35%, as shown in Fig. 6. The values obtained 189 are $\varepsilon_1^{p_0} = 2.40, b = -1.03, c = 0.45, d = -0.05$.

190 The second step is to determine parameters a and B by fitting Eq. (7) to the measured 191 data at $f_v = 0\%, 5\%, 35\%$. The parameters obtained are $a = 1.20, B = 0.22$.

192 Fig. 7 presents a comparison between the fitting curves and the measured data at $f_v =$ 0%, 5%, 35%. It appears that the proposed fatigue model can well fit the experimental data. Moreover, better fitting can be obtained when the permanent strain stabilizes at the ends of loading stages.

After determining the model parameters, a sensitivity analysis of all parameters is 197 performed based on the results from the multi-stage loading cyclic test at $f_v = 5\%$ (Wang et al. 2018c), and the results are shown in Fig. 8 and Fig. 9.

199 Since $k(f_v, \Delta q_{max})$ controls the end-stage permanent strain, the effects of 200 parameters $\varepsilon_1^{p_0}$, *b*, *c* and *d* on permanent strain curve are explained separately in Fig. 8. Fig. 201 8a shows that the increase of $\varepsilon_1^{p_0}$ leads to larger increase of end-stage permanent strain, 202 suggesting that parameter $\varepsilon_1^{p_0}$ controls the amplitude of permanent strain curve. The effect of *f*v on permanent strain is reflected through parameters *b* and *c*. It can be observed that with 204 the increase of parameter *b*, the amplitude of permanent strain curve changes slightly (Fig. 8b). In addition, Fig. 8c shows that the increase of parameter *c* gives rise to an increase of 206 permanent strain, suggesting that parameter c controls the effect of f_v through the amplitude of permanent strain curve. Fig. 8d shows that the increase of parameter *d* results in parallel movement of permanent strain curve, indicating that parameter *d* mainly controls the interception of permanent strain curve.

210 Parameters a and B in $h(N)$ expression affect the evolution of permanent strain with loading cycles *N*. It can be observed in Fig. 9a that the larger the value of parameter *B*, the larger the increase of permanent strain rate and the smaller the loading cycles *N* needed for permanent strain stabilization. Therefore, parameter *B* governs the evolution of permanent

214 strain with increasing loading cycles *N,* which is consistent with previous studies (Hornych

- 215 (1993); Gidel et al. (2001); Trinh et al. (2012); Jing et al. (2018)). In addition, parameter a
- 216 affects the amplitude of permanent strain (Fig. 9b), with its value being around unity (i.e., α
- 217 = 1.32 in Gidel et al. (2001); $a = 0.76$ in Trinh et al. (2012); $a = 1.20$ in the present study).
- 218 **4 MODEL VALIDATION**
- 219 In order to evaluate the performance of the proposed fatigue model, the data from the multi-
- 220 stage loading cyclic tests at $f_v = 10\%$, 20% and 45% are simulated. The model parameters
- 221 determined previously based on the results at $f_v = 0\%$, 5%, 35% are used for this purpose.
- 222 Fig. 11 presents a comparison between the measured data and the corresponding simulated 223 ones. It appears clearly that the parameters determined with $f_v = 0\%$, 5% and 35% enable 224 satisfactory simulations of the tests at $f_v = 10\%$, 20% and 45%, with the coefficients of
- 225 determination R^2 above 0.94 at various f_v values, as shown in Table 2.
- 226

227 **5 DISCUSSION OF THE PROPOSED FATIGUE MODEL**

228 \qquad 5.1 The relation of f_y with parameters *b* and *c*

229 As shown in Eq. (5), the effect of f_v on the end-stage permanent strain is reflected through 230 parameters *b* and *c*. Based on the determined parameters $\varepsilon_1^{p_0}$ and *d*, it can be observed from 231 Fig. 10 that the end-stage permanent strain $\bar{\varepsilon}_1^p$ decreases with the increasing f_v at different 232 Δq_{max} values. In order to investigate the relation of f_v with parameters *b* and *c*, the effect of 233 Δq_{max} on the end-stage permanent strain ε_1^p is eliminated as follows:

234
$$
\bar{\varepsilon}_1^p = \frac{k(f_v \Delta q_{max})}{\varepsilon_1^{p_0} \cdot (\frac{\Delta q_{max}}{P_a} + d)} = f_v^2 + bf_v + c
$$
 (8)

235 The variation of $\bar{\epsilon}_1^p$ with f_v follows a polynomial relationship. When $f_v = 0$,

$$
c = \bar{\varepsilon}_1^p \tag{9}
$$

Thus, parameter *c* represents the end-stage permanent strain $\bar{\varepsilon}_1^p$ at $f_y = 0$.

238 The changing trend of $\bar{\epsilon}_1^p$ with f_v can be determined from Eq. (8):

$$
\frac{\partial \bar{\varepsilon}_1^p}{\partial f_v} = 2f_v + b \tag{10}
$$

240 Eq. (10) indicates that when the change of permanent strain $\bar{\varepsilon}_1^p$ with f_v becomes zero; i.e. $\frac{\partial \bar{\varepsilon}_1^p}{\partial \varepsilon_1^p}$ 241 i.e. $\frac{\partial \varepsilon_1}{\partial f_v} = 0$,

$$
b = -2f_v \tag{11}
$$

243 Considering that f_v can vary from 0 to 100%, parameter *b* ranges from 0 to -2.

244 Based on the aforementioned determined parameters *b* and *c*, Eq. (12) can be obtained by 245 substituting these values into Eq. (8):

$$
\bar{\varepsilon}_1^p = f_v^2 - 1.03f_v + 0.45\tag{12}
$$

It can be observed from Fig. 10 that the determined parameters allow a reasonable 248 description of the variation of end-stage permanent strain $\bar{\epsilon}_1^p$ with *f*_v at different ∆*q*_{max} values. The main discrepancy appears at ∆*q*max = 10 kPa, which is consistent with the observation shown in Fig. 7 and Fig. 11.

251 **5.2 Interpretation of permanent strain behaviors by shakedown theory**

252 In terms of permanent strain behaviors, three categories are defined in shakedown theory 253 (Werkmeister et al. 2001, 2004; Song et al. 2010): category A (plastic shakedown) characterized by stabilized permanent strain with loading cycles *N*, category B (plastic creep) characterized by failure at a large *N*, and category C (incremental collapse) characterized by failure at a small *N*. The criterion to classify the three categories is dependent on the accumulated permanent strain. Following the French standard AFNOR (2004), the limit of 258 category A is reached when $\varepsilon_{1\,5000}^{p} - \varepsilon_{1\,3000}^{p} > 0.45 \times 10^{-4}$, where $\varepsilon_{1\,5000}^{p}$ and $\varepsilon_{1\,3000}^{p}$ are accumulated permanent strains at *N* = 5000 and 3000, respectively. In all the tests conducted 260 by Wang et al. (2018c), the maximum difference between $\varepsilon_{1\,5000}^{p}$ and $\varepsilon_{1\,3000}^{p}$ occurs at f_v = 261 0% and $\Delta q_{\text{max}} = 30$ kPa, equal to 0.3×10^{-4} , smaller than the plastic shakedown limit. Thus, the response of all tests considered is within category A. Fig. 11 shows that the proposed fatigue model is relevant to describe the permanent strain behavior for category A. This confirms the assumption made by Hornych (1993) in their model that the permanent strain reaches a finite limit as loading cycles *N* tends toward infinite.

6 CONCLUSIONS

 268 In order to model the effect of f_v on permanent strain of interlayer soil, a fatigue model 269 $\varepsilon_1^p(f_v, \Delta q_{max}, N)$ was developed based on the results from multi-stage loading cyclic tests conducted by Wang et al. (2018c), at six different *f*v values (0%, 5%, 10%, 20%, 35% and 45%) and five different ∆*q*max values (10 kPa, 15 kPa, 20 kPa, 25 kPa and 30 kPa), with 90000 loading cycles for each ∆*q*max. The proposed fatigue model accounts for the effects of coarse grain content *f*v, maximum deviator stress ∆*q*max and loading cycles *N* on permanent 274 strain. The model parameters were determined by fitting the cyclic tests at $f_v = 0\%$, 5% and 275 35%, and then used to simulate the tests at $f_v = 10\%$, 20% and 45%. A good agreement was

It is worth noting that the proposed model is valid when the permanent strain stabilizes at a certain number of cycles *N*. In other words, it can only describe the permanent strain of 280 category A (plastic shakedown). Moreover, the fatigue model $\varepsilon_1^p(f_v, \Delta q_{max}, N)$ has not taken the effect of water content into account. Further experimental data are needed to take this effect into consideration. 283

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287

288 NOTATIONS

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Table 2. Coefficients of determination R^2 of cyclic test results at various f_v values

0% 5% 10% 20% 35% 45%			
R^2 0.95 0.97 0.94 0.97 0.94 0.94			

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