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1 An experimentally-determined general formalism for evaporation and isotope fractionation of

- 2 $\,$ Cu and Zn from silicate melts between 1300 1500 $^{\circ}\text{C}$ and 1 bar $\,$
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8 Abstract

- 9 Vaporisation fractionates elements and their isotopes between condensed phase(s) and the gas phase 10 according to two end-member regimes; kinetic (Langmuir) or equilibrium (Knudsen). The fractionation factor of isotopes i and j of element E between gas and liquid, ${}^{i/j}E(\alpha_{vap-lia})$, in the former case depends 11 only on the molar masses of the evaporating species, $(M_i/M_i)^{0.5}$, whereas, at equilibrium, fractionation 12 is ~1 at high temperatures. The prevailing regime depends on the production rate of vapour species 13 14 relative to their rate of transport away from the evaporating surface, for which an accurate theory is 15 lacking. Here, we present results of Cu and Zn isotope fractionation during evaporation of ferrobasaltic 16 melts in the FeO^(T)-CaO-MgO-Al₂O₃-SiO₂ (FCMAS) system in a 1 atm gas-mixing furnace at oxygen fugacities (fO_2) from 10⁻⁸ bar to 10^{-0.68} bar (air) at temperatures between 1300 and 1500 °C. In air, the 17 fractionation factors are ${}^{65/63}Cu(\alpha_{vap-liq}) = 0.9972 \pm 0.0001$ and ${}^{66/64}Zn(\alpha_{vap-liq}) = 0.9959 \pm 0.0002$, but 18 increase under reducing conditions, at log $fO_2 = -8$ for ${}^{65/63}Cu(\alpha_{vap-liq})$ (0.9979) and at -3, -5.5 and -8 for 19 Zn, at which ${}^{66/64}$ Zn($\alpha_{vap-liq}$) = 0.9967, 0.9974 and 0.9978, respectively. This behaviour is caused by slow 20 21 elemental diffusion through the silicate melt relative to the rate of evaporative loss, thereby depressing 22 ${}^{ij}E(\alpha_{vap-lia})$. When evaporation rates far exceed those for diffusion in the melt, no isotopic fractionation 23 develops in the condensed phase. To account for the ${}^{65/63}$ Cu($\alpha_{vap-liq}$) and ${}^{66/64}$ Zn($\alpha_{vap-liq}$) values observed in air, we develop a formalism for mass transfer applicable to any evaporating species over a range of 24 25 pressures, gas compositions and flow regimes. For natural convection at 1 bar, diffusive transport 26 through the gas is the rate-limiting step, where $D_{(i,j)k}$ is the diffusion of isotope i or j through a gas with mean molar mass M_k . Under these conditions ${}^{ij}E(\alpha_{vap-liq})$ is proportional to $(D_{ik}/D_{ik})^{2/3}$, and not (D_{ik}/D_{ik}) 27 28 as previously suggested. Our model predicts ${}^{ij}E(\alpha_{vap-lia})$ in other experiments, and in nature, to a 29 precision of ± 0.0005 assuming ideality. The fractionation factors inferred for moderately volatile 30 elements in lunar mare basalts (>0.9994) are inconsistent with a mass transport process, and instead 31 reflect near-equilibrium conditions of vapour loss from the Moon.
- 32
- 33 Key words: Evaporation, Vapour, Cu, Zn, Silicate melt
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- 37

38 **1.0. Introduction**

39 The phase transition from liquid- to gas, termed evaporation, is commonplace in geological processes. 40 Because the gas phase, as quantified by the ideal gas law, is less dense than condensed phases, mass 41 transport occurs more rapidly such that it readily escapes the system, leaving the residue depleted in 42 volatile components.

43 Two end-members styles of evaporation are classified according to the ease with which the gas phase 44 escapes (Fuchs, 1959; Chapman and Cowling, 1970). In natural processes, evaporation may fall 45 anywhere between the Langmuir (kinetic) and Knudsen (equilibrium) regimes. The former occurs when 46 each parcel of evaporating gas is perfectly and instantaneously removed from the evaporating surface, 47 and evaporation rate is therefore at a maximum (Langmuir, 1916). Knudsen evaporation, by contrast, 48 takes place when the vapour pressure of the evaporating species at the surface is equal to the equilibrium 49 partial pressure, such that the system has reached an equilibrium state (Knudsen, 1909). Physically, 50 these two regimes predominate for evaporation into a vacuum where gas escapes readily (Langmuir) or in a closed system where the gas phase remains in contact with the condensed phase(s) (Knudsen). The 51 52 geological importance lies in the potential for the evaporative regime to give rise to different chemical 53 and isotopic signatures in the condensed phase (e.g., Davis et al., 1990; Hashimoto, 1990; Humayun

54 and Cassen, 2000; Day and Moynier, 2014).

55 At high temperatures, the isotopic fractionation of volatile elements in geological materials is an ideal

record of evaporative style. This is because, for pure Langmuir evaporation, fractionation in the 56 57

abundances, X, of two isotopes, i and j of element E, between liquid (*liq*) and vapour (vap), defined as:

58
$${}^{i/j}E(\alpha_{vap-liq}) = \frac{({}^{i}X_{E}/{}^{j}X_{E}){}_{vap}}{({}^{i}X_{E}/{}^{j}X_{E}){}_{liq}}, (1)$$

is predictable as the inverse square root of the molar masses (M) of the evaporating species; $(M_i/M_i)^{0.5}$. 59

For the naturally-occurring isotopes, this quantity lies between 0.707 (H/D) and 0.998 (²⁰⁷Pb/²⁰⁸Pb). 60 Conversely, the isotopic fractionation at equilibrium is controlled only by the ratio of the equilibrium 61 partial pressures of the two isotopes; $p_{i,eq}/p_{j,eq}$, which, at high temperatures, is very near unity. 62 Therefore, isotopic fractionation caused by Langmuir evaporation is considerably larger than for 63

64 Knudsen evaporation.

65 In a geo- and cosmochemical context, semi-volatile metals, such as Cu, Zn and K (Palme et al., 1988; Sossi and Fegley, 2018) provide useful insight into such processes, because of their balanced 66 67 partitioning between vapour and condensed phases. That the isotopic fractionation of potassium 68 observed in meteorites by Humayun and Clayton (1995) was negligible within the analytical uncertainty 69 $(\pm 0.5 \%)$ was used to argue against Langmuir vaporisation as the predominant regime of vapour loss 70 in the solar nebula. This result was surprising, considering that the total pressures at the solar nebular 71 mid-plane were sufficiently low (~10⁻⁴ bar; Boss, 1998) so as to have facilitated near-pure Langmuir 72 evaporation.

73 Although subsequent studies with improved mass spectrometric methods were able to identify isotopic 74 fractionation in semi-volatile elements among a variety of terrestrial- and extraterrestrial materials 75 (Poitrasson et al., 2004; Luck et al., 2005; Moynier et al., 2006; Wombacher et al., 2008; Moynier et 76 al., 2009; Wang and Jacobsen 2016; Pringle and Moynier 2017), the fractionation factors inferred for 77 these processes were still much smaller than anticipated for evaporation into a vacuum. These results 78 precipitated renewed interest in the experimental characterisation of isotopic fractionation of semi-79 volatile elements, particularly K, Mg and Si, in silicate melts of planetary materials under vacuum 80 conditions (Richter et al., 2002; Yu et al., 2003; Richter et al., 2007; Knight et al., 2009; Mendybaev et 81 al., 2017). Through experiment, isotopic fractionation factors in multicomponent silicate systems never reached that expected for the ideal Langmuir case, $(M_i/M_i)^{0.5}$ (although see Dauphas et al. 2004 for 82

- 83 simple systems), and instead were observed to be closer to unity due to modification by *i*) the kinetics
- 84 of vaporisation, related to the energy barrier associated with evaporation at the surface (Hashimoto,
- 85 1990; Richter et al. 2002) and *ii*) the total pressure and mean molar mass of the gas medium into which
- 86 evaporation occurred (Richter et al. 2011).

87 The smaller isotopic fractionation factors relative to the Langmuir case inferred for semi-volatile 88 elements in lunar mare basalts (Paniello et al., 2012; Wang and Jacobsen, 2016; Boyce et al., 2018) led 89 to the realisation that isotopic signatures recorded in natural rocks are sensitive to the conditions at 90 which evaporation occurred. Wang and Jacobsen (2016) concluded that K loss during the Moon-91 forming giant impact must have taken place at high total pressures in order to dampen the isotopic fractionation factor from the Langmuir value $(M_{39}/M_{41})^{0.5} = 0.9753$ expected in a vacuum, to the ~0.9998 92 93 observed. A similar fractionation factor is also observed in Zn- (Paniello et al., 2012; Kato et al., 2015) 94 and Cu isotopes (Day et al., 2019) of mare basalts, suggesting that this is a general feature of evaporation

- 95 during high temperature processes.
- 96 Indeed, diminished isotope fractionation factors between vapour and liquid are also recorded in recent
- 97 impact melt glasses on Earth, formed via both asteroidal impacts (tektites, Moynier et al., 2009;
- Rodovska et al., 2017; Creech et al., 2019, melt sheets, Kamber and Schoenberg, 2020) and nuclear detonation (trinitites, Day et al., 2017) in which ${}^{i/j}E(\alpha_{van-lin}) > 0.998$. To place these results into context,
- 99 detonation (trinitites, Day et al., 2017) in which ${}^{i/j}E(\alpha_{vap-liq}) \ge 0.998$. To place these results into context, 100 Wimpenny et al. (2019), subjected silica-rich compositions, taken to approximate the upper continental-
- 101 crustal source rocks of terrestrial impact melts, to temperatures between 1600 and 2200 °C in an Ar
- 102 atmosphere. Although the experimentally-measured fractionation factors, 0.9988 $\leq \frac{66}{4} Zn(\alpha_{vap-lia}) \leq$
- 0.9998, span those observed in impact melt glasses, the influence of thermodynamic- (oxygen fugacity,
- 104 temperature) relative to kinetic variables (mass transport in the gas phase, diffusion in the liquid) on the
- 105 fractionation factor is yet to be quantitatively addressed.

In order to characterise the effects of the evaporative regime on isotopic fractionation of semi-volatile 106 107 metals from silicate melts, we present results of Cu and Zn vaporisation experiments under controlled 108 thermodynamic conditions in a vertical tube furnace at a total pressure of 1 bar and known gas 109 composition, which is independently varied to explore the effect of oxygen fugacity. We build on the 110 combined thermodynamic-theoretical framework established in Sossi et al., (2019) to develop a 111 formalism for the effect of mass transport of the gas phase on the vaporisation rate, in order to model 112 the chemical and isotopic effects of evaporation in natural processes in a predictive manner. We apply 113 our models to assess the likely regimes of evaporative loss that were extant during tektite formation and 114 on the Moon.

115 **2.0. Methods**

116 117

2.1. Experimental

Starting materials were made from a combination of high purity (>99.9 %) oxide powders of SiO₂, 118 119 Al₂O₃, MgO, CaCO₃, and Fe₂O₃ in proportions of the anorthite-diopside eutectic (An₄₂Di₅₈) with ~15 wt. % forsterite and ~15 wt. % Fe₂O₃ to resemble a primitive natural basalt with a liquidus temperature 120 121 ~ 1300 °C (O'Neill and Eggins, 2002; Sossi et al., 2019). The powders were mixed together three times 122 in an agate mortar under acetone, and the ensemble was then fired overnight in a 1 atm box furnace at 123 1000 °C in air to decarbonate the mixture. The oxides of Cu and Zn were then added as oxides in order 124 to achieve ~20,000 ppm in the final mixture (Cu-Zn mix) or ~1000 ppm (Metalloids mix). The powders 125 were mixed into a slurry using 100,000 molecular weight polyethylene oxide and water, and ~25 mg 126 was smeared onto noble metal wire loops (Pt, except for experiments at or below log/O_2 -5.5, for which 127 Re was used).

Experiments were performed in a 1 atm GERO vertical furnace with a 4.2 cm-diameter alumina tube,
heated by MoSi₂ elements housed at the Institut de Physique du Globe de Paris (Sossi et al., 2019). The

130 wire loops were inserted directly into the ~3 cm-long furnace hotspot at the set temperature and desired 131 fO_2 . Temperature was digitally monitored and adjusted as necessary with a Tektronix 2110 5¹/₂ Digit 132 Multimeter connected to a Type B (Pt₇₀Rh₃₀-Pt₉₄Rh₆) thermocouple bead placed <5 mm above the 133 sample, with temperature externally set by a Eurotherm ® controller found to be stable to better than ± 0.5 °C. Oxygen fugacity was allowed to equilibrate for ~10 minutes prior to sample introduction and 134 135 was controlled by CO-CO₂ gas mixing, metered by four MKS G-series mass flow controllers (2 with 500 sccm full scale for CO and CO₂, 1 at 50 sccm full scale for CO, and 1 at 10 sccm full scale for 136 CO₂). The mass flow controllers were calibrated using an SIRO₂ oxygen sensor at 1000 °C, giving an 137 138 uncertainty of ± 0.05 log units at the mixing ratios used in the experiments. Experiments in air were performed under no gas flow. Run time was recorded once the temperature reading at the thermocouple 139 140 reached ~99% of the set-temperature (~5 minutes) to allow the thermal mass of the sample to equilibrate 141 with the furnace atmosphere. Samples were rapidly quenched by having them drop into a bath of de-142 ionised water.

143

144 2.2. Electron Probe MicroAnalysis

145 Quenched glass spheres were mounted, together with their wires, in epoxy and sanded down so as to 146 expose the surface of the sphere along its central axis. Electron Probe MicroAnalysis (EPMA) was 147 performed on a Cameca SX-Five Electron Microprobe, housed at CAMPARIS, Université Pierre et 148 Marie Curie, Paris, France. Analyses were carried out with a defocused electron beam of 20 µm 149 accelerated at 15 kV and with a current of 20 nA. X-ray emission was counted by five Wavelength-Dispersive Spectrometers (WDS). The standards used for calibration were: anorthite (Si), albite (Na, 150 151 Al), periclase (Mg), haematite (Fe), diopside (Ca) and sanidine (K). Phengite was run as an internal standard throughout the sequence to verify the accuracy of the ZAF correction and monitor instrumental 152 153 drift. Approximately 20 - 40 points per sample were made, including profiles across the sphere in order 154 to detect any zoning in major element composition.

155 2.3. Laser-Ablation Inductively-Coupled Plasma Mass Spectrometry

156 The concentrations of Cu and Zn in a subset of the experimental glasses were determined by Laser-Ablation Inductively-Coupled Plasma Mass Spectrometry (LA-ICP-MS) at the Institute of 157 158 Geochemistry and Petrology, ETH Zürich, Switzerland (Guillong et al., 2014). The polished, epoxy-159 mounted glasses were placed in a dual-volume Laurin Technics 155 cell filled with a 0.7 L/min He 160 carrier gas. A Resonetics Resolution 193 nm ArF excimer laser with a repetition rate of 4 Hz and a total fluence of 3.5 J/cm² was used to ablate spots of 29 μ m diameter. The ablation sequence consisted of 20 161 162 s background and 40 s of counting time, in which the ablated material was carried to the Thermo Element XR magnetic sector mass spectrometer running in low resolution mode. Each mass peak is 163 164 measured three times (100 samples per peak with a mass window of 4%) for a total of 0.011 s each. The isotopic masses measured were: ⁷Li, ²³Na, ²⁹Si, ³⁹K, ⁴³Ca, ⁴⁹Ti, ⁵⁷Fe, ⁶³Cu, ⁶⁴Zn, ⁶⁵Cu, ⁶⁶Zn, resulting 165 in one sweep every 0.465 s. The ²³²Th¹⁶O/²³²Th ratio measured during tuning indicates that oxide 166 167 production was ~ 0.1 %.

168 Laser spot traverses of ~ 1,200 μ m in length consisting of 10 – 12 spots each were performed from the centre of the glass sphere to its edge for three glass beads, 26/12/18a, b, and c. Sample ablation was 169 170 bracketed by standards every ~20 points, which comprised a sequence of one NIST-610 synthetic glass 171 and two silicate glass standards (BCR-2G and GSD-1G). Standardisation was accomplished by 172 normalisation of the counts per second of a given isotope in the sample glass relative to those in NIST-173 610 in which Cu and Zn occur at 444 \pm 4 ppm and 433 \pm 7 ppm, respectively (Eggins and Shelley, 2002). Then, the counts of ²⁹Si were normalised against those obtained by EPMA (41.7 wt. % SiO₂ in 174 samples) to correct for different ablation yields of different matrices between ferrobasaltic glasses and 175 176 NIST-610. Relative standard deviation (RSD) was 1.3% for Cu and 2.0 % for Zn.

177 2.4. Isotope Ratio Measurement

178 The glass spheres were broken up and separated from the noble metal wire, before being crushed into a 179 fine powder using an agate mortar. Roughly 5 - 25 mg of powder was dissolved in a mixture of concentrated HNO₃-HCl-HF acids in Teflon beakers for 24 – 48 h at ~130 °C. The chromatographic 180 181 and mass spectrometric methods follow those outlined in Sossi et al. (2015). Following complete 182 dissolution, the samples were evaporated and re-dissolved in 6M HCl and loaded onto 1 mL of AG1-183 X8, Cl-form, 200-400 mesh anion exchange resin in high aspect ratio (0.4 cm radius \times 7 cm length) Teflon columns. Matrix elements (Mg, Ca, Ti, and most others) are eluted by passage of 5 mL of 6 M 184 185 HCl, whereas Cu is collected by another 9 mL 6 M HCl. The iron fraction was eluted by 3.5 mL of 0.5 M HCl, while Zn is finally eluted with 4 mL 3 M HNO₃. Total analytical blank quantities of Cu and Zn 186 187 are 1 ng, and 2 ng, respectively, negligible with respect to typical sample amounts (Cu, $Zn \approx 250$ to 188 400,000 ng).

189 The isotope composition of Cu and Zn was determined on a Thermo Neptune Plus MC-ICP-MS, housed at the Institut de Physique du Globe de Paris, with nine Faraday cups on $10^{11} \Omega$ resistors. Individual 190 191 eluates are dissolved in 2% (0.32 M) HNO₃ and introduced into the MC-ICP-MS by means of a 50 192 µl/min micro-flow glass nebuliser, creating an aqueous aerosol that enters a quartz-glass Scott double-193 pass cyclonic spray chamber before being ionised by an Ar plasma. Copper and Zn solutions are diluted 194 to 300 ppb. In order to correct for instrumental mass bias, each sample is bracketed by an international 195 reference material (SRM 976 for Cu and JMC-Lyon for Zn), and both samples and standards were 196 doped with an external spike element (Ni for Cu analyses, and Cu for Zn analyses) at the same 197 concentration as the analyte element. Copper and Zn isotope compositions are analysed in low 198 resolution mode on flat-topped peaks. Each analysis consists of 40 integrations of 4.194 s each. Isotope 199 ratios of Cu and Zn are expressed in delta notation, where:

200
$$\delta^{i}E = \left(\frac{\left({}^{i}X_{E}/{}^{j}X_{E}\right)_{sample}}{\left({}^{i}X_{E}/{}^{j}X_{E}\right)_{standard}} - 1\right) \times 1000 (2)$$

The value of *i* = 66 or 68 for Zn and 65 for Cu, whilst the value of *j* = 64 for Zn and 63 for Cu. Solutions were run 2 – 3 times each and compared to international reference materials analysed for quality control along with the samples yielding, for BHVO-2, δ^{65} Cu = 0.06 ± 0.03 ‰, δ^{66} Zn = 0.26 ± 0.05 and for BCR-2, δ^{65} Cu = 0.10 ± 0.04 ‰, δ^{66} Zn = 0.29 ± 0.01 ‰, resulting in total analytical uncertainties of ±

204 BCR-2, δ^{65} Cu = 0.10 ± 0.04 ‰, δ^{66} Zn = 0.29 ± 0.01 ‰, resulting in total ana 205 0.04 ‰ for δ^{65} Cu and ± 0.06 ‰ for δ^{66} Zn (both 2SD).

206

Table 1. Sample	run conditions,	their Cu	and Zn	abundan	ces and i	sotope o	compo	sitions relative	to the star	ting mater	rial (SM), and m	odelled l	og <i>K</i> * val	ues.					
Sample name	Temperature (°C)	CO (sccm)	CO ₂ (sccm)	$\log fO_2$	ΔFMQ	Time (mins)	Loop	Starting mix	Cu (ppm)	lnf(Cu)	log <i>K</i> *	δ ⁶⁵ Cusm	1 2SD <i>N</i>	Zn (ppm)	lnƒ(Zn)	log <i>K</i> *	δ ⁶⁶ Zns _M	1 2SDd	⁶⁸ Znsм2§	SD N
P 5/04/17b	1500	-	-	-0.68	4.72	60	Pt	Cu-Zn	6580	-0.90	-2.72	2.15	0.02 2	4983	-1.39	-2.7	5.54	0.07	10.79 0.	05 2
P 10/04/17a	1500	-	-	-0.68	4.72	15	Pt	Cu-Zn	11113	-0.38	-2.50	1.03	0.02 2	9137	-0.77	-2.36	2.18	0.01	4.24 0.	.05 2
P10/04/17a-r	1500	-	-	-0.68	4.72	15	Pt	Cu-Zn	11113	-0.38	-2.50	0.92	0.08 2	9137	-0.77	-2.36	2.17	0.06	4.29 0.	14 2
P 6/04/17c	1500	-	-	-0.68	4.72	120	Pt	Cu-Zn	3219	-1.61	-2.77	4.39	0.08 2	835	-3.16	-2.65	12.83	0.01	25.23 0.	.05 2
P 5/04/17a	1400	-	-	-0.68	5.62	60	Pt	Cu-Zn	9694	-0.51	-2.98	1.15	0.06 2	12403	-0.48	-3.18	1.79	0.01	3.58 0.	.08 2
P 7/04/17b	1400	-	-	-0.68	5.62	15	Pt	Cu-Zn				0.79	0.02 2				0.87	0.02	1.72 0.4	.02 2
P 6/04/17b	1400	-	-	-0.68	5.62	120	Pt	Cu-Zn	6939	-0.85	-3.06	2.03	0.06 2	6884	-1.05	-3.14				
P 4/04/17c	1300	-	-	-0.68	6.62	60	Pt	Cu-Zn	13978	-0.15	-3.54	0.36	0.09 2	16860	-0.16	-3.67	0.67	0.02	1.31 0.4	05 2
P 6/04/17a	1300	-	-	-0.68	6.62	120	Pt	Cu-Zn	11935	-0.30	-3.52	0.57	0.10 2	13962	-0.35	-3.63	0.94	0.01	1.86 0.4	.09 2
P 7/04/17a	1300	-	-	-0.68	6.62	15	Pt	Cu-Zn	15586	-0.04	-3.51	0.11	0.05 2	18881	-0.04	-3.62	0.30	0.04	0.60 0.4	.04 2
P 31/07/18a	1502	-	200	-2.74	2.64	15	Pt	Cu-Zn	8888	-0.60	-2.72	1.78	0.07 3	6360	-1.13	-2.82	4.17	0.01	8.18 0.	.09 3
P 31/07/18b	1502	-	20	-2.74	2.64	13	Pt	Cu-Zn	10140	-0.47	-2.77	1.01	0.05 3	6892	-1.05	-2.67	3.25	0.03	6.35 0.4	.04 3
P 21/06/18a	1500	-	200	-2.74	2.66	60	Pt	Metalloids	201	-1.60	-2.99			6	-5.07	-3.17				
P 01/08/18a	1397	-	200	-3.07	3.26	30	Pt	Cu-Zn	8533	-0.64	-3.15	1.60	0.05 3	4697	-1.44	-3.44	4.47	0.04	8.78 0.	04 3
P 01/08/18b	1396.6	-	20	-3.07	3.27	29	Pt	Cu-Zn	6628	-0.89	-3.06	2.51	0.04 3	2886	-1.92	-3.29	6.04	0.06	11.78 0.	14 3
P 19/06/18d	1400	-	200	-3.07	3.23	60	Pt	Metalloids	545	-0.61	-3.50			100	-2.30	-3.69	7.14	0.01	13.94 0.4	06 3
P 02/08/18a	1345.5	-	200	-3.26	3.57	55	Pt	Cu-Zn	7427	-0.78	-3.34	1.66	0.06 3	4434	-1.49	-3.85	4.62	0.03	9.09 0.	07 3
P 19/06/18a	1299	-	200	-3.44	3.87	67	Pt	Metalloids	682	-0.38	-3.86			533	-0.63	-4.51	1.86	0.09	4.06 0.	08 3
P 21/06/18b	1500	16	184	-5.50	-0.10	28	Pt	Metalloids	47	-3.06	-3.06			0.6	-7.42					
P 20/06/18a	1400	5.5	194.5	-5.51	0.79	30	Pt	Metalloids	244	-1.41	-3.45			3	-5.91					
P 22/06/18d	1400	5.5	194.5	-5.51	0.79	10	Pt	Metalloids						12	-4.30	-3.86	9.81*	0.01	19.35* 0.	01 3
P 19/06/18b	1299.5	1.6	200	-5.53	1.78	29	Pt	Metalloids	468	-0.76	-3.72			215	-1.40	-4.63	3.40	0.05	6.76 0.	02 3
P 01/08/18c	1396.6	6	194	-5.62	0.71	30	Re	Cu-Zn				2.88	0.08 3	5	-8.39		1.39*	0.02	2.69* 0.	04 2
P 31/07/18c	1501.7	20	180	-5.70	-0.31	8	Re	Cu-Zn	4279	-1.33	-2.79	3.44	0.02 3	8	-7.83		1.75*	0.01	3.62* 0.	15 2
P 3/08/18a	1347	4	196	-5.80	1.02	15	Re	Cu-Zn	7940	-0.71	-3.36	1.68	0.04 3	696	-3.35	-3.85	8.60	0.05	17.01 0.	02 3
P 25/07/18a	1398	9.5	190.5	-6.02	0.30	30	Re	Cu-Zn	2277	-1.96	-3.30	5.53	0.03 3	12	-7.38		0.60*	0.07	1.32* 0.	03 2
P 03/08/18b	1346.5	40.5	159.5	-7.99	-1.17	30	Re	Cu-Zn	6179	-0.96	-4.11	2.18	0.02 3	122	-5.09	-5.35	11.10	0.03	21.86 0.0	05 3
P 31/07/18d	1500.5	121.5	78.5	-8.00	-2.60	12	Re	Cu-Zn	303	-3.98	-3.15	8.81	0.07 3	7	-7.98		1.91*	0.11	4.00* 0.	18 2
P 19/06/18c	1299	24	176	-8.00	-0.69	17	Re	Metalloids	325	-1.12	-3.93			26	-3.51	-5.11	7.44	0.06	14.54 0.0	08 2
P 21/06/18c	1500	121.5	78.5	-8.00	-2.60	14	Re	Metalloids	12	-4.42	-3.23			0.5	-7.60					
P 22/06/18b	1500	121.5	78.5	-8.00	-2.60	7	Re	Metalloids						7	-4.81		8.70*	0.08	16.53* 0.	10 2
P 20/06/18b	1398	67	133	-8.03	-1.71	13	Re	Metalloids	91	-2.39	-3.48			0.4	-7.82					
P 01/08/18d	1396.6	66.5	133.5	-8.04	-1.70	30	Re	Cu-Zn	62	-5.56	-3.50	11.96	0.09 3	11	-7.45		1.11*	0.01	2.15* 0.0	04 2
Stand-alone expe	riments																			
P 26/12/18a	1300	2.7	197.3	-5.99	1.31	10	Re	Cu-Zn	9137	-0.57				9421	-0.54					
P 26/12/18b	1300	2.7	197.3	-5.99	1.31	20	Re	Cu-Zn	4786	-1.22				2860	-1.73					
P 26/12/18c	1300	24	176	-8.00	-0.69	5	Re	Cu-Zn	5321	-1.11				2256	-1.97					
*denotes samples	affected by con	ntaminat	ion; $N =$	number	of replic	ates; Δ	FMQ =	= log unit devia	tion in fO2	from the	Fayalite	e-Magne	tite-Quar	tz buffer;	sccm = s	standard	cubic c	entime	tres per m	ninute

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231

- 210 **3.0. Results**211
- 212 *3.1. Experimental Glasses*

A subset of glasses run at 1300, 1400 and 1500 °C, each at three log fO_2 (-3, -5.5 and -8), totalling nine samples, were analysed for their major element composition by EPMA. Samples at 1400 °C and 1500 °C quenched to glass spheres of \approx 1000 µm radius; whereas those performed at 1300 °C contained ~5 *wt.* % of olivine ± spinel crystals, as calculated by mass balance. The major element compositions of the wholly glassy experiments (T > 1300 °C) are homogeneous, with an average (expressed as *wt.* % oxide) of 41.70 ± 0.30 SiO₂, 10.60 ± 0.07 Al₂O₃, 15.54 ± 0.11 MgO, 14.58 ± 0.30 FeO^T, and 17.59 ± 0.41 CaO. The composition of each glass is reported in *Supplementary Table S1*.

220 No zoning in major elements as a function of sphere radius is observed due to their being non-volatile 221 at the experimental conditions. Three standalone experiments were run at 1300 °C for 10 and 20 minutes 222 at $\log fO_2 = -6$, and for 5 minutes at $\log fO_2 - 8$, in order to assess the degree of zoning of Cu and Zn at low temperatures and low fO_2 , where zoning should be most prevalent because the diffusion rate of the 223 224 volatile species through the melt decreases with temperature, while evaporation rate increases at more 225 reducing conditions (Sossi et al., 2019). Copper contents vary by <10% between the edge and the centre 226 of experiments run at $\log fO_2$ -6 (Fig. 1a, b), whereas at $\log fO_2$ -8 the outer 300 µm display a decrease 227 in concentration by up to 40 % relative to the interior (Fig. 1c). Zinc concentrations are zoned in all three experiments; with Zn_{rim}/Zn_{core} of 0.8 to 0.7 at log/O₂ -6 (Fig. 1a, b), and more markedly at log/O₂ 228 229 -8, where they are six times lower in the rim than in the core (Fig. 1c). Data for each zoning profile is 230 presented in Supplementary Table S2.



Figure 1. The fraction of Cu or Zn remaining in the glass as a function of distance from the centre of the sphere (in μ m) after evaporation at 1300 °C at **a**) logfO₂ = -6, *t* = 10 minutes, **b**) logfO₂ = -6, *t* = 20 minutes, and **c**) logfO₂ = -8, *t* = 5 minutes. Cu = black circles, Zn = white circles.

235 *3.2. Copper and Zinc concentrations*

In the two starting mixtures, labelled 'Metalloids' and 'Cu-Zn', Cu is present at 944 ± 12 ppm and 16177 ± 188 ppm, respectively, whereas Zn concentrations are 974 ± 21 ppm and 19747 ± 178 ppm. Bulk copper contents in the experimental glasses of the 'Metalloids' mix are between 682 ppm (run P19/06/18a) and 12 ppm (run P21/06/18c), while those for the 'Cu-Zn mix' fall within the range of 15586 ppm (run P07/04/17a) to 62.3 ppm in run P01/08/18d. Bulk zinc contents of the experimental glasses range from 533 ppm (run P19/06/18a) to 0.5 ppm (run P21/06/18c) in the 'Metalloids' mix and from 18881 ppm (run P07/04/17a) to 4.5 ppm in run P01/08/18c for the 'Cu-Zn' mix (Table 1).

Element depletions in the glasses are expressed as f(E) (E = Cu or Zn), where:

244
$$f(E) = \frac{X_E^t}{X_E^0} (3)$$

245 Where X_E refers to the concentration of the element E in the glass at time t and at time 0, respectively.

246 Calculated values of lnfCu and lnfZn positively co-vary and form discrete linear trends at logfO₂ -0.68

and -3 with intercepts within uncertainty of 0 (Fig. 2). For experiments in air, the relative depletion of

248 Zn relative to Cu (lnfZn/lnfCu) is approximately unity, meaning that both Zn and Cu vaporise to similar 249 extents. The average value is 1.12 ± 0.12 (N = 5) for experiments in air at 1300 °C and 1400 °C, while

relatively more Zn depletion is observed for the series at 1500 °C (1.85 ± 0.27 , N = 3). This behaviour

is predicted thermodynamically for the evaporation of Cu and Zn from basaltic melts, for which the

- vapour pressure of Zn increases more rapidly with temperature than does that of Cu (Sossi et al., 2019).
- 253



254

Figure 2. A plot of the natural logarithm of the fraction of Cu remaining in the melt (ln/Cu) compared with that of Zn (ln/Zn) in a given experiment for the Cu-Zn mix. The points form roughly linear arrays in log-log space for a given fO_2 , colour-coded by blue = air, green = pure CO₂ (log $fO_2 \sim -3$), yellow = log $fO_2 -5.5$, red = log $fO_2 -8$. The points qualitatively show that Zn becomes relatively more volatile with respect to Cu at lower fO_2 s, as expected according to their reaction stoichiometries. The effect of temperature is to favour Zn loss relative to Cu, though this is minor between 1300 °C and 1500 °C compared to changing fO_2 . Longer run times and higher temperatures result in a decrease in both ln/Cu and ln/Zn at a given log fO_2 .

262 Experiments performed at lower oxygen fugacities are sparse and do not permit assessment of any 263 temperature dependence. However, with decreasing fO_2 , lnfZn/lnfCu increases from 2.09 ± 0.17 (N = 264 5) in pure CO₂ experiments (log $fO_2 \approx -3$), 4.53 ± 0.86 (N = 3) at log $fO_2 \approx -5.5$ and the single reliable 265 point at logfO₂ -8 gives 5.30 (Fig. 2). The dependence of lnfZn/lnfCu with fO₂ stems from the stoichiometry of their respective vaporisation reactions. Copper is present as $CuO_{0.5}$ in silicate melts 266 267 (i.e., monovalent) and Zn occurs in divalent form as ZnO. However, the stable gas species of both is the monatomic gas (that is, Cu⁰ and Zn⁰; Lamoreaux et al., 1987) and their vaporisation reactions from 268 269 silicate melts are therefore written:

270
$$CuO_{0.5}(l) = Cu(g) + \frac{1}{4}O_2(4)$$

and, for Zn:

272
$$ZnO(l) = Zn(g) + \frac{1}{2}O_2 (5)$$

The n = 1 reaction of Cu means that the vapour pressure of Cu(g), pCu, is proportional to $(fO_2)^{-1/4}$ whereas pZn depends on $(fO_2)^{-1/2}$. Therefore, lower oxygen fugacities will promote relatively more Zn vaporisation with respect to Cu, resulting in progressively higher lnfZn/lnfCu, proportional to $(fO_2)^{-1/4}$.

In detail, the degree of elemental loss of both Cu and Zn depends on the physical properties of the silicate melt sphere, the experimental run time and the effective equilibrium constant of the reaction (K^*) . To quantify the effects of these variables on elemental loss, we perform a non-linear least-squares

- 279 minimisation to lnf(E) measured experimentally by varying $K^* (=K\gamma_{ev}\gamma_i)$, where K is the equilibrium
- 280 constant for reactions (4) and (5) in their standard states at *T* and 1 bar, γ_{ev} is the evaporation coefficient 281 and γ_i is the activity coefficient of the melt oxide component) in the equation developed by Sossi et al.
- 282 (2019):

283
$$\ln f(E) = \left(-\frac{K^*}{f(O_2)^{n/4}}\frac{3M}{r\rho}\sqrt{\frac{1}{2\pi M_i RT}}(t-t_0)\right).$$
(6)

284 Where n refers to the number of electrons exchanged in the vaporisation reaction (set equal to 1 for Cu and 2 for Zn; eqs. (4) and (5)). Other factors in the equation are known or controlled in each experiment; 285 286 r the radius of the sphere, p its density, M and M_i are the molar mass of the sphere and of the evaporating species respectively, R the gas constant, T the absolute temperature, t the experimental run time and t_0 287 the time at which the element begins evaporating. This treatment invokes equilibrium only insofar as 288 289 equations (4) and (5) are presumed to accurately describe the evaporation reactions occurring at the 290 melt surface (as verified experimentally; Sossi et al., 2019), and the fO_2 of the melt is that imposed by 291 the gas mixture. However, activity and evaporation coefficients of the evaporating species, as quantified 292 by fits to the experimental data with the K^* term, may deviate from unity, and hence from the 293 equilibrium conditions of Knudsen evaporation (e.g., Hoenig and Searcy, 1966).





Figure 3. Fitted values of $\log K^*$ expressed as a function of inverse temperature (1000/*T*) in Kelvin for **a**) Cu and b) Zn. Each point corresponds to a single experiment, where $\log K^*$ is calculated by minimising the misfit to the measured $\ln f(E)$ using equation (6). The colour corresponds to a different oxygen fugacity, as in Fig. 2, while circles stand for the 'Cu-Zn' mixture and squares the 'Metalloids' mixture. The straight line fits are calculated from linear regressions to the data (*T* in K) for the 'Cu-Zn mix' (this work, solid line), excluding points at $\log fO_2$ = -8 and -5.5 (for Zn) and $\log fO_2 - 8$ (for Cu), and to the data of Sossi et al. (2019) (dashed line).

The log*K** of reaction for both Cu and Zn define a linear relationships with inverse temperature, expressed as 1000/T (Fig. 3), ranging from ~-3.5 at 1300 °C to ~-2.5 at 1500 °C, where an increase denotes that the vapour species is increasingly favoured (eqs. 4, 5). Compared with the log*K** values in Sossi et al. (2019), in which silicate melts containing 1000 ppm Cu and Zn were evaporated, the log*K** calculated herein is generally ~0.5 log units higher. This is also verified from measurements of the

- 306 'Metalloids' mixture (~1000 ppm) which plot near the Sossi et al. (2019) determination, suggesting this
- 307 difference is likely because $CuO_{0.5}$ and ZnO in the Cu-Zn melts (~20,000 ppm) are no longer in the 308 Henry's Law region, resulting in differences in their activity coefficients. Also evident is a systematic
- decrease in $\log K^*$ as a function of $\log fO_2$ for both Cu (at $\log fO_2 8$) and Zn (at or below $\log fO_2 5.5$).
- 310 This attests to a decrease in the evaporation rate at that oxygen fugacity compared to that anticipated
- from equation (6) with n = 1 for Cu and n = 2 for Zn, for which log*K* should be independent of the fO_2 .
- 312 *3.3. Copper and Zinc isotope ratios*

The starting material (SM) has δ^{65} Cu of +0.09 ± 0.02 ‰ (CuO, Alfa Aesar) relative to SRM-976 and δ^{66} Zn = +0.16 ± 0.02 ‰ (ZnO, Alfa Aesar) relative to JMC-Lyon. All isotopic ratios are reported

relative to those of the starting materials ($\delta^{x}E_{SM}$), and are summarised in Table 1. Values of $\delta^{65}Cu_{SM}$

 $range from +0.11 \pm 0.05 \%$ (run P07/04/17a) to +11.96 ± 0.09 % (run P01/08/18d) and for δ^{66} Zn_{SM}

317 vary between $+0.30 \pm 0.04 \%$ (run P07/04/17a) to $+12.83 \pm 0.01 \%$ (run 06/04/17c).

318 All experiments had sufficient quantities of Cu remaining in the glass to permit their isotopic analysis. 319 For Zn, however, higher temperature experiments (\geq 1400 °C) at reducing conditions (logfO₂ -5.5 and -8) and longer run times (> 10 minutes) were poor in Zn. These samples, marked with an asterisk in 320 Table 1, deviate considerably from the lnf(E) vs. $\delta^{x}E$ trends defined by the other samples, indicative of 321 322 contamination by exchange with the furnace atmosphere (see Supplementary Information) and are not discussed further. The slope in δ^{68} Zn vs. δ^{66} Zn space is 1.962±0.008 with an intercept of -0.032 ± 0.041 323 324 (N = 20). The value of the slope theoretically reflects the mass fractionation law governing isotope fractionation, with an equilibrium process giving rise to a slope of 1.971 in δ^{68} Zn vs. δ^{66} Zn space 325 whereas purely kinetic fractionation yields 1.942. Following the approach of Young and Galy (2004) 326 and Wombacher et al. (2011), this dependence is better resolved in a plot of Δ^{68} Zn'_(smp-eq) vs. δ^{66} Zn (Fig. 327 4), where Δ^{68} Zn'_(smp-eq) = δ^{68} Zn_{smp}- δ^{66} Zn_{smp}×1.971, and 'smp' denotes the measured value. Although 328 329 some samples appear to follow the kinetic trend defined for the masses or reduced masses of Zn in air 330 (1.951) or CO₂ (1.954), deviation from the equilibrium line shows no apparent dependence on the logfO₂ 331 or temperature at which the sample equilibrated.



332

Figure 4. The Δ^{68} Zn'_(smp-eq) vs. δ^{66} Zn_{SM} of the experimental glasses. The slope of the line in δ^{68} Zn_{SM} vs. δ^{66} Zn_{SM} space is sensitive to the mode of isotopic fraction, in which, for the harmonic approximation, the kinetic and equilibrium end-members define slopes of 1.971 (a horizontal line in this representation) and 1.942, respectively. For kinetic transport in a diffusion-limited regime, the slope depends on the reduced masses, which gives 1.951

- for ambient gas with the molar mass of air (0.029 kg/mol), and 1.954 in pure CO_2 (0.044 kg/mol). Colours denote
- 338 the fO_2 of the experiment and are as per Fig. 1. Error bars are shown as 2SD.
- 339

For the isotopic evolution of a homogeneous and finite reservoir, the Rayleigh equation cast in termsof isotopic fractionation is written:

342
$$\frac{{}^{i}_{X_{E,liq}^{t}}/{}^{j}_{X_{E,liq}^{t}}}{{}^{i}_{X_{E,liq}^{0}}/{}^{j}_{X_{E,liq}^{0}}} = \frac{{}^{i/j}_{R_{E,liq}^{t}}}{{}^{i/j}_{R_{E,liq}^{0}}} = f_{E}^{(i'j_{E}\alpha_{vap-liq}-1)}.$$
(7)

343 The fractionation factor may be calculated from measured data according to the approximation:

344
$${}^{i/j}E(\alpha_{vap-liq}) = \left(\left(\frac{\delta^{i/j}E_{liq}}{\ln f_E}\right)\frac{1}{10^3}\right) + 1. (8)$$

345 Thus, the isotopic fractionation factor is determined by plotting δ^{65} Cu, δ^{66} Zn or δ^{68} Zn against ln*f*(Cu or 346 Zn) (Fig. 5a, b).



347

Figure 5. The isotopic composition of a) Cu, expressed as $\delta^{65}Cu_{SM}$ and b) Zn, expressed as $\delta^{66}Zn_{SM}$ (where 'SM' denotes the per mille deviation from the starting material), as a function of their respective relative abundances remaining in the glass, lnf(Cu) and lnf(Zn). Circles correspond to the 'Cu-Zn' mix, and squares to the 'metalloids' mix. The thin black lines are regressions through the data; for Cu, all data fall on a single line with a fractionation factor, ${}^{65/63}Cu(\alpha_{vap-liq}) = 0.9972$, save for the three samples equilibrated at $logfO_2 = -8$, which define ${}^{65/63}Cu(\alpha_{vap-liq}) = 0.9979$. For Zn, ${}^{66/64}Zn(\alpha_{vap-liq})$ decreases as a function of fO_2 , from 0.9959 in air, 0.9967 at $logfO_2 \approx -3$, 0.9974 at $logfO_2 \approx -5.5$ and 0.9978 at $logfO_2 = -8$.

For Cu, there is no correlation between ${}^{65/63}$ Cu($\alpha_{vap-liq}$) and temperature or run duration. For ${}^{65/63}$ Cu($\alpha_{vap-liq}$) 355 lig) calculated for different fO₂ series (-0.68, -3, -5.5, -8), the three most oxidised series define the same 356 fractionation factor, 0.9972 ± 0.0001 (N = 17) (Fig. 5a), whereas at log/O₂ -8 the fractionation factor is 357 smaller, ${}^{65/63}Cu(\alpha_{vap-lia}) = 0.9979 \pm 0.0001$ (N = 3). Both series have intercepts ($\delta^{65}Cu_0$) very near 0; -358 0.18 ± 0.08 % and +0.17 ± 0.21 %, respectively. For Zn, both Cu-Zn and Metalloids mixes give 359 consistent values, with a difference in ${}^{66/64}$ Zn($\alpha_{vap-lia}$) observed at each logfO₂; 0.9959 ± 0.0002 (N = 8) 360 at -0.68, 0.9967 ± 0.0002 (N = 7) at -3, 0.9974 (N = 2) at -5.5 and 0.9978 (N = 2) at -8 (Fig. 5b). At at 361 $\log fO_2 = -0.68$, $\delta^{66}Zn_0$ is -0.35 ± 0.23 % while $\delta^{66}Zn_0 = -0.07 \pm 0.34$ % at $\log fO_2 = -3$, whereas the two 362 reducing series had their intercept forced through 0 due to the lack of points. Regressions not forced 363 through the origin yield ${}^{66/64}$ Zn($\alpha_{vap-liq}$) = 0.9973 and 0.9977 at logfO₂ = -5.5 and -8, respectively. 364

365 **4.0. Discussion**

367 368 4.1. Diffusion and the effect of oxygen fugacity on elemental loss and the vapour-liquid 368 *fractionation factor*

366

The observation that the apparent isotopic fractionation factors of Cu and Zn between liquid silicate 369 370 and the gas phase decrease as a function of oxygen fugacity behaves an explanation. Over the range of fO_2 investigated, thermodynamic stability of the gas species for Cu and Zn should remain unchanged, 371 with Cu⁰ and Zn⁰ predominating under all conditions (Lamoreaux et al., 1987; Sossi et al., 2019). 372 Although Cu may also exist in its 2+ oxidation state in silicate melts at high oxygen fugacities (*e.g.*, in 373 374 air), the observed shift in ${}^{65/63}$ Cu($\alpha_{vap-lia}$) occurs at logfO₂ between -6 and -8; too reducing for Cu²⁺ to be 375 stable (Holzheid and Lodders, 2001). On the other hand, Zn only exists as Zn^{2+} at all oxygen fugacities, meaning the systematic change in fractionation factor is not readily ascribed to a change in liquid or gas 376 377 speciation as a function of fO_2 .

378 The shift does coincide, however, with the appearance of zonation in both elements in the melts; for the 379 experiment at $\log fO_2$ -8 and 1300 °C (26/12/18c) for Cu, and below $\log fO_2$ -6 for Zn (26/12/18a, b; Fig. 380 1). Formation of such a chemical and isotopic boundary layer at the evaporating surface may cause deviations of the fractionation factor between vapour - liquid inferred from the measurement of the 381 382 bulk glass relative to cases in which the glass is homogeneous. The magnitude and sense of this isotopic 383 divergence depend on the relative timescale of the element's evaporation rate vs. its homogenisation 384 rate in the melt (which, for a sphere in the absence of a thermal gradient, can only occur by diffusion) and the difference in diffusion rates between the two isotopes in the melt (Young, 2000; Richter, 2004; 385 386 Moynier et al., 2009).

Thus, if the vaporisation rate at the surface is known, the elemental zoning profiles, in conjunction with the observed ${}^{ij}E(\alpha_{vap-liq})$, can be used to derive *i*) the elemental diffusion coefficient, *D* and *ii*) the relative differences in diffusion coefficients between two isotopes through the silicate melt. In order to do so, a central finite difference discretisation diffusion model in spherical co-ordinates (Crank, 1975; Ford-Versypt and Braatz, 2014) is implemented (*Appendix A1*). The model approximates the diffusion of an element or isotope through the silicate melt medium with a time-dependent boundary condition set by its evaporation at the surface of the bead.

The K^* value in eq. 6 is varied in order to produce the correct value of $X_{Cu,Zn}^t$ observed at the surface, taken to represent the steady-state value due to evaporation. Then, the value of *D* is varied in order to minimise the misfit to the objective function;

397
$$\chi^2 = \frac{\Sigma(X_{Cu,Zn,r}^t(obs) - X_{Cu,Zn,r}^t(calc))^2}{\Sigma\sigma(obs)}$$
(9)

398 Where χ^2 quantifies the sum of the misfit between the normalised concentration at each value of *r* 399 (radial distance from the centre of the bead) that are observed (obs) and calculated by the model (calc) 400 given the experimental run time, *t*. Results are shown in Table 2 and Fig. 6.

401 The fitted diffusion coefficient of Zn in ferrobasaltic melt is consistent among the three experiments, 402 $1.56 \pm 0.25 \times 10^{-9}$ m²/s at 1300 °C. There are no measurements of Zn diffusion coefficients in relevant compositions, however, tracer diffusivities of other divalent metal cations (Co^{2+} , Mn^{2+}) in basaltic melts 403 are ~ 10^{-10} m²/s (Lowry et al., 1982) at the same temperature. For Cu, the value of 2.61×10^{-9} m²/s 404 determined herein from a single experiment is nearly an order of magnitude higher than measured by 405 Ni and Zhang (2016) in a basaltic melt at 1300 °C (~ 4×10^{-10} m²/s). However, given the empirical 406 dependence of logD on 1/n (e.g., Mungall, 2002), and the factor of 10 lower viscosity of the melt 407 composition used here, ~2.3 Pa.s, compared to the experimental basaltic melts of Lowry et al. (1982) 408 409 and Ni and Zhang (2016), both ~ 27 Pa.s at 1300 °C, the values of D would be expected to be an order of magnitude higher. 410

411 Isotopic composition is predicted by constructing two finite difference profiles; one for each isotope.

- 412 The fractionation factor between liquid and vapour at the boundary of sphere is modified by adjusting
- 413 the ratio of the equilibrium constants of the isotope vaporisation reactions (K^*/K^*_j ; eqs. A4 and A5) to
- 414 yield the expected value of ${}^{i/j}E(\alpha_{vap-liq})_{surf}$ under conditions that are not diffusion-limited (*i.e.*, in air; 415 0.9959 for ${}^{66/64}Zn$, 0.9972 for ${}^{65/63}Cu$). Tracer diffusivity of two isotopes in a given medium is
- 415 0.9959 for ^{66/64}Zn, 0.9972 for ^{65/63}Cu). Tracer diffusivity of two isotopes in a given medium is 416 proportional to the inverse ratio of their masses, related by an exponent, β , i.e., $(M_j/M_i)^{\beta}$. Because the
- 417 isotopic composition of the bulk sample is unknown, β cannot be determined independently, and must
- 418 be assumed. By analogy with the diffusion of other divalent first-row transition metal cations in silicate
- 419 melts, we adopt a value of $\beta = 0.015 \pm 0.010$ (Richter et al., 2009). This results in an isotopic
- 420 fractionation factor due to diffusion, ${}^{i/j}E(\alpha_{diff})$ of 0.9998 ($\beta = 0.005$) to 0.9993 ($\beta = 0.025$).

measured for elemental zoning profiles, and the associated model parameters and results, assuming β = 0.015.26/12/18a26/12/18b26/12/18clogfO2-6-6Time (mins)1020D0 (m²/s)1.56(0.18) × 10-91.25(0.08) × 10-91.56(0.18) × 10-91.25(0.08) × 10-91.75(0.05) × 10-9f(Zn or Cu) _{surf} 0.460.130.050.450.150.120.31logK* _{surf} -4.84-4.73-4.96-3.30-4.96-5.11-3.37
$\begin{array}{c c c c c c c c c c c c c c c c c c c $
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
Time (mins)10205ElementZnZnZnZnCu $D_0 (m^2/s)$ $1.56(0.18) \times 10^{-9}$ $1.25(0.08) \times 10^{-9}$ $1.75(0.05) \times 10^{-9}$ $2.61(0.33) \times 10^{-9}$ $f(Zn \text{ or } Cu)_{surf}$ 0.46 0.13 0.05 0.25 $f(Zn \text{ or } Cu)_{bulk}$ 0.49 0.15 0.12 0.31 $\log K^*_{surf}$ -4.84 -4.73 -4.96 -3.30 $\log K^*_{bulk}$ -4.88 -4.76 -5.11 -3.37
ElementZnZnZnCu $D_0 (m^2/s)$ $1.56(0.18) \times 10^{-9}$ $1.25(0.08) \times 10^{-9}$ $1.75(0.05) \times 10^{-9}$ $2.61(0.33) \times 10^{-9}$ $f(Zn \text{ or } Cu)_{surf}$ 0.46 0.13 0.05 0.25 $f(Zn \text{ or } Cu)_{bulk}$ 0.49 0.15 0.12 0.31 $\log K^*_{surf}$ -4.84 -4.73 -4.96 -3.30 $\log K^*_{bulk}$ -4.88 -4.76 -5.11 -3.37
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
$f(Zn \text{ or } Cu)_{surf}$ 0.460.130.050.25 $f(Zn \text{ or } Cu)_{bulk}$ 0.490.150.120.31 $\log K^*_{surf}$ -4.84-4.73-4.96-3.30 $\log K^*_{bulk}$ -4.88-4.76-5.11-3.37
$f(\text{Zn or Cu})_{\text{bulk}}$ 0.490.150.120.31 $\log K^*_{\text{surf}}$ -4.84-4.73-4.96-3.30 $\log K^*_{\text{bulk}}$ -4.88-4.76-5.11-3.37
$\log K^*_{surf}$ -4.84-4.73-4.96-3.30 $\log K^*_{bulk}$ -4.88-4.76-5.11-3.37
$\log K^*_{\text{hulk}}$ -4.88 -4.76 -5.11 -3.37
t_{evap} (s) 1176 1379 316 435
δ^{66} Zn / δ^{65} Cu (‰) (calc) 2.93 7.88 6.85 3.16
$^{ij}E(\alpha_{vap-liq})_{surf}$ (assumed) 0.9959 0.9959 0.9959 0.9972
$^{ij}E(\alpha_{vap-liq})_{bulk}$ (calc) 0.9959 0.9959 0.9968 0.9973

421



422

423 **Figure 6.** Laser-Ablation ICP-MS data for Zn abundances (white circles) as a function of core (0 μm) to rim 424 (~1200 μm) in experimental glass spheres synthesised at 1300 °C; **a**) 26/12/18b, t = 20 mins, $\log/O_2 = -6$ and **b**) 425 26/12/18c, t = 5 mins, $\log/O_2 = -8$. Overlain on the data are, on the primary ordinate axis, the finite-difference 426 model fit to the Zn abundances measured (solid black curve), and on the secondary ordinate axis, the modelled 427 δ^{66} Zn_{SM} evolution with $\beta = 0.015$ as a function of radius (dashed black curve). The boundary condition is set by 428 evaporative loss according to eq. (6) for both ⁶⁶Zn and ⁶⁴Zn, with the constraint that vaporisation rates at the 429 surface are ^{66/64}Zn($\alpha_{vap-lig}$) = 0.9959.

430 For $\beta = 0.015$, the isotopic composition of Zn (or Cu) in the centre of the bead is lighter than at the 431 boundary, where ${}^{ij}E(\alpha_{vap-liq})_{surf}$ is fixed (Fig. 6). This may seem counterintuitive, because the lighter 432 isotope is able to diffuse more quickly than the heavier isotope, and therefore reaches the surface more 433 rapidly. However, the key factor controlling whether the interior of the bead is isotopically heavy or 434 light relative to the surface is the ratio of isotopic fractionation factor due to diffusion, ${}^{ij}E(\alpha_{diff})$ to the

- 435 isotopic fractionation factor due to evaporation, ${}^{i/j}E(\alpha_{vap-liq})$. Where ${}^{i/j}E(\alpha_{diff}) > {}^{i/j}E(\alpha_{vap-liq})_{surf}$, evaporation
- induces larger isotopic fractionation than can be compensated for by the faster diffusion of the lighterisotope relative to the heavier isotope, and the interior remains lighter than the rim, yet both are enriched
- 437 isotope relative to the heavier isotope, and the interior remains lighter than the rim, yet both are enriched 438 relative to the initial composition. This causes the bulk ${}^{ij}E(\alpha_{vap-liq})_{bulk}$ value to increase (i.e., smaller
- fractionation) relative to that predicted by ${}^{ij}E(\alpha_{vap-liq})_{surf}$ (Table 2). However, as β increases such that
- 440 ${}^{ij}E(\alpha_{vap-liq})$ surf, then ${}^{ij}E(\alpha_{vap-liq})$ surf, then ${}^{ij}E(\alpha_{vap-liq})$ surf, is lower (i.e., larger fractionation factor) than ${}^{ij}E(\alpha_{vap-liq})$ surf,
- 441 because the heavier isotope is unable to diffuse sufficiently rapidly to the surface, and becomes
- 442 increasingly concentrated in interior of the bead. This phenomenon is illustrated graphically in *Fig. A1*.
- At the constant value of $\beta = 0.015$ used to model the data, then, the degree to which ${}^{i/j}E(\alpha_{vap-lia})_{bulk}$ 443 increases (i.e., fractionation factor becomes closer to unity) relative to ${}^{ij}E(\alpha_{vap-liq})_{surf}$ is proportional to 444 the timescale of evaporation relative to diffusion, denoted t_{diff}/t_{evap} . Experimental charges at log/O₂ -6 445 446 are predicted to show only little- to modest changes in ${}^{ij}E(\alpha_{vap-liq})_{bulk}$ compared to ${}^{ij}E(\alpha_{vap-liq})_{surf}$; as 447 illustrated by the similar isotope composition of their interiors relative to the boundary layer (Fig. 6a). On the other hand, δ^{66} Zn is predicted to be lower by ~ 8 % in the interior relative to the rim in the run 448 at log fO_2 -8 (Fig. 6b), causing an increase in ${}^{ij}E(\alpha_{vap-liq})_{bulk}$ (0.9968) relative to ${}^{ij}E(\alpha_{vap-liq})_{surf}$ (0.9959). 449 Given that the diffusion rate is near-constant with fO_2 (Table 2) and temperature is constant, this 450 phenomenon arises due to the faster evaporation rate of Zn at low fO_2 (eq. 5). The characteristic 451 452 evaporation timescale, t_{evap} (*i.e.*, the time taken to evaporate $(1-f(E)_{surf})$ relative to the experimental run 453 time, t_{exp}), is given by:

454
$$t_{evap} = \frac{t_{exp}}{(1 - f(E)_{surf})}(10)$$

455 It is important to note that $(1-f(E)_{surf})$ is the fractional loss observed at the surface boundary layer, not 456 that integrated throughout the entire bead. Whereas the diffusion timescale is given by (Crank, 1975):

457
$$t_{diff} = \frac{1}{2} \frac{r^2}{D} (11)$$

458 With this in mind, t_{evap} is shown to be a factor of ~4 faster at log/O₂ = -8 than at log/O₂ = -6 (Table 2), 459 giving rise to t_{diff}/t_{evap} of ~0.9 and ~0.28, respectively. The effect of t_{diff}/t_{evap} on ${}^{i/j}E(\alpha_{vap-liq})_{bulk}$ follows a 460 logistic function (Fig. 7), where, for $\beta = 0.015$:

461
$$\frac{i/j}{E(\alpha_{vap-liq})_{bulk}} = \frac{\left(1 - \frac{i}{j}E(\alpha_{vap-liq})_{surf}\right)}{1 + \exp\left(-3.85\left(\frac{t}{diff}_{tevap}-1.24\right)\right)} + \frac{i}{j}E(\alpha_{vap-liq})_{surf}(12)$$

462



463

Figure 7. The dependence of ${}^{ij}E(\alpha_{vap-liq})_{net}$ on the relative characteristic timescales of evaporation (t_{evap}) and diffusion (t_{diff}), assuming diffusion in the liquid is proportional to (M_j/M_i)^{β}, where $\beta = 0.015$ (solid line) and 0.005 and 0.030 (dashed lines). Model results (eq. 12) for the predicted ${}^{ij}E(\alpha_{vap-liq})_{net}$ in experiments 26/12/18a-c (1300°C) are shown as yellow (logfO₂ -6) and red (logfO₂ -8) circles, assuming ${}^{ij}E(\alpha_{vap-liq})_{surf} = 0.9959$. The measured ${}^{ij}E(\alpha_{vap-liq})_{net}$ from other experimental runs at logfO₂s -0.68, -3, -5.5 and -8 (blue, green, yellow and red, respectively) are shown as horizontal lines.

470 The predicted increase in ${}^{ij}E(\alpha_{vap-liq})_{net}$ falls short of that measured (Fig. 5) for a given fO_2 , as shown by 471 the horizontal lines on Fig. 7. Overlap between the red and yellow points with their respective coloured 472 horizontal lines would constitute perfect agreement. However, given the uncertainties in the value of β 473 and in the fractionation factor itself (especially considering the Cu and Zn isotope compositions of the 474 zoned standalone samples were not determined), high t_{diff}/t_{evap} at lower fO_2 seems the most likely cause 475 of increasing ${}^{ij}E(\alpha_{vap-liq})_{net}$ observed.

476

477 *4.2. A general law for vaporisation*

The Hertz-Knudsen-Langmuir (HKL) equation provides a quantitative means of assessing the mechanisms of elemental and isotopic fractionation due to evaporation that are observed experimentally. The degree to which gas molecules evaporating at the surface of a melt sphere equilibrate with the melt depends on the rate with which they are transported away from the surface, relative to the rate at which they are produced, a relationship described numerically;

483
$$\left(\frac{dn_i}{dt}\right)_{net} = -4\pi r^2 \frac{\gamma_{ev} p_{i,eq} - \gamma_{cn} p_{i,s}}{\sqrt{2\pi R M_i T}}.$$
(13)

Equation (13) states that the molar rate at which a species, *i*, in an ideal gas with a Maxwell-Boltzmann distribution of kinetic energies impinges upon a spherical surface is proportional to difference between the equilibrium partial pressure of that species ($p_{i,eq}$) and its actual pressure at the boundary layer of the evaporating surface, $p_{i,s}$, multiplied by their evaporation (γ_{ev}) and condensation (γ_{cn}) coefficients, respectively. Although the value of $p_{i,s}$ is not readily measured (*e.g.* by a probe that would itself perturb the boundary layer), it can be estimated by considering that, in a system with finite quantity of *i*, the net 490 production of gaseous molecules at the evaporating surface and their molar removal rate (mol/s) by 491 mass transport must be equal, *i.e.*, $\left(\frac{dn_i}{dt}\right)_{net} = \left(\frac{dn_i}{dt}\right)_{trans}$, where $\left(\frac{dn_i}{dt}\right)_{trans}$ is given by (Bartlett, 1967):

492
$$\left(\frac{dn_i}{dt}\right)_{trans} = -4\pi r^2 k_c \frac{(\gamma_{cn} p_{i,s} - p_{i,\infty})}{P} (1 - \exp(\xi) \operatorname{erfc}\sqrt{\xi}), (14)$$

Here, $\xi = \frac{D_{ik}t}{2r^2}$, where D_{ik} the diffusion rate of species *i* through the gas otherwise composed of 493 molecules with an average molar mass of k, r is the radius of the sphere, designates the approach to 494 495 steady state conditions, which, in our experiments occurs after ~5 s ($\xi > 500$). At steady state, the mass 496 transport rate is thus proportional to the partial pressure difference between $p_{i,s}$ and $p_{i,\infty}$ at an infinite distance from the boundary layer (taken here to be 0), related by the reciprocal total pressure (P) and 497 the mass transfer coefficient, k_c . This quantity, which has units of mol/m².s, describes the facility with 498 499 which mass is transported within a given medium, in this case, a flowing gas, and hence determines the 500 thickness of the boundary layer surrounding the melt droplet.

The mass transfer coefficient is estimated through empirical correlations between dimensionless numbers determined under experimental conditions, and, for gases, is generally proportional to the diffusion rate raised to the power of 2/3 (Fuchs, 1959; Cussler, 2009). Expressions for k_c vary depending on whether the medium through which mass transfer occurs is subject to forced- or natural convection. The threshold between the two regimes is given by the ratio of the Grashof number¹ to the Reynolds number² squared, where values >> 1 indicate natural convection, and those << 1 reflect forced convection. For forced convection, Frössling (1938) derived the following expression:

508
$$k_c = \left(\frac{P}{RT}\right) \frac{D_{ik}}{r} \left(2 + 0.6Re^{\frac{1}{2}}Sc^{\frac{1}{3}}\right), (15)$$

509 Where *Re* is the Reynolds number and *Sc* is the Schmidt number³. Under natural convection conditions 510 or for laminar flow (*Gr/Re*² >> 1), as is the case for our experimental set-up (*Appendix B1*), the Chilton-

511 Colburn equation (Chilton and Colburn, 1934; Wimber et al., 1977; Liu and Bautista, 1981), is suitable

512 for calculating k_c :

513
$$k_c = \frac{hP}{RT\rho C_P} \left(\frac{C_P \rho D_{ik}}{\kappa}\right)^{\frac{2}{3}}, (16a)$$

514
$$k_{c} = \left(\frac{P}{RT}\right) \frac{(D_{ik})^{\frac{2}{3}}}{r} \left(\left(\frac{\kappa}{\rho C_{P}}\right)^{\frac{1}{3}} + 0.3(U_{\infty}L)^{\frac{1}{2}} \left(\frac{\rho}{\eta}\right)^{\frac{1}{6}}\right) (16b)$$

515 Where *h* is the heat transfer coefficient, U_{∞} is velocity of the flowing gas at an infinite distance from 516 the sample, *L* is the diameter of the tube, ρ is the density of the gas, η its viscosity, κ its thermal 517 conductivity. Values and units for each term, and their meaning, are described in *Appendix B1*. The 518 value of k_c is evaluated for the conditions of the furnace, at 1 bar both by direct measurement of *h*, 90 519 W/m²K (Sossi et al. 2019) with eq. 16a, and by eq. 16b from the gas flow rate (0.025 m/s) and tube 520 diameter (0.042 m), for which k_c values of 12.4 and 13.3 mol/m².s are obtained, respectively.

Recent studies (Richter et al., 2002; Young et al., 2019), have approximated k_c by assuming transport occurs purely by binary diffusion, and hence, in their analysis $k_c = \frac{D_{ik}P}{rRT}$, see also Craig (1968). Although our expression has a similar form, it differs in two principal ways; 1) it accounts for the advection and convection of the gas in the vicinity of the sample in accelerating mass transport (Stefan

¹ Grashof number, $Gr = g\rho^2\beta\Delta TL^3/\eta^2$, where g is the acceleration due to gravity, β is the coefficient of thermal

expansion (1/T for an ideal gas) and ΔT is the temperature difference between the sample surface and bulk gas.

² Reynolds number, $Re = U_{\infty}\rho L/\eta$.

³ Schmidt number, $Sc = \eta/D_{ik}\rho$.

- flow) and 2) k_c is proportional to $(D_{ik})^{\frac{2}{3}}$ at the diffusive limit (where D_{ik} is small) and not D_{ik} . Under forced convection, the dependence of k_c on D_{ik} varies as a function of the Schmidt number, from a 525 526
- proportionality with $(D_{ik})^{\frac{2}{3}}$ at low *Sc* to one with D_{ik} at high *Sc* (eq. 15). The k_c calculated herein for natural convection is ~3 times faster than the diffusion-only value, ~3.8 mol/m².s. 527
- 528
- 529 Equating eq. (13) with eq. (14), and re-arranging, the unknown $p_{i,s}$ term is eliminated to obtain:

530
$$\left(\frac{dn_i}{dt}\right)_{net} = -4\pi r^2 \frac{\frac{\gamma_{i,ev}p_{i,eq}}{\sqrt{2\pi RM_i T}}}{1 + \frac{\gamma_{i,cn}P}{k_c \sqrt{2\pi RM_i T}} (1 - \exp(\xi) \operatorname{erfc}(\sqrt{\xi}))}.$$
(17)

531 As such, when mass transport is fast (*i.e.*, k_c is large), the denominator in eq. (17) tends to 1, and the 532 net evaporation rate approaches the maximum evaporation rate ($p_{i,s} = 0$), given by the numerator. The

value of $p_{i,eq}$ for any melt oxide species, $M^{x+n}O_{\underline{x+n}}$, is given by its congruent evaporation: 533

534
$$M^{x+n}O_{\frac{x+n}{2}}(l) = M^xO_{\frac{x}{2}}(g) + \frac{n}{4}O_2(g)$$
(18)

where the equilibrium partial pressure of the stable gas species, $M^{x}O_{\frac{x}{2}}$, at the surface is: 535

536
$$p_{i,eq} = p\left(M^{x}O_{\frac{x}{2}}\right) = \frac{K_{(r)}X\left(M^{x+n}O_{\frac{x+n}{2}}\right)\gamma\left(M^{x+n}O_{\frac{x+n}{2}}\right)}{f(O_{2})^{\frac{n}{4}}} (19)$$

Where X is the mole fraction and γ the activity coefficient of $M^{x+n}O_{\frac{x+n}{2}}$ in the melt. Integrating with 537 538 respect to time and concentration, following Sossi et al. (2019) (see their equations (2) to (8) for 539 derivation), gives the analytical form of the equation:

540
$$\frac{X_{i}^{t}}{X_{i}^{0}} = \exp\left(-\frac{\frac{K_{(r)}^{*} 3M}{f(O_{2})^{n/4}r\rho}\sqrt{\frac{1}{2\pi M_{i}RT}}(t-t_{0})}{1+\frac{\gamma_{i,cn}\rho C_{P}}{h}\left(\frac{\kappa}{C_{P}\rho D_{ik}}\right)^{\frac{2}{3}}\sqrt{\frac{RT}{2\pi M_{i}}}(1-\exp(\xi)\operatorname{erfc}\sqrt{\xi}),}\right)(20)$$

Where $K_{(r)}^* = K_{(r)} \gamma \left(M^{x+n} O_{\frac{x+n}{2}} \right) \gamma_{i,ev}$. Evaluating the denominator with k_c calculated from eq. (16) 541 for evaporation at 1 bar yields ~ 100 (dimensionless), which results in a flux that is therefore ~ $10^2 \times$ 542 543 lower (cf. eq. 17) than for evaporation into a vacuum (for which the denominator is equal to unity), all 544 else being equal. This factor was determined empirically when calculating K^* values in Sossi et al. 545 (2019) and is predicted from first-principles herein.

546 Importantly, k_c is nearly independent of which element is being investigated, as it is determined 547 primarily by the properties of the fluid medium surrounding the sample, and only mildly by those of the evaporating species themselves, via the D_{ik} term (cf. eqs. 15, 16). Furthermore, k_c does not change 548 549 significantly as a function of fO₂, nor for different gas flow rates (provided flow remains laminar). This 550 expectation is confirmed in tests with two different flow rates at 1500 °C (P31/07/18a and b; 200 ml/min 551 and 20 ml/min, respectively) and 1400 °C (P01/08/18a and b; 200 ml/min and 20 ml/min, respectively) 552 each using pure CO_2 , in which the fractional vapour loss was within uncertainty of unity (Table 1). The same is true of samples run in air compared to those run in a flowing gas, k_c varies from 13.3 mol/m².s 553 with U = 0.025 m/s to 11.1 mol/m².s with no gas flow. 554

555 Compared with elemental loss, predicting isotopic fractionation is comparatively simpler, because the

- global variables cancel when taking the ratio of fluxes of two isotopes. Isotopic fractionation is 556
- calculated as: 557

$$558 \qquad \qquad i/j E(\alpha_{vap-liq})_{net} = -4\pi r^2 \frac{\frac{\gamma_{i,ev}^{p}_{i,eq}}{\sqrt{2\pi RM_{i}T}}}{1 + \frac{\gamma_{i,cn}^{P}}{k_{c,i}\sqrt{2\pi RM_{i}T}}(1 - \exp(\xi) \operatorname{erfc}\sqrt{\xi})} / -4\pi r^2 \frac{\frac{\gamma_{j,ev}^{p}_{j,eq}}{\sqrt{2\pi RM_{j}T}}}{1 + \frac{\gamma_{j,cn}^{P}}{k_{c,j}\sqrt{2\pi RM_{j}T}}(1 - \exp(\xi) \operatorname{erfc}\sqrt{\xi})}$$
(21)

559 This equation can be simplified considering that the denominator is related to the ratio of $p_{i,s}$ and $p_{i,eq}$ 560 by equations (13) and (14) and simplifying:

561
$$1 - \frac{1}{1 + \frac{\gamma_{i,cn}P}{k_c\sqrt{2\pi RMT}}(1 - \exp(\xi)\operatorname{erfc}\sqrt{\xi})} = \left(\frac{p_{i,s}}{p_{i,eq}}\right) (22)$$

562 Therefore, simplifying eq. (21) and substituting in eq. (22), one obtains:

563
$$i/j E\left(\alpha_{vap-liq}\right)_{net} = \frac{\gamma_{i,ev}p_{i,eq}}{\gamma_{j,ev}p_{j,eq}} \sqrt{\frac{M_j}{M_i}} \frac{\left(1 + \frac{\gamma_{j,cn}^p}{k_{c,j}\sqrt{2\pi RM_jT}}\right)}{\left(1 + \frac{\gamma_{i,cn}^p}{k_{c,i}\sqrt{2\pi RM_iT}}\right)} = \frac{\gamma_{i,ev}p_{i,eq}}{\gamma_{j,ev}p_{j,eq}} \sqrt{\frac{M_j}{M_i}} \frac{\left(1 - \frac{p_{i,s}}{p_{i,eq}}\right)}{\left(1 - \frac{p_{j,s}}{p_{j,eq}}\right)} (23)$$

564 Which is applicable to evaporation in a steady-state, open system for any pressure and gas flow regime. 565 When transport is sufficiently fast that $p_{i,s}/p_{i,eq} \rightarrow 0$, then ${}^{i/j}E(\alpha_{vap-liq})_{net} \rightarrow (M_j/M_i)^{0.5}$. The inverse case 566 occurs when transport is slow relative to evaporation such that $p_{i,s}/p_{i,eq} \rightarrow 1$. Thus, when taking the ratio 567 of the fluxes of two isotopes (eq. 21), all terms become small with respect to $1/k_c$ to give:

$$568 \qquad \qquad \frac{{}^{\frac{i}{j}}}{E} \left(\alpha_{vap-liq}\right)_{net} \left(D_{ik} \to 0\right) = \frac{\frac{\gamma_{j,cn}\rho C_P}{h} \left(\frac{\kappa}{C_P \rho D_{jk}}\right)^{\frac{1}{3}}}{\frac{\gamma_{i,cn}\rho C_P}{h} \left(\frac{\kappa}{C_P \rho D_{ik}}\right)^{\frac{2}{3}}} = \frac{\gamma_{i,cn}}{\gamma_{i,cn}} \left(\frac{D_{ik}}{D_{jk}}\right)^{\frac{2}{3}} = \frac{\gamma_{i,cn}}{\gamma_{j,cn}} \left(\frac{\mu_{jk}}{\mu_{ik}}\right)^{\frac{1}{3}} (24)$$

Where $\mu_{ik} = \frac{m_i m_k}{m_i + m_k}$, the reduced mass of *i* and *k*. Since, save for D_{ik} , all terms that determine k_c are properties of the gas phase in which evaporation occurs (*i.e.*, they are independent of isotopic mass) they also cancel. This assumption holds provided the evaporating species are dilute enough that they do not themselves influence the properties of the gas medium *k*. Then, because D_{ik} is itself proportional to the inverse square root of the reduced mass $(\mu_{ik})^{-\frac{1}{2}}$ (eq. B6), ${}^{ij}E(\alpha_{vap-liq})_{net}$ is proportional to $(\mu_{jk}/\mu_{ik})^{1/3}$ at the diffusive limit (*i.e.*, when diffusion through the gas is the rate-limiting step for mass transfer of the evaporating species away from the evaporating surface).

576 At the high-temperatures relevant to these experiments, quantum contributions (e.g. vibrational 577 frequency) to the free energy change of the isotopic substitution are insignificant relative to the thermal 578 energy of the system $(3/2 k_BT, k_B = Boltzmann's constant)$ such that they can be ignored. Thus, we make the assumption that $p_{i,eq} = p_{j,eq}$. Similarly, we assume that both the evaporation and condensation 579 coefficients are unity for liquids (see Sossi and Fegley, 2018 and Shornikov, 2015 for discussions). 580 581 Evaluating the denominator of the left-hand side of eq. (22) for evaporation experiments at 1 bar (~ 100), one finds that $p_{i,s}/p_{i,eq} \approx 0.99$. In detail, this value varies according to the molar mass of the 582 evaporating species, because k_c and M depend on the precise mass of the isotope considered. Thus, using eq. (22), the values of $\frac{p_{i,s}}{p_{i,eq}}$ and $\frac{p_{j,s}}{p_{j,eq}}$ obtained for the mass pairs ⁶⁵Cu-⁶³Cu and ⁶⁶Zn-⁶⁴Zn, (where 583 584 $i = {}^{66}$ Zn or 65 Cu and $j = {}^{64}$ Zn or 63 Cu) are substituted into eq. (23) and show that ${}^{i/j}$ E($\alpha_{vap-liq}$)_{net} approaches 585 $(D_{ik}/D_{jk})^{2/3}$, the diffusive limit (as D_{ik} tends to 0), which is 0.9966 in air or 0.9958 in pure CO₂ for both 586 ^{66/64}Zn and ^{65/63}Cu. These calculations overlap with the values observed in samples for which elemental 587 zoning in the condensed phase is absent (as informed from analogue experiments, Sossi et al., 2019); 588 0.9959 ± 0.0002 for ^{66/64}Zn and 0.9972 ± 0.0001 for ^{65/63}Cu. 589

- 590 For Cu, whether the experiments were performed in air or CO-CO₂ mixtures, the isotopic fractionation 591 factor remains constant, whereas eq. 24 would predict a decrease in ${}^{ij}E(\alpha_{vap-liq})$ (*i.e.*, more fractionation)
- as the molar mass of the gas phase increases from air (0.029 kg/mol) to CO₂ (0.044 kg/mol). We also

note that slight deviations from unity are permitted for $\frac{\gamma_{i,ev}}{\gamma_{j,ev}}$ and $\frac{p_{i,eq}}{p_{j,eq}}$. For a monatomic gas, $\frac{p_{i,eq}}{p_{j,eq}}$ must be < 1, as the heavier isotope (*i*) will have a slightly lower equilibrium partial pressure than the lighter 593 594 isotope (*j*). The same is true for $\frac{\gamma_{i,ev}}{\gamma_{j,ev}}$ because the value of $\gamma_{i,ev}$ relates to vibrational frequencies (Knacke 595 and Stranski, 1952; Penner, 1952; Ackermann et al., 1962) making it difficult to envisage any kinetic 596 597 mechanism that would favour detachment of the heavier isotope over the lighter isotope of the same chemical species. Both processes will decrease ${}^{ij}E(\alpha_{liq-vap})$ (more fractionation) compared to those 598 calculated from eq. 23 assuming $\frac{\gamma_{i,ev}p_{i,eq}}{\gamma_{j,ev}p_{j,eq}} = 1$. For example, given ${}^{66/64}\alpha_{Zn(g)-ZnO(s)} = \frac{p_{66,eq}}{p_{64,eq}} = 0.99985$ from Ducher et al. (2016) at 1573 K, a value of $\frac{\gamma_{66,ev}}{\gamma_{64,ev}} = 0.9995$ would be required to give ${}^{66/64}Zn(\alpha_{vap-liq}) =$ 599 600 0.9959. However, given the complexity of predicting the value of k_c in real systems together with 601 possible small variations in $\frac{\gamma_{i,ev}}{\gamma_{j,ev}}$ and $\frac{p_{i,eq}}{p_{j,eq}}$ and in the experimental conditions, we consider that the 602 experimental values are satisfactorily reproduced by the model. It therefore also illustrates that the 603 assumption of the ratios of evaporation coefficients of two isotopes of a given species being equal to 604 605 unity is well-founded.

606

607 5.0. Implications

608

609

5.1. Comparison with experimental data

Although vaporisation studies have typically sought to explain the cosmochemical features of CalciumAluminium-rich Inclusions (CAIs) or chondrules, and have thus been performed at very low pressure
(vacuum) conditions (Wang et al., 2001; Richter et al., 2002; Yu et al., 2003; Janney et al., 2004;
Wombacher et al., 2004; Dauphas et al., 2004; Richter et al., 2007; Knight et al., 2009; Mendybaev et
al., 2017), an increasing number of studies have turned to volatilisation experiments at 1 bar (Yu et al.,
2003; Richter et al., 2011; Wimpenny et al., 2019) in order to understand the origin of the limited
isotopic fractionation observed in planetary materials.

617 The formalism developed in section 4.2. permits enumeration of the effect of total pressure on the 618 vapour-liquid fractionation factor. Higher total pressures cause a linear decrease in both the diffusion 619 coefficient, D_{ik} (eq. B6) and in the density of the ambient gas (eq. B2). The net effect is to decrease the 620 mean free path of evaporating molecules, thereby depressing the evaporation rate indirectly through the

- build-up of molecules (higher $\frac{p_{i,s}}{p_{i,eq}}$) in the gaseous boundary layer surrounding the melt sphere. Because
- 622 the mass transfer coefficient, k_c , is proportional to $(D_{ik})^{\frac{2}{3}}$, which is itself proportional to 1/P, and $\rho^{-1/3}$,
- which is itself proportional to P(cf. eq. 16), k_c varies with 1/P. This dependence mirrors that predicted
- from the diffusion-only mass transfer coefficient, for which k_c is proportional to D_{ik} (*e.g.*, Richter et al., 2002).



626

627 Figure 8. The effect of pressure, expressed as log(P) (with P in bars) on the vapour-liquid isotopic fractionation 628 factor, ${}^{ij}E(\alpha_{vap-liq})_{net}$. Here, $i = {}^{41}K$ and $j = {}^{39}K$, and the mass transfer coefficient is calculated at 1450 °C for natural 629 convection in air (k), $M_k = 0.029$ kg/mol. The fractionation factor is then calculated according to the dependence 630 on $(D_{ik}/D_{jk})^{2/3}$ (solid line) and (D_{ik}/D_{jk}) (dashed line), where the value of the mass transfer coefficient is otherwise 631 constant. Solid vertical lines delineate the fields of Langmuir evaporation $(p_{i,s}/p_{i,eq} < 0.01)$ and the diffusion-632 limited regime $(p_{i,s}/p_{i,eq} > 0.99)$ with the intervening pressure range giving rise to a 'mixed' evaporative regime. 633 Lighter ambient gases (k) will shift these curves to the left and to a higher diffusion-limited ceiling, and vice-634 versa.

Calculation of ${}^{41}\text{K}/{}^{39}\text{K}(\alpha_{vap-lia})_{net}$ from 10 bar to 10⁻⁶ bar at 1450 °C for a gas with mean molar mass of 635 0.029 kg/mol indicates that the diffusive limit (defined as $p_{i,s}/p_{i,eq} > 0.99$) occurs above ~0.5 bar, 636 whereas pure Langmuir vaporisation (when $p_{i,s}/p_{i,eq} < 0.01$) is expected below ~10⁻⁴ bar (Fig. 8). High-637 precision evaporation experiments over a range of pressures are required in order to verify these 638 639 predictions. Note that, because this treatment assumes steady-state loss (cf. eq. 14), the fractionation factor tends to the diffusion-limited value (~0.993 in air for ^{41/39}K), rather than to the equilibrium 640 fractionation factor (~ 1). The latter would be applicable as an upper limit to cases in which the gas 641 642 remains in contact with the condensed phase (*i.e.*, a closed system) at any pressure.

At the diffusive limit, as is relevant for evaporation at 1 bar, our expression predicts a fractionation 643 factor that is proportional to $(\mu_{ik}/\mu_{ik})^{1/3}$ (eq. 24). However, because Richter et al. (2002) and Young et 644 al. (2019) assume that k_c depends simply on D_{ik} , these studies predicted that ${}^{i/j}E(\alpha_{vap-liq})_{net}$ tends to 645 $(\mu_{ik}/\mu_{ik})^{1/2}$. To ground-truth these different dependencies, we summarise existing experimental data for 646 the isotope fractionation of moderately volatile elements during their vaporisation from silicate melts 647 648 at 1 bar in Table 3 and Fig. 9. These experiments were all performed under low flow rates that permits 649 application of eq. (16) in the limit D_{ik} tends to 0. Increasingly higher flow rates would accelerate mass transfer, with the net effect of decreasing $p_{i,s}/p_{i,eq}$, and thus ${}^{ij}E(\alpha_{vap-liq})_{net}$ (*i.e.*, more fractionation) relative 650 651 to the $p_{i,s}/p_{i,eq} = 1$ limit.

652

Table 3. Isotopic fractionation of moderately volatile elements during their evaporation from silicate melts at a total pressure of 1 bar.

Eleme	Isotope	Gas		Temperatur		$^{i/j}E(\alpha_{vap-})$	$^{i/j}E(\alpha_{va})$ $^{p-liq})$ This	$^{i/j}E(\alpha_{vap-liq})$	
nt	Ratio	medium	$log fO_2$	e (° C)	Material	only	work	Observed	Ref.
K	41/39	Air	-0.68	1450	IIAB Chondrule	0.9890	0.9925	0.9917 ± 0.0015 0.9935 +	Y+' 03 R+'
К	41/39	CO ₂ -H ₂	-6.93	1430	IIAB Chondrule IIAB Chondrule (K-	0.9891	0.9927	0.0006 $0.9993 \pm$	11 R+'
K	41/39	H_2	-	1450	rich, Fe-free)	0.9987	0.9990	0.0004	11



653



Figure 9. A comparison between the isotopic fractionation factor between vapour and liquid, ${}^{i/j}E(\alpha_{vap-liq})_{net}$, observed in experimental studies of the evaporation of ${}^{41/39}K$ (orange), ${}^{65/63}Cu$ (green) and ${}^{66/64}Zn$ (blue) from silicate melts at 1 bar and a variety of gas mixtures (labelled next to points), compared to that predicted according to **a**) a $(\mu_{jk}/\mu_{ik})^{1/2}$ dependence and **b**) a $(\mu_{jk}/\mu_{ik})^{1/3}$ dependence on mass transport through the gas phase. The dashed 1:1 line denotes perfect agreement between experiment and theory.

660 Although both expressions correctly predict the sense of isotopic fractionation, expressions with a $(\mu_{jk}/\mu_{ik})^{1/2}$ dependence underestimate the value of ${}^{i/j}E(\alpha_{vap-liq})_{net}$ (Fig. 9a), whereas the $(\mu_{jk}/\mu_{ik})^{1/3}$ 661 proportionality derived herein (Appendix B1) lies within ± 0.0005 of the experimental data (Fig. 9b). 662 Experiments over a wide range of gas mixtures and isotopic systems therefore empirically verify the 663 dependence on $(\mu_{ik}/\mu_{ik})^{1/3}$. This new formalism also ameliorates the difficulty of having to account for 664 fractionation factors that are smaller (i.e., higher ${}^{i/j}E(\alpha_{vap-liq})_{net}$) than predicted by the $(\mu_{jk}/\mu_{ik})^{1/2}$ 665 dependence, as is the case for almost all isotopic systems investigated (Fig. 9a). Values of ${}^{ij}E(\alpha_{vap-liq})_{net}$ 666 that exceed the diffusion-limited value require either that i) $p_{i,eq} > p_{j,eq}$ and/or ii) $\gamma_{i,ev} > \gamma_{j,ev}$; both of which 667 are equally unphysical (section 4.2.). The departure to higher values of ${}^{i/j}E(\alpha_{vap-liq})_{net}$ observed in some 668 vacuum experiments (particularly for ^{25/24}Mg; Richter et al. 2007; Mendybaev et al. 2017) may relate 669 to different evaporation coefficients among *different species*. That is, that $\gamma MgO/\gamma Mg > 1$, such that 670 there is more MgO(g) relative to Mg(g) than expected under equilibrium conditions, meaning the mean 671 672 molar mass of Mg in the gas phase increases. A detailed exploration of such a hypothesis is beyond the scope of this work. 673

674 Conspicuous in Fig. 9 are the ${}^{66/64}$ Zn($\alpha_{vap-liq}$) fractionation factors of Wimpenny et al. (2019), which fall

675 to slightly (rhyolitic soil) or significantly (arkosic soil) higher values. Notably, the experimental charges 676 at temperatures below 1800 °C were not fully molten, as attested to by their non-aerodynamic forms,

677 making it difficult to quantify evaporation rates thermodynamically. Moreover, all other variables being

held constant, the amount of Zn remaining in the melt does not decrease as a function of time (for runs < 60 s) as would be expected from eq. 6. This suggests evaporation did not reach a steady state until ~ 60 s. Indeed, arkosic soil shows a variation of ${}^{66/64}Zn(\alpha_{vap-liq})$ with run time. After 60 s, the vaporisation rate can be modelled with a log $K*_{Zn}$ value of -3.75 ± 0.29 at all temperatures for both the arkosic and rhyolitic soil, which is lower (slower evaporation rate) than predicted from extrapolation of the trends shown in Fig. 3. The rhyolitic soil shows no dependence of ${}^{66/64}Zn(\alpha_{vap-liq})$ on experimental run time, and is also much closer to the predicted value in pure Ar, 0.9960.

Because both compositions have > 70% SiO₂ by definition (and likely >90% in the case of arkose) and 685 686 the experiments were performed at 1 bar where water solubility is low (< 0.1 wt. %; Dixon et al., 1995), the melt viscosity in both cases is likely to be of the order of logn ≈ 3 to 4 at 2000 °C (Stevenson et al., 687 1998; Giordano et al., 2008); at least $10^3 \times$ more viscous than the melt compositions used herein, 688 meaning diffusion rates of Zn were also $10^3 \times$ slower. A quantitative model of vaporisation rate for the 689 experiments of Wimpenny et al. (2019) cannot be constructed because they were not fO_2 -buffered, nor 690 691 were zoning profiles across the glass beads measured. However, the empirical observation that $^{66/64}$ Zn($\alpha_{vap-liq}$) in their experiments are higher than *i*) predicted for a diffusive-limited gas regime (Fig. 692 9b) and *ii*) observed for ferrobasaltic melts in which no diffusion profiles are present (Fig. 5b), strongly 693 694 suggests the influence of incomplete diffusion to the evaporating surface in increasing $^{66/64}$ Zn($\alpha_{vap-liq}$) 695 during evaporation from rhyolitic and particularly arkosic melts.

696 697

5.2. Evaporation processes in natural rocks

698 The corollary that the rate of mass transfer of two isotopes from the evaporation surface is proportional to the ratios of the reduced masses of the evaporating species, $(\mu_{ik}/\mu_{ik})^{1/3}$, is that fractionation factors at 699 the diffusive limit are sensitive to the mean molecular mass of the surrounding gas. In detail, isotopic 700 701 fractionation is suppressed if diffusion occurs through lighter gases, and promoted for diffusion through 702 heavier gases. Physically, this phenomenon arises because, when the difference in molar mass between 703 two constituents is large, the collisions between the lighter molecules in a binary gas mixture govern its 704 velocity distribution (Chapman and Cowling, 1970). This can be verified mathematically, where the 705 reduced mass tends to that of the lighter constituent as the mass difference between the two increases, 706 independent of their abundance ratio. In our case, as the lighter, ambient gas (k) is in excess of both 707 evaporating species, *i* and *j* (the so-called quasi-Lorentzian condition; Mason, 1957), then, the greater 708 the difference between m_k and $m_{i,j}$, the more the reduced masses μ_{jk} and μ_{ik} tend to a common value (m_k) , 709 and hence the closer the fractionation factor is to unity. Conversely, if $m_k >> m_{i,i}$, then the reduced mass of the mixture *ik* is approximated by m_i (and the mixture *jk* by m_i), and the fractionation factor 710 approaches $(m_i/m_i)^{1/3}$. Figure 10 illustrates the dependence of ${}^{i/j}E(\alpha_{van-lia})_{net}$ on the atmospheric molar 711 mass (m_k) at the diffusive limit for four moderately volatile element isotope pairs. 712





Figure 10. The modelled change of ${}^{ij}E(\alpha_{vap-liq})_{net}$ at the diffusive limit for four moderately volatile element isotope pairs (${}^{87/85}$ Rb, black; ${}^{66/64}$ Zn, blue; ${}^{65/63}$ Cu, green; ${}^{41/39}$ K, orange) evaporating as monatomic gases, as a function of the mean molar mass of the gas through which they diffuse. Common molecules or atmospheres to which these molar masses correspond are shown as dashed grey lines. The grey horizontal bar corresponds to ${}^{ij}E(\alpha_{vap-liq})_{net}$ inferred for the Moon, deduced from the isotopic compositions of lunar mare basalts. In each case, the fractionation factor lies between 0.9994 and 0.9999 (see text).

720 *5.2.1. Tektites*

Samples for which the composition and total pressure of the atmosphere into which evaporation occurs
is known presents the simplest scenario to understand the conditions of vaporisation in natural systems.
This criterion is satisfied by tektites, glasses that formed upon melting and subsequent quenching of
crustal rocks during hypervelocity impact events (Koeberl, 1986 and references therein). Because these
events are recent (<35 Myr; Koeberl, 1994) up to ~790,000 years ago for Australites (Schneider et al.,
1992), evaporation occurred into air with characteristics identical to those observed today.

727 The derivation of ${}^{i/j}E(\alpha_{vap-liq})_{net}$ from analyses of tektites is sensitive to the assumed composition of their 728 source rocks. Although the Cu and Zn isotope composition of the continental crust is not expected to 729 differ significantly from igneous rocks (at least on the scale relative to the fractionation observed in 730 tektites), their initial concentrations may vary by more than a factor of 2 (Taylor and Kaye, 1969; 731 Koeberl, 1986; Žák et al., 2016). Owing to the compositional similarity borne by non-volatile elements in tektites to the upper continental crust (UCC), it has been customary to use it to calculate Cu_0 and Zn_0 732 733 which yields 28 ppm and 67 ppm, respectively (Rudnick and Gao, 2003). However, source compositions among tektite groups may vary, as substantiated by the non-linear arrays in lnf(E) vs. $\delta^{i}E$ 734 space (Moynier et al., 2009; Jiang et al., 2019), complicating the extraction of accurate ${}^{ij}E(\alpha_{vap-lia})_{net}$ 735 736 from these data.

Considering these uncertainties, both ${}^{66/64}Zn(\alpha_{vap-liq})$ and ${}^{65/63}Cu(\alpha_{vap-liq})$ lie in the range 0.996 to 0.999 (Moynier et al., 2009; Rodovska et al., 2017; Jiang et al., 2019), values which are broadly consistent with those predicted from our model (0.9966). The smaller fractionation of ${}^{66/64}Zn(\alpha_{vap-liq})$ with respect to ${}^{65/63}Cu(\alpha_{vap-liq})$ inferred by Moynier et al., (2010) was attributed to the slower diffusion of Zn in the tektite melt at high temperatures with respect to Cu. On the other hand, a recent measurement of and elemental profiles of Cu, Zn and K in a tektite from Hainan did not observe systematic zoning in abundance for any of the three elements. Nevertheless, the absence of zoning in the Hainan tektite (r =

744 0.045 m) does not necessarily exclude diffusion-limited fractionation in other tektites, as they are each

- 745 sensitive to the local formation conditions and may have also re-homogenised by convection during- or 746 post-vaporisation. Our expression predicts no dependence of t_{evap}/t_{diff} on r for diffusion-limited 747 conditions, meaning zoning is as likely to manifest itself in small tektites as it is in larger ones. That K 748 isotopes do not show any measurable fractionation in tektites (Jiang et al., 2019), despite the high 749 diffusion coefficient of K in silicate melts (Jambon, 1982) relative to Zn, instead suggests that potassium remained non-volatile; a loss of ~ 1 % of its initial budget with ${}^{41/39}K(\alpha_{vap-liq}) = 0.993$ would result in 750 isotopic fractionation of + 0.07 %. Its lack of evaporative loss is plausibly related to its very low activity 751 coefficient in silicate melts, $\sim 10^{-4}$ (Sossi et al., 2019), and in particular those that are silica-rich (Borisov, 752 753 2009), causing a $10,000 \times$ decrease in partial pressure relative to cases in which K behaves ideally. As
- such, much of the K remains in the melt, even for considerable losses of Cu and Zn.
- Our experiments demonstrate that ${}^{66/64}Zn(\alpha_{vap-liq})$ is slightly lower (more fractionation) than ${}^{65/63}Cu(\alpha_{vap-liq})$ 755 756 lig) when the glass is homogeneous, opposite to that observed in tektites. This discrepancy is most readily 757 explicable by diffusion-limited Zn isotope fractionation during evaporation due to its slower diffusion 758 through the tektite liquid relative to Cu, as verified experimentally in Fig. 5, and modelled in section 759 4.1 and in Moynier et al. (2009). Indeed, core and rim analyses of a single Australite tektite (Moynier et al., 2009) show that the core is enriched in Zn (265 ppm) and light isotopes (δ^{66} Zn = +1.22 %) relative 760 to the rim (19 ppm and +1.83 %), in qualitative agreement with such a scenario. On the basis that Sn 761 762 isotopes, with a similar relative mass difference, show comparable isotopic fractionation to Zn (and 763 thus less than Cu) in the same tektites also lends support a diffusive barrier to isotope fractionation 764 during evaporation (Creech et al., 2019).
- 765 It remains challenging to use experimental results in a uniform temperature environment to 766 quantitatively assess isotopic fractionation in tektites. This is because, in the impact scenario that forms tektites, shocked material follows a Hugoniot before undergoing decompression that leads to 767 768 fragmentation in which material intersects the liquid-vapour phase transition from the liquid side 769 (Melosh and Vickery, 1991), meaning temperature cannot be assumed to be constant over the 770 vaporisation timescale and steady-state conditions may have not been achieved (Humayun and Koeberl, 771 2004). Some authors have also appealed to a vapour-cloud produced by the impact itself in modifying 772 the local atmospheric conditions around tektite precursors undergoing fusion and vaporisation 773 (Rodovska et al. 2017). Further work is required to evaluate the degree and sense of internal elemental 774 and isotope zonation within tektite glasses, together with a better estimate of their initial abundances in 775 potential source rocks (e.g. Zak et al. 2016) to discriminate between the mechanisms of vaporisation during their formation. 776

777 5.2.2. The Moon

778 Assessment of the volatile loss that was thought to have affected the composition of the Moon following 779 a giant impact event is subject to the opposite problem; although the fractionation factors for moderately 780 volatile elements are well-defined, the composition of its likely atmosphere or the locus of volatile 781 depletion are not. The separation of condensed phases from gas may have occurred during various 782 stages of lunar formation, such as upon viscous spreading attending proto-lunar disk collapse (Canup 783 et al. 2015), partial condensation during cooling of a synestia (Lock et al. 2018), or loss of an 784 atmosphere in equilibrium with an early lunar magma ocean (Sossi et al. 2018; Charnoz et al. 2019). 785 The bulk composition of the atmosphere at the vapour-liquid interface in each scenario, and the 786 mechanisms by which volatiles are lost, are poorly constrained and are expected to have varied 787 according to the local physico-chemical conditions. Stable isotopes may shed light on these issues, as 788 their fractionation is sensitive to both the mode of evaporative loss and transport (sections 4.1, 4.2) and 789 the thermodynamic conditions (section 3.2) under which volatile depletion took place.

790 The ${}^{ij}E(\alpha_{vap-liq})_{net}$ inferred for the Moon is calculated on the basis of the elemental and isotopic 791 compositions of lunar mare basalts, the most extensive form of magmatism exposed on the lunar surface 792 (BVSP, 1981), which have subsequently been used to inform compositional models for the bulk Moon 793 (O'Neill, 1991; Taylor and Wieczorek, 2014; Ni et al., 2019). Although lunar pyroclastic glass beads 794 have also been used for this purpose (Hauri et al., 2015; Ni et al., 2019), their utility is limited in this 795 context because recondensation occurring during fire-fountaining has resulted in isotopic fractionation, 796 overprinting the primary mantle signature (Moynier et al., 2006; Herzog et al., 2009). Mg Suite rocks, 797 due to their high Mg#, pristine nature and old crystallisation ages are also useful probes of lunar interior 798 composition (Warren, 2005; Shearer et al., 2015). Mg Suite cumulates have lower Zn contents and are more isotopically fractionated than mare basalts, with the net result being the inferred ${}^{66/64}$ Zn($\alpha_{vap-liq}$) is 799 800 comparable (~0.9993) to that defined by mare basalts (0.9996) (see Day et al., 2020).

As such, the definition of a bulk lunar mantle is a conceptual construct, akin to the 'bulk silicate Earth',

and should not be taken to imply that the lunar interior is homogeneous. Rather, we examine rocks of the same lithology (*i.e.*, mare basalts) for which compositional and isotopic variations are statistically

similar within a given group such that they permit comparison among different elements. Then, given

the isotopic and chemical similarity observed for non-volatile elements between the Earth's mantle and the lunar mantle (Warren, 2005; Zhang et al., 2012; Young et al., 2016; Sossi and Moynier, 2017;

the lunar mantle (Warren, 2005; Zhang et al., 2012; Young et al., 2016; Sossi and Moynier, 2017; Sedaghatpour and Jacobsen, 2019), the Cu and Zn elemental and isotope compositions of the bulk

silicate Earth are adopted as the compositional starting points from which lunar volatile loss is modelled.

Here we investigate the ${}^{i/j}E(\alpha_{vap-liq})$ of four moderately volatile elements, K, Cu, Zn and Rb, for which

- 810 both the isotopic and chemical composition in the lunar mantle is well constrained, as summarised in
- 811 Table 4.

Table 4. A summary of the Zn, Cu, K and Rb abundances and isotopic compositions in the Earth's and Moon's mantle (based on mare basalts), and calculated vapour-Moon fractionation factors.

	Zn (ppm)	δ ⁶⁶ Zn (‰)	Cu (ppm)	δ ⁶⁵ Cu (‰)	K (ppm)	δ41K (‰)	Rb (ppm) δ ⁸⁷ Rb (‰)		
Moon's mantle	2.1 ± 1	1.4 ± 0.2	11	0.68 ± 0.17	42 ± 6	-0.07 ± 0.09	0.125 ± 0.005	0.04 ± 0.09	
Earth's mantle	53.5 ± 3	0.16 ± 0.06	30 ± 6	0.06 ± 0.10	260 ± 39	-0.48 ± 0.03	0.605 ± 0.060	-0.13 ± 0.06	
$lnf(E)_{Moon}$	-3.24	± 0.39	-1.00	± 0.22	-1.8	2 ± 0.28	-1.58 ± 0.13		
$\Delta^i E_{Moon-Earth}$	1.24	± 0.21	0.61	± 0.20	0.4	1 ± 0.09	0.17 ± 0.11		
$^{i/j}E(\alpha_{vap-Moon})$	0.9996 ± 0.0001		0.9994 ± 0.0003		0.999	8 ± 0.0001	0.9999 ± 0.0001		

Palme and O'Neill (2014) – Zn, K, Rb abundances BSE; Wang and Becker (2015) – Cu abundances BSE; Taylor and Wieczorek (2014), O'Neill (1991) – Zn, K, Rb abundances Moon; Ni et al. (2019) – Zn, Cu, K abundances Moon; Paniello et al. (2012), Kato et al. (2015) – δ^{66} Zn_{Moon}; Sossi et al., (2018) – δ^{66} Zn_{Earth}; Herzog et al. 2009, Day et al. (2019) – δ^{65} Cu_{Moon}; Liu et al. (2015) – δ^{65} Cu_{Earth}; Wang and Jacobsen (2016), Tian et al. (2020) – δ^{41} K_{Earth}, Moon; Pringle and Moynier (2017), Nie and Dauphas (2019) – δ^{87} Rb_{Earth}, Moon.

812

813 In each case, the calculated ${}^{ij}E(\alpha_{vap-liq})$ lies between 0.9994 ± 0.0002 (Cu) and 0.9999 ± 0.0001 (Rb).

814 The diffusion-limited fractionation factor approaches these values only for an H₂-rich gas with mean

molar mass ~ 2 g/mol (Fig. 10). However, such a scenario is doubtful considering that i) the strong temperature contrast in the proto-lunar atmosphere that would have promoted convection preventing the establishment of a diffusive gradient (Thompson and Stevenson, 1988), ii) a hydrogen-rich

818 atmosphere likely never existed in the protolunar disk or early Moon due to the propensity for 819 hydrodynamic escape to occur in its early evolution in the vicinity of the Earth's Roche Limit (Nakajima

- and Stevenson, 2018; Charnoz et al., 2019), *iii*) it is not clear whether the Moon's atmosphere was ever
- thick enough to produce total pressures that would cause evaporative loss to be diffusion-limited. Even
- had the Moon retained most of its hydrogen, at any reasonable oxygen fugacity in an atmosphere in equilibrium with silicate material, between the IW and FMO buffers (Visscher and Fegley, 2013), the
- H_2/H_2O ratio varies between 0.5 and 0.02, respectively, such that the mean molecular mass of the gas
- was likely to be >10 g/mol. Figure 10 was constructed presuming that each element vaporised as a
- monatomic gas (*e.g.* Cu^0 , Zn^0). However, in volcanic gases, Cu, Zn and the alkali metals tend to form
- chloride species (Symonds and Reed, 1993; Churakov et al., 2000; Renggli et al., 2017; Henley and
- Seward, 2018). Nevertheless, Sossi and Fegley (2018) showed that, for a steam atmosphere produced
- by evaporation of the bulk silicate Earth at 2000 K, $ZnCl_2(g)$ and CuCl(g) form only at pressures >> 1

- 830 bar, suggesting they were unlikely to have been present in the more tenuous atmosphere of the proto-
- 831 Moon at magmatic temperatures (> 1000 °C).



832

Figure 11. Best estimates for the isotopic fractionation factor of four well-defined moderately volatile elements between the Earth's mantle and the Moon's mantle against the square root of their mean molar masses. Overlain on the lunar data are grey dashed curves showing the fractionation that would arise during diffusion-limited evaporation into fictive atmospheres with different mean molar masses in g/mol (numbers in circles).

837 That these metals were likely present as monatomic gases suggests that, should transport phenomena 838 have been important in causing isotopic fractionation, a correlation would be expected with molecular 839 mass, the predominant variable controlling diffusion rates in condensed phases and gases. Figure 11 840 illustrates that this is not observed, strongly arguing against any kind of non-equilibrium process in 841 setting the relative isotopic fractionations among MVEs. Fractionation factors shown in Table 3 also 842 overlap with those calculated by *ab-initio* models, for which equilibrium values of ${}^{ij}E(\alpha_{vap-liq})$ between 843 common silicate minerals and monatomic gas range from ~ 0.9995 at 1000 K to ~ 0.9999 at 2000 K for 844 K, Zn and Rb (Ducher et al. 2016; Li et al. 2019; Zeng et al. 2019), though the relevance of these 845 mineral-gas fractionation factors to Moon-forming conditions remains uncertain. That equilibrium 846 partial pressures more strongly influence lunar volatile depletion than do mass transport phenomena is 847 also supported by the scaling of lunar element depletion factors with chemical affinity (e.g. O'Neill, 848 1991). The alkali metals evaporate according to a similar stoichiometry; where $M^+O_{0.5}(l, s) = M^0(g) +$ 849 ¹/₄O₂ (barring Cs, for which Cs₂O(g) is an abundant gas species; Sossi and Fegley, 2018), and are each 850 conspicuously depleted to a similar extent in the Moon relative to Earth's mantle (a factor of 6, save for 851 Li which is non-volatile). This commonality comes despite large differences in molar masses ($\Delta m_{\rm Rb-Na}$ = 55.5 g/mol) that far exceed any small differences in isotopic mass ($\Delta m_{41K-39K}$ = 2 g/mol), a property 852 853 that would engender elemental separation by mass transport in a gas phase (section 4.2.). A chemical equilibrium control on volatile element fractionation on the Moon is also supported by dynamical 854 855 models of planetesimal atmospheres which suggest that equilibrium is readily attained, even at low total pressures (Young et al. 2019), and the lighter isotope compositions of Cr and Sn in the Moon (Sossi et 856 857 al., 2018; Wang et al., 2019) relative to Earth's mantle, which would be violated by any mass-transport 858 process that favours loss of the lighter isotope.

859 Conversely, H_2 -rich gases may be instrumental in dampening isotopic fractionation in primary planetary

atmospheres that evolved by accretion of nebular gas. These high-pressure, hydrogen-rich environments likely characterised accretion zones of chondrites and of the terrestrial planets < 5 Myr, the approximate

timing of loss of the nebular gas to the Sun (Dauphas and Chaussidon, 2011). This phenomenon may

- 863 also explain why isotopic fractionation attending chondrule formation is limited in the solar nebula (e.g. Alexander et al., 2000; Galy et al., 2000; Pringle et al., 2017), where H₂ is by far the dominant 864 865 constituent. Alternatively, when evaporation becomes so fast relative to the diffusion rate that t_{diff}/t_{evap} tends to infinity, ${}^{ij}E(\alpha_{vap-liq})_{net}$ tends to unity, which means that evaporation can occur without any 866 isotopic fractionation provided the diffusion rate in the condensed phase is very low and/or the 867 868 evaporation rate is very fast. These conditions may typify the evaporation of dry, siliceous silicate melts 869 or sublimation of solids in the reducing nebular gas (see also Ozawa and Nagahara, 2001). Such H-rich 870 conditions may also be expected to be present on hot, close-in exoplanets with escaping steady-state atmospheres (Owen, 2019), and may serve to understand isotope ratios of volatile elements heavier than 871
- 872 hydrogen.

873

874 **6.0. Conclusions**

875 We establish that isotopic fractionation during evaporation of Cu and Zn from basaltic silicate melts at 1 bar, for which evaporation is not limited by diffusion in the melt, follows ${}^{66/64}Zn(\alpha_{vap-liq}) = 0.9959 \pm$ 876 0.0002 and ${}^{65/63}Cu(\alpha_{vap-lia}) = 0.9972 \pm 0.0001$. Fractionation factors become closer to unity for lower 877 878 oxygen fugacity, as the vaporisation rate increases, despite no change in vaporisation reaction stoichiometries. These experiments are zoned, and we derive diffusion rates for Cu and Zn in ferrobasalt 879 at 1300 °C (2.61 × 10⁻⁹ m²/s and 1.56 ± 0.25×10^{-9} m²/s, respectively), that remain constant with fO₂. 880 Thus, the ratio of the timescale of evaporation/diffusion decreases such that a heavy-isotope rich 881 882 boundary layer develops at the evaporating surface of the melt at lower fO_2 . This occurs because, even though the diffusion of the lighter isotope is faster than the heavier isotope by a factor $(M_i/M_i)^{\beta}$, this 883 factor, in which $\beta \approx 0.015$, is closer to 1 than is the vapour-liquid fractionation factor at the surface. The 884 885 net fractionation factor is therefore also closer to unity in cases where diffusion in the liquid is slower 886 than evaporation, and, at the extreme, results in no isotopic fractionation for infinitesimally slow 887 diffusion rates.

888 We develop a new formalism describing transport of the evaporating species in the gas phase, which dictates its ability to escape from the evaporating surface. For natural convection in the gas at 1 bar, the 889 890 partial pressure of the evaporating species at the surface in a steady state is ~99% of that of its 891 equilibrium partial pressure. Under these conditions, we show that mass loss is limited according to the 892 diffusion rate of species *i* through the gas of mean molar mass k to the power of 2/3, which is itself proportional to the inverse square-root of their reduced mass, $\mu_{ik}^{-1/2}$. Isotopic fractionation between two 893 isotopes *i* and *j*, is therefore proportional to $(\mu_{ik}/\mu_{ik})^{1/3}$. This formalism reproduces the fractionation factor 894 of the isotopes of K, Cu and Zn in experiments of silicate melt evaporation at 1 bar in different gas 895 896 mixtures to within ${}^{ij}E(\alpha_{vap-liq}) \pm 0.0005$. As the fractionation factor depends on the reduced mass, it is 897 sensitive to not only the mass of the evaporating species, but also to that of the atmosphere into which

898 it evaporates, with heavier atmospheres promoting fractionation.

899 Provided that the evaporation of tektites occurs in air and at 1 bar, the isotopic fractionation recorded

900 in Cu and Zn in these impact glasses overlaps with those predicted by our model, $i/(i-2)E(\alpha_{vap-liq}) = 0.9966$.

901 Contrastingly, the isotopic fractionation factors of semi-volatile metals for vapour loss from the Moon,

902 as inferred from the composition of lunar mare basalts, are much closer to unity than predicted, save for

903 if vaporisation occurred into a pure H_2 atmosphere. However, the fact that such atmospheric

904 compositions are unlikely to have been stable on the early Moon, together with a lack of a strong mass

- 905 dependence among the depletion of alkali metals or their isotopes, suggest that mass transport was not
- an important process in causing isotopic fractionation on the Moon.
- 907

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