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Three-dimensional numerical and analytical study of horizontal group of square anchor plates in sand

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7 Abstract

8 In this paper, numerical and analytical methods are used to evaluate the ultimate 9 pullout capacity of a group of square anchor plates in row or square configurations, 10 installed horizontally in dense sand. The elasto-plastic numerical study of square 11 anchor plates is carried out using three-dimensional finite-element analysis. The soil 12 is modeled by an elasto-plastic model with a Mohr-Coulomb yield criterion. An 13 analytical method based on a simplified three-dimensional failure mechanism is 14 developed in this study. The interference effect is evaluated by group efficiency η , 15 defined as the ratio of the ultimate pullout capacity of group of N anchor plates to that of a single isolated plate multiplied by number of plates. The variation of the group 16 17 efficiency η was computed with respect to change in the spacing between plates. 18 Results of the analyses show that the spacing between the plates, the internal friction 19 angle of soil and the installation depth are the most important parameters influencing 20 the group efficiency. New equations are developed in this study to evaluate the group 21 efficiency of square anchor plates embedded horizontally in sand at shallow depth 22 (H=4B). The results obtained by numerical and analytical solutions are in excellent 23 agreement.

24 Keywords

Square anchor plate, group efficiency, finite elements, pullout capacity, sand, criticalspacing.

27 1 Introduction

28 Anchor plates are lightweight structural elements, buried in the ground, used to resist 29 the pullout forces acting on geotechnical structures such as submerged pipelines, 30 offshore structures, retaining walls, and transmission towers. They may have various 31 shapes (circular, helical, square, rectangular or strip). They are installed in the 32 ground horizontally, vertically or in an inclined way. In the literature there are different 33 theoretical, numerical and experimental works investigating the behavior of an 34 isolated anchor plate and calculate its ultimate uplift capacity. One can cite Meyerhof 35 and Adams (1968), Das (1978), Murray and Geddes (1987), Merifield and Sloan 36 (2006), Hanna et al (2007), Khatri and Kumar (2009, 2010, 2011), Wang et al (2013), 37 Bhattacharva and Kumar (2014), Mabrouki and Mellas (2014), Ardebili et al (2016), 38 among others.

39 However, little information is available in the literature concerning the ultimate pullout 40 capacity of a group of anchor plates. Table 1 presents some experimental, analytical and numerical works. Meyerhof and Adams (1968) proposed a theoretical 41 42 relationship for calculating the ultimate pullout force of group of circular or rectangular 43 foundations, buried in sand or in clay. Das and Yang (1987) have developed a 44 physical model to evaluate the ultimate pullout force of a group of circular anchor 45 plates buried in medium dense sand. They compared their results in terms of group 46 efficiency with the theoretical solution of Meyerhof and Adams (1968), and they found 47 that the ratio spacing/diameter (S/D) for a group efficiency $\eta = 100\%$, for a given 48 configuration, is approximately equal to the double of the one obtained theoretically. 49 However, the general trend of the evolution of the group efficiency with respect to 50 S/D ratio is similar to that of the theory.

51 In the present study, special attention was paid to the experimental model of Geddes 52 and Murray (1996), to study the pullout force of a group of square anchor plates

53 embedded in a dense sand at a fixed depth, in different configurations. They reported 54 that, from a critical spacing ratio ($S_{cr}/B = 2.9$ for the test conditions used), the 55 maximum group efficiency is 100% and remains at that level when increasing the 56 spacing. This critical spacing is valid for all configurations and for a number of studied 57 anchor plates.

Abbad et al. (2013), have carried out an experimental study of the interaction of the failure zones of square anchor plates installed at a depth of 5*B* in an analogical environment formed by plastic granules. They used digital photographs at high resolution processed by image correlation software to observe the displacement field and plane strain of the analogical environment. They have reported that a minimum spacing between axes of about seven times the width of the plate (7*B*) is necessary for two neighboring anchor plates to act independently of each other.

In addition, other analytical studies of interferences within a group of strip anchor plates, were established by Kumar and Kouzer (2008a), Kouzer and Kumar (2009a, 2009b), Merifield and Smith (2010), Ghosh and Kumari (2012), Kumar and Naskar (2012), and Sahoo and Kumar (2014a, 2014b). These works fall within the limit analysis framework, using the lower bound or the upper bound method. Table 1 shows the previous experimental and analytical works related to the study of the interference of anchor plates in soils.

The main objective of this study is, on the one hand, to investigate numerically, using three-dimensional non-linear finite element analysis, the group efficiency of square anchor plates buried horizontally in a dense sand for several values of spacing/width ratio (*S/B*). The effect of parameters like installation depth, internal friction angle of soil, anchor roughness, and flow rule have been investigated numerically. On the other hand, an additional objective is to develop an analytical solution of the group efficiency of square anchor plates buried horizontally in the sand based on a failure

79 mechanism available in the literature, where a modification of the shape of the failure 80 mechanism was introduced to simplify the calculation of the interference of failure 81 mechanisms.

This study aims at highlighting recommendations concerning the calculation of pulloutcapacity of group of square anchor plates buried horizontally in a dense sand.

84 2 Numerical modeling

85 In this study, a three-dimensional numerical model was developed using the finite 86 element method in Plaxis software, to investigate the ultimate uplift capacity of a 87 group of square plate anchors. From previous experimental and theoretical studies on groups of plate anchors in soil (Table 1), the experimental work of Geddes and 88 89 Murray (1996) seems the most appropriate as a reference for our work because it 90 concerns the problem of square plates and contains the required data for numerical 91 modeling. Geddes and Murray (1996) have performed a series of laboratory pullout 92 tests on group of square plate anchors buried horizontally in dense sand. These tests 93 were conducted in a steel box of size $1.28m \times 1.22m \times 0.89m$. The plate anchor 94 have a square shape of width B = 50.8 mm, buried at a fixed depth H = 203.2 mm to 95 give a ratio H/B = 4. Vertical uplift tests were carried out on two and five square 96 plates in row configuration with constant spacing; and on groups of four square 97 plates placed in a square configuration.

The symmetry of the problem enables to take a quarter model in all calculations as shown in Fig.1 which presents an example of a group of four anchor plates in square configuration. The dimensions of the numerical model adopted in all calculations (width, length and height) are constants according to the experimental model of Geddes and Murray (1996). The width of the model adopted is 0.61*m* and the height is 1*m*; the square plate anchor have a width of *B* = 50*mm*. It is verified that these

104 dimensions do not prevent the development of the failure mechanism for the large 105 values of the spacing (*S*) considered in this study.

106 The small displacement assumption has been considered in all numerical analysis. 107 The adopted soil model is a linear elastic-perfectly plastic model, obeying Mohr-108 Coulomb criterion with a non-associative flow rule. Referring to the study of Bolton (1986) on the strength and dilatancy of sands, the adopted dilation angle is $\psi' = \varphi' - \varphi'$ 109 110 30°. The anchor plate is modeled by plate elements with a linear elastic model. The 111 values of soil parameters and elastic stiffness parameters of plate anchor used in this 112 investigation are shown in Table 2. The soil parameters were taken from the Geddes 113 and Murray (1996) study, and the elastic parameters of the material constituting the 114 anchor plates were estimated from the literature studies (e.g., Hanna et al, 2011, 115 Aghazadeh Ardebili et al, 2015, Ghosh, and Kumari, 2012).

116 Interface elements are used between soil and anchor plate elements to ensure sol-117 plate interaction. This type of interface elements allow for soil detachment. The 118 interface behavior is defined by Mohr Coulomb criterion, with shear-strength 119 characteristics calculated by the introduction of the strength reduction factor $R_{inter} \leq$ 120 1, which gives the values of strength parameters of the interface element from the 121 soil parameters by applying the strength reduction method suggested by Plaxis 122 (Brinkgreve and Vermeer 2001) as follows:

123 $c'_i = R_{inter}c'_{soil}$,

124 $\tan \varphi'_i = R_{inter} \tan \varphi'_{soil} \le \tan \varphi'_{soil}$

125 $\psi_i' = 0^\circ$ for $R_{inter} < 1$, otherwise $\psi_i' = \psi_{soil}'$

where c'_{i} , φ'_{i} and ψ'_{i} are the cohesion, the friction angle and the dilation angle of interface elements respectively. 128 A modified shear box test carried out by Geddes and Murray (1996) gave an 129 interface friction angle of 10.6° for the sand studied in contact with polished steel 130 plates, of the same kind as the anchors plates used in the uplift test. So for our case 131 the strength reduction factor $R_{inter} = 0.19$.

Prescribed upwards displacements were applied at the nodes of anchor plates, and increase gradually until the stabilization of the resultant force which corresponds to the ultimate pullout force Q_u of the anchor plates group (Fig. 5). It should be noted that, using a displacement loading procedure, the parameters of the plate anchor do not affect the calculation results.

137 Before adopting the reference numerical model, several calculation tests were 138 executed to check the influence of the mesh and the size of the model on calculation 139 results, which allowed to suggest not only the use of a fine mesh in the vicinity of the 140 anchor plate but also that the plate element itself must imperatively be discretized in 141 10 elements minimum on the x-y plane to get more accurate results. It was also 142 verified that the boundaries of the numerical model based on the dimensions of the 143 experimental model of Geddes and Murray (1996) have no effect on the value of the 144 ultimate force obtained. It was finally checked that the values of the elastic 145 parameters of soil have a negligible effect on the ultimate force computed by the 146 numerical analysis.

147 3 Numerical results

The numerical finite element analyses that have been performed in this study concern the calculation of the ultimate pullout capacity of a group of square anchor plates, installed in row configuration: two (2×1) , three (3×1) , four (4×1) and five (5×1) square plates, or in square configuration: four (2×2) and nine (3×3) square plates, with a constant spacing *S* between the plates varying between 0 and 2.5*B*.

The group efficiency η was analyzed as a function of the spacing/width ratio (*S/B*) for both row and square configurations for these relatively low values of *S/B* ratio. Then the critical spacing S_{cr} between anchor plates was evaluated (corresponding to $\eta =$ 100%). S_{cr} was defined as the distance from which each anchor plate acts independently without interference between failure mechanisms (results discussed in section 6).

159 **3.1** Group of square anchor plates in row configuration

Before starting the numerical analyses for group of plates, the pullout capacity of an isolated square anchor plate was calculated. The evolution of pullout load with displacement was plotted in Fig. 5 (bottom curve). The failure mechanism of this isolated square anchor plate can be observed in Fig. 2. Its shape can be considered as a truncated cone with slightly curved failure planes near the ground surface.

165 In order to investigate the influence of elastic parameters of soil on the ultimate 166 pullout capacity, the case of a single square anchor plate are analysed with different 167 values of Young's modulus (E = 10, 30 and 60 MPa). Fig. 3 shows the results 168 obtained for H/B = 4 and H/B = 6; It can be observed that the values of the elastic 169 parameters have a small effect on the ultimate pullout capacity. However, for great 170 values of *E* the ultimate load is reached for a smaller displacement.

Fig. 4 illustrates a group of square anchor plates of width *B*, installed in rowconfiguration with a similar spacing *S*. The total line length is noted *L*.

Fig. 5 shows the results of the ultimate pullout load as a function of displacement for a group of two square anchor plates with different values of *S/B* ratio varying from 0 to 2, indicating that the force Q_u increases with increasing spacing between the two anchor plates. This trend illustrates the presence of group effects on the ultimate pullout capacity. Fig. 6 presents the total displacements obtained in the case of two

anchor plates with a ratio of S/B = 2. It also shows the interference of the failure mechanisms of the two adjacent plates.

180 The group efficiency η was calculated by the following conventional relation (Das 181 (1990), Geddes and Murray (1996), Emirler et al (2015)):

$$\eta (\%) = \frac{\text{Ultimate load of group of } N \text{ anchors } \times 100}{N \times \text{ultimate load of an isolated anchor}}$$
(1)

182 with *N* the total number of anchor plates.

Fig. 7 shows the evolution of the group efficiency of square anchor plates in row configuration (two (2×1) , three (3×1) , four (4×1) and five (5×1)) with the spacing/width ratio (*S/B*). In the same figure are plotted the experimental results obtained by Geddes and Murray (1996) in the case of two (2×1) and five (5×1) plates.

188 The numerical results show that the evolution of the group efficiency as a function of 189 (S/B) ratio is perfectly linear, and may be fitted with Equations (2), (3), (4) and (5) for 190 configurations (2×1) , (3×1) , (4×1) and (5×1) respectively. For the case of two plates 191 (2 x 1), the group efficiency *n* increases linearly from 61% for S/B = 0 corresponding 192 to a rectangular plate L/B = 2 to 78% for S/B = 2. For the case of three plates (3 x 1), 193 η increase linearly from 48% for S/B = 0 corresponding to a rectangular plate L/B = 3 194 to 77% for S/B = 2.5. For the case of four plates (4 x 1), η increase linearly from 41% 195 for S/B = 0 corresponding to a rectangular plate L/B = 4 to 74% for S/B = 2.5. For five 196 plates (5 x 1), n increase also linearly from 37% for S/B = 0 corresponding to a rectangular plate L/B=5 to 72% for S/B = 2.5. 197

$$\eta_{2\times 1}(\%) = 8.537 \frac{S}{B} + 60.96 \tag{2}$$

$$\eta_{3\times 1}(\%) = 11.45\frac{S}{B} + 48.13\tag{3}$$

$$\eta_{4\times 1}(\%) = 13.25 \frac{S}{B} + 40.68 \tag{4}$$

$$\eta_{5\times 1}(\%) = 13.85 \frac{S}{B} + 36.94 \tag{5}$$

198 The values of group efficiency obtained experimentally by Geddes and Murray (1996) 199 are larger than the numerical results, except for the first point (S/B = 0) which is 200 superimposed to the numerical point in both cases (2 x 1) and (5 x 1). For the case of 201 five plates (5 x 1), the difference between the experimental and numerical results 202 increases with the increase of S/B ratio, and remains nearly constant around 10% for 203 the case of two plates (2 x 1). However, the experimental results also show a linear trend from the second point corresponding to S/B = 0.25 or S/B = 0.5. On this point, 204 205 Geddes and Murray (1996) reported that the relationship between S/B and the group 206 efficiency demonstrates an initial perturbation followed by a linear trend.

The group efficiency obtained experimentally varies from about 59% for S/B = 0 to about 90% for S/B = 2 in the case of two plates (2 x 1). For five plates, η varies from about 37% for S/B = 0 to about 71% for S/B = 2.5.

From these results in row configuration, we can conclude that the group efficiency of N plates is lower than that of (N - 1) plates for the same spacing S, and this difference of efficiency decreases when the spacing/width ratio (*S/B*) increases.

3.2 Group efficiency of square plates in square configuration

For a square configuration, Fig. 8 illustrates the two cases studied: groups of four (2 215 \times 2) and nine (3 \times 3) square anchor plates. Fig. 9 presents the total displacements 216 obtained in the case of nine anchor plates with a ratio of *S*/*B* = 2. It also shows the 217 interference between failure mechanisms of plates.

Fig. 10 shows the numerical results of these cases in comparison with the experimental results obtained by Geddes and Murray (1996). The numerical results show that η increases linearly as a function of S/B ratio, following the two Equations (6) and (7) for the case of four (2 × 2) and nine (3 × 3) plates respectively. For the case of four plates (2 × 2), η evolves linearly from 34% for *S* = 0 (corresponding to a single square plate of width equal to 2*B*), to 67% for *S/B* = 2.5. For the case of nine (3 × 3) plates, η increase from 20% for S = 0 (corresponding to the case of a single square plate of width equal to 3*B*), to 52% for *S/B* = 2.5.

The experimental results of Geddes and Murray (1996) for four square plates (2 x 2), shows that η evolves almost linearly with *S/B* ratio, from 34% for *S* = 0 to approximately 85% for *S/B* = 2.5. However, the experimental values of η are larger than the numerical values except for the case of *S/B* = 0 where the values of η are equal, then the difference between the numerical and experimental values of η increases gradually with the increase of *S/B*.

$$\eta_{2\times 2}(\%) = 13.39\frac{S}{B} + 33.48\tag{6}$$

$$\eta_{3\times3}(\%) = 12.92\frac{S}{B} + 19.81\tag{7}$$

232 It is also remarkable that for any given value for S/B ratio, the group efficiency of four 233 square anchor plates installed in square configuration is lower than in the case of 234 four square anchor plates installed in row configuration. The reason is that in square 235 configuration, the failure mechanism of each of the four plates interferes with that of 236 the two or three other plates. In row configuration, the failure mechanism of each of 237 the intermediate plates interferes with that of the two nearby plates, and the failure 238 mechanism of each of the edge plates interferes only with that of a single plate. This 239 difference of group efficiency between a row and square configuration becomes 240 larger with the increase of the number of anchor plates.

241 3.3 Load factors

The previous numerical results highlighted that the group efficiency of a group of square anchor plates installed horizontally in sand, in row or square configuration, evolves linearly with *S/B* ratio. In order to establish a general equation of the group efficiency of *N* anchor plates, the previous data of group efficiency, for row and square configurations, were redrawn in terms of load factor F_L versus *L/B* ratio. According to Geddes and Murray (1996), the following relationship holds:

$$\frac{L}{B} = n + (n-1)\frac{S}{B} \tag{8}$$

248 with n the number of plate per row,

$$F_L = \frac{Ultimate \ load \ of \ N \ plates}{Ultimate \ load \ of \ a \ single \ isolated \ plate}$$
(9)

249 or

$$F_L = \eta \times N/100 \tag{10}$$

Fig. 11 presents the variation of the load factor according to *L/B* ratio for all row configurations studied previously. The load factor evolves linearly with *L/B* ratio for two, three, four and five anchor plates in row configuration. This linear relation is best fitted by the following equation:

$$F_L = 0.182 \ (L/B) + 0.866 \tag{11}$$

From Equations (8), (10) and (11), we can write a general relation (12) of the group efficiency of *n* square anchor plates installed horizontally in the sand in row configuration (n = N). Nevertheless, this relation is valid only for the geotechnical and geometrical characteristics chosen in this study.

$$\eta_{n \times 1}(\%) = \frac{18.2}{n} \left(n + (n-1)\frac{S}{B} \right) + \frac{86.6}{n}$$
(12)

Besides, by drawing the curve of the load factor according to *L/B* ratio for the case of four and nine anchor plates in square configuration (Fig. 12), a global linear relation of the evolution of the load factor is obtained:

$$F_L = 0.561 \, (L/B) + 0.167 \tag{13}$$

So, from equations (8), (10), and (13) we can write the general relation (14) of the group efficiency of ($N = n \times n$) square anchor plates installed horizontally in the sand in square configuration, which also is valid only for the geotechnical and geometrical characteristics considered in this study:

$$\eta_{n \times n}(\%) = \frac{56.1}{n^2} \left(n + (n-1)\frac{S}{B} \right) + \frac{16.7}{n^2}$$
(14)

265 4 Parametric study

266 The previous numerical calculations have established the general Equations (12) and 267 (14) of the group efficiency for row and square configurations respectively. These 268 relations concern the case of H/B = 4, and involve the following variables: number of 269 anchor plates, spacing between anchor plates and width of plates. However, a 270 parametric study is needed to verify the influence of various parameters on the 271 obtained results. To this aim, a numerical parametric study was carried out on a 272 group of two square anchor plates, studying the influence of installation depth, 273 internal friction angle of soil, flow rule and roughness of anchors.

274 **4.1** Influence of installation depth

To study the influence of installation depth on the group efficiency, the ultimate pullout capacity of two square anchor plates was calculated for a depth/width ratio 277 H/B = 2 and H/B = 6. Then the group efficiency was calculated and compared with 278 those obtained for the reference model (H/B = 4) as shown in Fig. 13.

Fig. 13 shows that the group efficiency for a given spacing decreases when the *H/B* ratio increases. Indeed, the critical spacing (S_{cr}) increases with depth (*H*). This is explained by the relationship between the critical spacing and the installation depth theoretically estimated by $S_{cr} = 2H \tan \theta$, with θ is the inclination angle of the failure plane with the vertical as shown in Fig. 21.

In previous studies, the installation depth has also an influence on the shape of failure mechanisms. There is a critical embedment ratio which presents the transition between shallow anchor behaviour and deep anchor behaviour. Meyerhof (1973) proposed a critical embedment ratio H/B = 4 for square anchors in loose sand, and it increases up to about 8 in dense sand. Also, Das (1983) proposed an empirical correlation for the critical embedment ratio for square anchor plates in the form $H/B = 5.5 + 0.166(\varphi - 30)$, (for $30^\circ \le \varphi \le 45^\circ$).

Fig. 14 shows the total displacement for the case of two square anchor plates embedded at different depths with *H/B* varying from 4 to 10. The mechanisms are depicted by the contours of finite element displacement; where the same scale was used to present the displacement field for all embedment ratio values. It is seen that from embedment ratio $H/B \ge 8H$ the failure mechanism begins to develop locally. From the present study, the embedment ratio H/B = 8 can be considered as the critical embedment ratio.

298 **4.2** Influence of internal friction angle

The reference numerical model was studied with an internal friction angle $\varphi' = 43.6^{\circ}$. However, to study the influence of this parameter on the group efficiency, other numerical calculations were performed, also for a group of two square anchor plates,

302 with other values of the internal angle friction $\varphi' = 30^{\circ}$ and $\varphi' = 20^{\circ}$. For these values 303 of φ' , the adopted dilation angle is equal to zero. The results of numerical calculations 304 are presented in Fig. 15 showing a little influence compared to the depth parameter 305 on the group efficiency. *n* increases by 8% when φ' decreases from 43.6° to 20°. This 306 influence can be explained by the relation of the failure mechanism with the internal 307 friction angle. Some authors such as Clemence and Veesaert (1977) found that the 308 inclination angle of the failure plane with the vertical is equal to the half of the internal 309 friction angle of soil. Murray and Geddes (1987), and Merifield et al (2006) found that 310 this inclination angle is equal to the internal friction angle. So, when φ' decreases the 311 interference between failure mechanisms decreases and *n* increases.

312 4.3 Influence of dilation angle

313 To study the influence of the flow rule on the group efficiency, other numerical 314 calculations were established for the case of two square anchor plates. An 315 associated flow rule ($\psi' = \phi'$) was considered, and the obtained results of the group 316 efficiency were compared with the results of the reference case calculated with a 317 non-associated flow rule ($\psi' = \phi' - 30^\circ$). This comparison is presented in Fig. 16 and 318 shows an almost negligible effect on the group efficiency according to S/B ratio. 319 However, it should be noted that there is a significant influence of the dilation angle 320 on the value of the ultimate pullout capacity, which is overestimated with an 321 associated flow rule (up to 38%).

322 **4.4 Influence of anchor roughness**

In the reference model, the interface between the soil and the anchor plate was determined by using a strength reduction factor $R_{inter} = 0.19$. To study the influence of anchor roughness on the group efficiency, other calculations were performed for a group of two square anchor plates, with the following values of the strength reduction

327 factor $R_{inter} = 0.33$; 0.5; 0.75 and 1. The results of group efficiency are presented in 328 Fig. 17, which show that there is a very little influence on the values of group 329 efficiency. This is can be explained by the shape of failure mechanism, where there is 330 no significant mobilization of shearing resistance between the soil and the anchor 331 plate during the pullout action. Rowe and Davis (1982b) found that the roughness 332 has a negligible effect on the capacity of horizontal anchors at all depths, but 333 significantly increases that of shallow vertical anchors (H/B < 3). For this latter case, 334 they found that the effect of roughness is increased further if the soil is dilatant.

335 **5** Analytical solution for *n* square anchor plates in row configuration

336 5.1 Isolated anchor plate

Murray and Geddes (1987) have developed a failure mechanism using the upper bound limit analysis, for a rectangular anchor plate installed horizontally in a frictional soil, and subjected to a vertical pullout loading. This failure mechanism consists in a failure plane inclined at an angle φ' to the vertical at the edge of the plate. At the corners the failure mechanism consists in a portion of a circular cone. They have obtained the following expression for the break-out factor N_{γ} :

$$N_{\gamma} = 1 + \frac{H}{B} \tan \varphi' \left(1 + \frac{B}{L} + \frac{\pi}{3} \frac{H}{L} \tan \varphi' \right)$$
(15)

To simplify the analytical calculation of the interference of a group of square anchor plates, the portion of a circular cone at the corners were replaced by a vertical pyramid. The inclination angle (θ) of the failure plane with the vertical was adopted using this empirical relation $\theta = 0.785 \varphi'^{1.1}$ with φ' is expressed in degree (Fig. 18). Following the theory of Mors (1959), the ultimate pullout capacity is assumed equal to the weight of soil located within the failure mechanism; and the frictional resistance acting along the failure surface was ignored. Ilamparuthi et al. (2002) have reported that the method of Mors (1959) is usually conservative for shallow anchors but overpredicts pullout capacity for deeper anchors. This method was also followed by Ganesh and Sahoo (2015) to estimate the ultimate uplift resistance of circular anchor plate. They reported that the frictional resistance acting along the failure surface can be ignored, conservatively, for the case of shallow anchors. It is worthwhile noting that the present study considers the anchor plates embedded at shallow depth (*H=4B*).

The break-out factor of this modified failure mechanism is given in equation (16) (see details in appendix A). The values of N_{γ} obtained by this expression (16) give a very satisfactory agreement with the upper bound results obtained by Murray and Geddes (1987), and the lower bound results obtained by Merifield et al. (2006) as shown in Fig. 19.

$$N_{\gamma \ isolated} = 1 + 2\frac{H}{B}\tan\theta + \frac{2}{3}\left(\frac{H}{B}\right)^2 \tan^2\theta \tag{16}$$

In order to examine the effect of soil strength along the failure surface on the ultimate pullout capacity, numerical analyses were carried out by modeling a full-scale square plate (B = 1m) with embedment ratio H/B varying from 1 to 5, and $\phi' = 20^{\circ}$, 30° and 40° by considering an associative flow rule. The model adopted in these numerical analyses, has a depth of 10 m and extends 6 m beyond the planes of symmetry.

The values of the break-out factor Ny obtained from the present numerical analyses were compared with those calculated with the expression (16) as shown in Fig. 20. The comparison shows that the values of Ny obtained by the expression (16) are slightly smaller than the numerical values. Consequently, when the soil strength along the failure surface is ignored, the result always errs on the safe side; it underestimates the ultimate pullout capacity. However, the relative error from the use 373 of this assumption varies between 3% and 17%, and it increases slightly with the 374 increase in embedment ratio.

375 **5.2 Two square anchor plates**

For a group of two square anchor plates spaced by $S < 2H \tan \theta$, the ultimate pullout capacity of each anchor plate is simply equal to the weight of the soil located within the failure mechanism (defined by points a, b, c, d, e for the left anchor, as shown in Fig. 21). The break-out factor corresponding to this volume is noted by N_{yend} and given by: (see details in appendix B)

$$N_{\gamma end} = 1 + \frac{1}{3} \left(\frac{H}{B}\right)^2 (\tan\theta)^2 + \frac{1}{2} \left(3 + \frac{S}{B}\right) \frac{H}{B} \tan\theta + \frac{1}{8} \frac{S}{H} \frac{S}{B} \left(\frac{1}{3} \frac{S}{B} - 1\right) \cot\theta - \frac{1}{4} \left(\frac{S}{B}\right)^2 + \frac{1}{2} \frac{S}{B}$$
(17)

381 The group efficiency of two anchor plates noted $\eta_{2\times 1}$ can be calculated with the 382 following relationship:

$$\eta_{2\times 1}(\%) = \frac{N_{\gamma \ end}}{N_{\gamma \ isolated}} \times 100 \tag{18}$$

Fig. 22 shows the group efficiency of two anchor plates as a function of *S/B* ratio, as predict by Equation (18), in comparison with our numerical results and the experimental results obtained by Geddes and Murray (1996). Additional calculations were performed using Plaxis software for (*S/B* = 4.5, 5 and 5.5).

In general, it can be noted that the analytical results are in good agreement with
numerical results. However, the experimental results obtained by Geddes and Murray
(1996) show higher values than both analytical and numerical results.

390 **5.3** *n* square anchor plates in row configuration

For a group of *n* square anchor plates spaced by $S < 2H \tan \theta$, the ultimate pullout capacity of an intermediate anchor plate is simply equal to the weight of the soil located within the failure mechanism defined by points a, b, c, d, e, f as shown in Fig. 394 23. The break-out factor corresponding to this volume is noted $N_{\gamma inter}$ and given by: 395 (see details in appendix C)

$$N_{\gamma \ inter} = 1 + \left(1 + \frac{S}{B}\right) \frac{H}{B} \tan \theta - \frac{1}{3} \frac{S}{B} \frac{S}{H} \left(\frac{1}{4} \frac{S}{B} - 1\right) \cot \theta - \frac{1}{2} \left(\frac{S}{B}\right)^2 + \frac{S}{B}$$
(19)

396 In this case, the group efficiency of *n* anchor plates can be calculated with the 397 following expression:

$$\eta_{n\times 1}(\%) = \frac{(n-2)N_{\gamma inter} + 2N_{\gamma end}}{n N_{\gamma isolated}} \times 100$$
(20)

Fig. 24 shows the comparison of numerical, analytical and experimental results of the group efficiency of five square anchor plates in row configuration. These results correspond to small values of the spacing between the plates (0 < S/B < 2). A good agreement is observed between the analytical results and the numerical results.

402 6 Critical spacing for two square anchor plates

Based on previous analytical and numerical results, we can determine the critical spacing for which two anchor plates (placed at a depth H = 4B in this study) act independently, so that the group efficiency is equal to 100%.

The numerical results highlight that a critical spacing of $S_{cr} = 5.5B$, is necessary for a group of anchor plates installed in linear configuration to obtain a group efficiency of 100%. The critical spacing obtained by equation (12) is $S_{cr} = 4.24B$. However, the additional calculations performed for verification by Plaxis software have given a group efficiency $\eta = 97\%$ for S/B = 4.24 as shown in Fig. 22.

The analytical calculation have given results very similar to the numerical results especially for small values of *S/B* (0 < *S/B* <2). However the critical spacing obtained analytically for $\eta = 100\%$ is $S_{cr} = 7.5B$ as shown in Fig. 22. Despite this remarkable difference between the critical spacing obtained by the numerical calculation and that obtained by an analytical solution, the relative error between them is of the order of 416 3.86% for a critical spacing $S_{cr} = 5.5B$. On the other hand, Geddes and Murray 417 (1996) found in their experimental study a critical spacing of $S_{cr} = 2.9B$.

418 In addition, there is little information in the literature on the critical spacing with the 419 exception of the works presented in Table 3. It is important to examine the 420 experimental study of Abbad et al. (2013) on the interference of square anchor plates 421 (B = 5 cm) installed at a depth of H = 5B in a material made of plastic grains with a 422 diameter of 1 mm. The analogical medium has a relative density of Dr = 96% ($e_{min} =$ 0.302, $e_{max} = 0.855$), with a dry unit weight of $\gamma_d = 14.6 \text{ kN/m}^3$, a null cohesion and an 423 424 initial friction angle $\varphi = 39^{\circ}$. Using high resolution digital pictures, they have found that a minimum spacing $S_{cr} = 6B$, is necessary for two anchor plates to act 425 426 independently.

427 Das and Yang (1987) has developed an experimental study for circular anchor plates 428 embedded in a sand with $\varphi' = 37^{\circ}$, he found a critical spacing $S_{cr} = 3D$. For the same 429 characteristics, Meyerhof and Adams (1986) found $S_{cr} = 1.8D$.

The difference observed between the critical spacing obtained numerically and that obtained analytically is attributed to the shape of the failure mechanism. Analytical calculations consider an associated soil ($\psi' = \phi'$), which overestimates the ultimate pullout capacity and provides a larger failure mechanism, thus requiring a bigger critical spacing. Inversely, the numerical calculations, account for a non-associated flow rule ($\psi' = \phi' - 30^\circ$) which induce a narrower failure mechanism thus requiring a smaller critical spacing.

437 7 Conclusion

The ultimate pullout capacity of a group of square anchor plates in row or square configurations was calculated, using three-dimensional finite elements analyses. The square anchor plates were installed horizontally in dense sand and pulled vertically. The soil is characterized by the Mohr-Coulomb yield criterion and non-associative flow rule. In this study, a simple three-dimensional failure mechanism has been proposed to evaluate the anchor break-out factor and the group efficiency. The evolution of the group efficiency η with the spacing/width ratio (*S/B*) was analyzed and compared with results available in the literature.

446 In this paper, a numerical parametric study was conducted on a group of two square 447 anchor plates to identify the most influential parameters on the group efficiency. This 448 parametric study revealed that the group efficiency *n* increases considerably with the 449 decrease of the internal friction angle φ' , and the installation depth H. On the other 450 hand, n is slightly influenced by the anchor roughness and the choice of an 451 associative flow rule. Nevertheless, it is worthwhile noting that the associative flow 452 rule highly overestimates the value of the ultimate pullout capacity. The group 453 efficiency of N square anchor plates installed in row configuration is greater than that 454 of *N* square anchor plates installed in square configuration.

455 The comparison of the numerical results with analytical solutions confirmed that the 456 proposed failure mechanism predict a group efficiency values in good agreement with 457 those obtained by elasto-plastic analyses. New equations are developed in this study 458 to evaluate the group efficiency of shallow square anchor plates (H=4B). The group 459 efficiency evolves linearly with S/B ratio, until a critical value of the spacing between 460 plates beyond which the anchor plates act independently. For this critical spacing, the 461 ultimate pullout load of the group arrives at its maximal value and remains stable, in 462 spite of the increase of the spacing. The value of critical spacing for which the two 463 square anchor plates can be assumed isolated, as predicted by the present 464 numerical computations, is approximately 5.5 times the width of the plate B.

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467 **References**

- Abbad, H., Meghachou, M., Dekar, C., and Daoud, S. M. (2013). Interaction of
 Rupture Zones of Adjacent Anchor Plates in an Analogical Medium. *ETASR Engineering, Technology & Applied Science Research*, 3(6):562-565.
- 471 2. Ardebili ZA, Gabr MA, Rahman MS (2016). Uplift Capacity of Plate Anchors in
 472 Saturated Clays: Analyses with Different Constitutive Models. *International*473 *Journal of Geomechanics*, *16*(2), 4015053.
- 3. Bhattacharya, P., and Kumar, J. (2014). Vertical pullout capacity of horizontal
 anchor plates in the presence of seismic and seepage forces. *Geomechanics and Geoengineering*, 9(4):294-302.
- 477 4. Bolton, M. D. (1986). The strength and dilatancy of sands. *Géotechnique*478 36(1):65-78
- 479 5. Brinkgreve, R.B.J., and Vermeer, P.A. (2001). Plaxis Finite Element Code for
 480 Soil and Rock Analyses, Version 1, BALKEMA.
- 481 6. Clemence SP, Veesaert CJ (1977) Dynamic pullout resistance of anchors in
 482 sand. In: roceedings of the International Symposium on Soil-Structure
 483 Interaction, Roorkee, India, pp 389–397
- 484 7. Das B. M., Yang Jin-Kaun (1987), Uplift Capacity of Model Group Anchors in
 485 Sand. Foundations for Transmission Line Towers, *Geotechnical Special*486 *Publication* No. 8, ASCE
- 487 8. Das, B. M. (1978). Model tests for uplift capacity of foundations in clay. *Soils*488 and Found. 18(2):17-24.
- 489 9. Das, B.M., (1983). A procedure for estimation of uplift capacity of rough piles.
 490 Soils and Found., Japan, 23(3):122-126.
- 491 10. Das, B. M. (1990). *Earth Anchors. Developments in Geotechnical Engineering*,
- 492 50: 1-241.

- 493 11. Emirler, B. Bildik, S., and Laman, M. (2015). Numerical Investigation of Group
 494 Anchors. *IFCEE 2015* © *ASCE* 279–288.
- 495 12. Ganesh, R., and Sahoo, J. P. (2015). Influence of ground water on the
 496 ultimate uplift resistance of circular plate anchors. 50th Indian geotechnical
 497 Conference 17th 19th December 2015, Pune, Maharashtra, India.
- 498 13. Geddes, J.D., and Murray, E.J. (1996). Plate anchor groups pulled vertically in
 499 sand. *J. Geotech. Engrg.*, ASCE 122(7):509–516.
- 500 14. Ghosh, P., and Kumari, R. (2012) Seismic interference of two nearby
 501 horizontal strip anchors in layered soil. *Nat Hazards*, 63:789–804
- 502 15. Hanna, A., Ayadat, T., and Sabry, M. (2007). Pullout resistance of single
 503 vertical shallow helical and plate anchors in sand. *Geotechnical and*504 *Geological Engineering*, 25(5):559–573.
- 505 16. Hanna A, Rahman F, Ayadat T (2011) Passive earth pressure on embedded
 506 vertical plate anchors in sand. Acta Geotechnica, 6(1), 21–29.
- 507 17. Ilamparuthi, K., Dickin, E. A., and Muthukrisnaiah, K. (2002). Experimental
 508 investigation of the uplift behaviour of circular plate anchors embedded in
 509 sand. *Can. Geotech. J.*, 39: 648–664.
- 510 18. Khatri, V. N., and Kumar, J. (2009). Vertical uplift resistance of circular plate
 511 anchors in clays under undrained condition. *Computers and Geotechnics*,
 512 36(8):1352–1359.
- 513 19. Khatri, V. N., and Kumar, J. (2010). Stability of an unsupported vertical circular
 514 excavation in clays under undrained condition. *Computers and Geotechnics*,
 515 37(3):419–424.
- 516 20. Khatri, V. N., and Kumar, J. (2011). Effect of anchor width on pullout capacity
 517 of strip anchors in sand. *Canadian Geotechnical Journal*, 48(3):511–517.

- 518 21. Kouzer, K. M., and Kumar, J. (2009a). Vertical uplift capacity of two interfering
 519 horizontal anchors in sand using an upper bound limit analysis. *Computers*520 *and Geotechnics*, 36(6):1084–1089.
- 521 22. Kouzer, K. M., and Kumar, J. (2009b). Vertical uplift capacity of equally 522 spaced horizontal strip anchors in sand. *International Journal of* 523 *Geomechanics*, 9(5):230-236.
- 524 23. Kumar, J., and Kouzer, K.M. (2008a). Vertical uplift capacity of a group of 525 shallow horizontal anchors in sand. *Géotechnique*, 58(10):821–823.
- 526 24. Kumar, J., and Naskar, T. (2012). Vertical uplift capacity of a group of two
 527 coaxial anchors in a general c–φ soil. *Canadian Geotechnical Journal*, 49(3):
 528 367–373.
- 529 25. Mabrouki, A., and Mellas, M. (2014). Étude tridimensionnelle de la capacité
 530 ultime des plaques d'ancrage dans un sol frottant. *Courrier Du Savoir*,
 531 (18):15–19.
- 532 26. Merifield, R.S., and Sloan, S.W. (2006). The ultimate pullout capacity of 533 anchors in frictional soils. *Can. Geotech. J.* 43(8):852–868.
- 534 27. Merifield R S, Lyamin A V, Sloan S W (2006) Three dimensional lower bound
 535 solutions for the stability of plate anchors in sand. Géotechnique 56(2):123–
 536 132.
- 537 28. Merifield, R.S and Smith, C.C. (2010). The ultimate uplift capacity of multi538 plate strip anchors in undrained clay. *Computers and Geotechnics* 37:504–514
 539 29. Meyerhof, G. G. and Adams, J. I. (1968). The ultimate uplift capacity of
 540 foundations. *Canadian Geotechnical Journal* 5(4):225–244.
- 541 30. Meyerhof, G. G. (1973) "Uplift resistance of inclined anchors and piles" Proc.
 542 of VIII International Conference on Soil mechanics and Foundation
 543 Engineering, Moscow, USSR, 2, 1, 167-172.

- 544 31. Mors, H. (1959). The behaviour of mast foundations subject to tensile forces.
 545 *Bautechnik*, 10: 367–378.
- 546 32. Murray, E. J., and Geddes, J. D. (1987). Uplift of anchor plates in sand. *J.* 547 *Geotech. Engrg.*, 113(3):202–215.
- 548 33. Rowe, R. K. and Davis, E. H. (1982b). The behaviour of anchor plates in sand.
 549 *Géotechnique*, 32(1):25–41.
- 34. Sahoo, J. P., and Kumar, J. (2014a). Vertical uplift resistance of two closely
 spaced horizontal strip anchors embedded in cohesive frictional weightless
 medium. *Can. Geotech. J.*, 51:223–230.
- 35. Sahoo, J. P., and Kumar, J. (2014b). Vertical uplift resistance of two interfering
 horizontal anchors in clay. *J. Geotech. Geoenviron. Eng.*, 140(4):06013007
- 555 36. Wang, D., Merifield, R.S., and Gaudin, C. (2013). Uplift behaviour of helical 556 anchors in clay. *Can. Geotech. J.* 50:575-584.
- 557

558 Appendix A: Analytical solution of break-out factor $N_{\gamma isolated}$ for an isolated 559 square anchor plate

560 Volumes of the portions 1, 2 and 3 shown in Fig. 25:

$$V_1 = B^2 H \tag{21}$$

$$V_2 = 0.5BH^2 \tan\theta \tag{22}$$

$$V_3 = \frac{1}{6} H^3 \tan^2 \theta$$
 (23)

561 The ultimate pullout load Q_u is equal to the weight of the soil located within the failure 562 mechanism:

$$Q_u = \gamma (V_1 + 4V_2 + 4V_3) \tag{24}$$

563 Using Equations 21, 22 and 23, we finally get:

$$Q_u = B^2 \gamma H + 2\gamma H^2 B \tan \theta + \frac{2}{3} \gamma H^3 \tan^2 \theta$$
⁽²⁵⁾

564 By definition, the ultimate pullout capacity q_u :

$$q_u = \frac{Q_u}{A} = \frac{Q_u}{B^2} \tag{26}$$

$$q_u = \gamma H \left(1 + 2\frac{H}{B} \tan \theta + \frac{2}{3} \left(\frac{H}{B}\right)^2 \tan^2 \theta \right)$$
(27)

565 By convention, q_u is also given by:

$$q_u = \gamma H N_{\gamma} \tag{28}$$

566 So that the break-out factor N_{γ} for an isolated square plate anchor is:

$$N_{\gamma \, isolated} = 1 + 2 \frac{H}{B} \tan \theta + \frac{2}{3} \left(\frac{H}{B}\right)^2 \tan^2 \theta \tag{29}$$

567 Appendix B: Analytical solution of break-out factor $N_{\gamma end}$ for a square anchor 568 plate located at an end

569 For two or n square anchor plates with $S < 2H \tan \theta$, the ultimate pullout load of one 570 anchor plate at the end is equal to the weight of the soil located within its failure 571 mechanism defined by points a, b, c, d, e shown in Fig. 21.

572 Volumes of the portions 4 and 5 shown in Fig. 26:

$$V_4 = \frac{1}{2} (2H \tan \theta - S) \left(H - \frac{S}{2} \cot \theta \right) B$$
(30)

$$V_4 = BH^2 \tan \theta + B \frac{S^2}{4} \cot \theta - BSH$$
(31)

$$V_{5} = \frac{1}{3} \times \frac{1}{2} \left(\sqrt{2}H \tan \theta - S \frac{\sqrt{2}}{2} \right)^{2} \left(H - \frac{S}{2} \cot \theta \right)$$
(32)

$$V_5 = \frac{1}{3}H^3 \tan^2 \theta - \frac{1}{2}SH^2 \tan \theta - \frac{S^3}{24}\cot \theta + \frac{1}{4}S^2H$$
(33)

573 The volume V corresponding to points a, b, c, d, e shown in Fig.16 is equal to:

$$V = V_T - \frac{1}{2}V_4 - 2\left(\frac{1}{2}V_5\right) = V_T - \frac{V_1}{2} - V_5$$
(34)

574 Where V_{T} is the total volume of soil located within the failure mechanism for an 575 isolated square anchor plate.

576 So:

$$V = B^{2}H + \frac{3}{2}H^{2}B\tan\theta + \frac{1}{3}H^{3}\tan^{2}\theta - \frac{1}{8}BS^{2}\cot\theta + \frac{1}{2}BSH + \frac{1}{2}SH^{2}\tan\theta + \frac{1}{24}S^{3}\cot\theta - \frac{1}{4}S^{2}H$$
(35)

577 The ultimate pullout capacity of anchor plate located at the end is then:

$$q_{u\,end} = \frac{Q_{u\,end}}{A} = \frac{Q_{u\,end}}{B^2} = \frac{\gamma \times V}{B^2}$$
(36)

578 Using Equation 35, we get:

$$q_{u\,end} = \gamma H \left(1 + \frac{3}{2} \left(\frac{H}{B} \right) \tan \theta + \frac{1}{3} \left(\frac{H}{B} \right)^2 (\tan \theta)^2 - \frac{1}{8} \left(\frac{S}{B} \right) \left(\frac{S}{H} \right) \cot \theta + \frac{1}{2} \left(\frac{S}{B} \right) \left(\frac{H}{B} \right) \tan \theta + \frac{1}{24} \left(\frac{S}{B} \right)^2 \left(\frac{S}{H} \right) \cot \theta - \frac{1}{4} \left(\frac{S}{B} \right)^2 \right)$$
(37)

579 Since:

$$q_{u\,end} = \gamma H N_{\gamma\,end} \tag{38}$$

580 We finally obtained $N_{\gamma end}$

$$N_{\gamma end} = 1 + \frac{1}{3} \left(\frac{H}{B}\right)^2 (\tan \theta)^2 + \frac{1}{2} \left(3 + \frac{S}{B}\right) \frac{H}{B} \tan \theta + \frac{1}{8} \frac{S}{HB} \left(\frac{1}{3} \frac{S}{B} - 1\right) \cot \theta - \frac{1}{4} \left(\frac{S}{B}\right)^2 + \frac{1}{2} \frac{S}{B}$$
(39)

581

582 Appendix C: Analytical solution of break-out factor $N_{\gamma \text{ inter}}$ for an intermediate

583 square anchor plate

For *n* square anchor plates in row configuration with $S < 2H \tan \theta$, the ultimate pullout load of an intermediate anchor plate is equal to the weight of the soil located within its failure mechanism defined by points a, b, c, d, e, f as shown in Fig. 23. The breakout factor corresponding to this volume is noted $N_{\gamma inter}$

588 The volume *V* corresponds to points a, b, c, d, e, f shown in Fig.18 is equal to:

$$V = V_T - 2\left(\frac{1}{2}V_4\right) - 4\left(\frac{1}{2}V_5\right) = V_T - V_4 - 2V_5$$
(40)

- 589 Where V_{T} is the total volume of soil located within the failure mechanism for an 590 isolated square anchor plate.
- 591 Using Equations (31 and 33), we obtain:

$$V = B^{2}H + H^{2}B\tan\theta - \frac{1}{4}BS^{2}\cot\theta + BSH - SH^{2}\tan\theta + \frac{1}{12}S^{3}\cot\theta - \frac{1}{2}S^{2}H$$
 (41)

592 The ultimate pullout capacity of one anchor plate located between two anchor plates593 is given by:

$$q_{u\,inter} = \frac{Q_{u\,inter}}{A} = \frac{Q_{u\,inter}}{B^2} = \frac{\gamma \times V}{B^2}$$
(42)

$$q_{u\,inter} = \gamma H \left(1 + \left(\frac{H}{B}\right) \tan \theta - \frac{1}{4} \left(\frac{S}{B}\right) \left(\frac{S}{H}\right) \cot \theta + \frac{S}{B} + \left(\frac{S}{B}\right) \left(\frac{H}{B}\right) \tan \theta + \frac{1}{12} \left(\frac{S}{B}\right)^2 \left(\frac{S}{H}\right) \cot \theta - \frac{1}{2} \left(\frac{S}{B}\right)^2 \right)$$

$$(43)$$

594 Since:

$$q_{u\,inter} = \gamma H N_{\gamma\,inter} \tag{44}$$

595 We get:

$$N_{\gamma inter} = 1 + \left(1 + \frac{S}{B}\right)\frac{H}{B}\tan\theta - \frac{1}{3}\frac{S}{B}\frac{S}{H}\left(\frac{1}{4}\frac{S}{B} - 1\right)\cot\theta - \frac{1}{2}\left(\frac{S}{B}\right)^2 + \frac{S}{B}$$
(45)

596

597 List of figures captions:

- 598 Fig. 1 Geometrical model of group of four square anchor plates
- 599 Fig. 2 Total displacements for an isolated square anchor plate (H/B=4)
- Fig. 3 Influence of Young's modulus on the pullout load for an isolated plate (H/B = 4,

601 H/B = 6)

- 602 Fig. 4 Group of square anchor plates in row configuration
- 603 Fig. 5 The ultimate pullout load versus displacement for two anchor plates with
- 604 varying spacing and an isolated anchor plate

- Fig. 6 Deformed mesh for two anchor plates, H/B = 2 and S/B = 2
- Fig. 7 Group efficiency of square anchor plates in row configuration
- 607 Fig. 8 Group of square anchor plates in square configuration
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- 609 = 4 and S/B = 2
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- 624 square anchor plates
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- 626 Fig. 24 Comparison of numerical, analytical and experimental results of group
- 627 efficiency of five square plates in row configuration
- 628 Fig. 25 Failure mechanism for isolated square plate
- 629 Fig. 26 Interference detail of two failure mechanisms

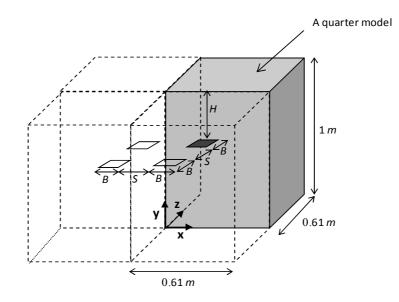


Fig. 1

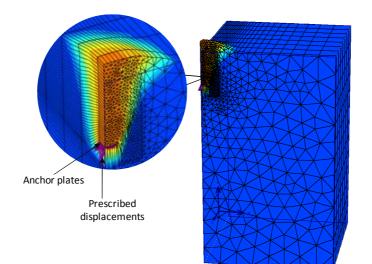


Fig. 2

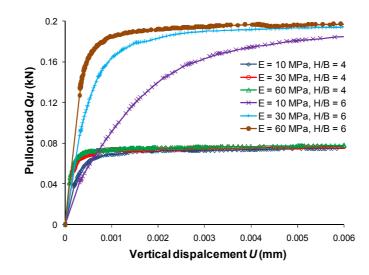


Fig. 3

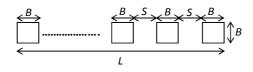


Fig. 4

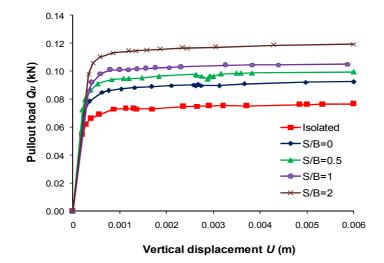


Fig. 5

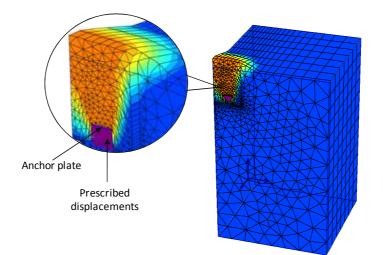


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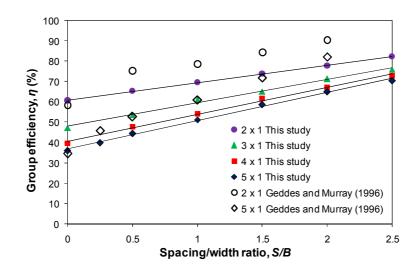
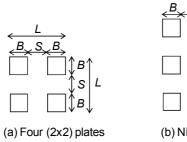


Fig. 7



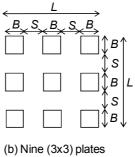


Fig. 8

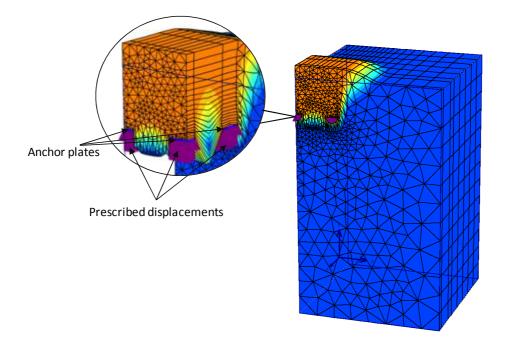


Fig. 9

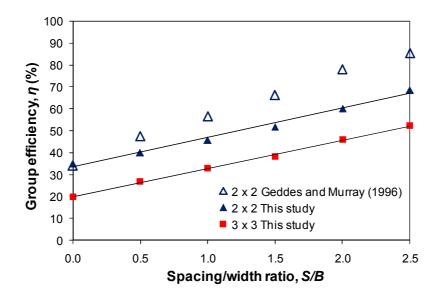


Fig. 10

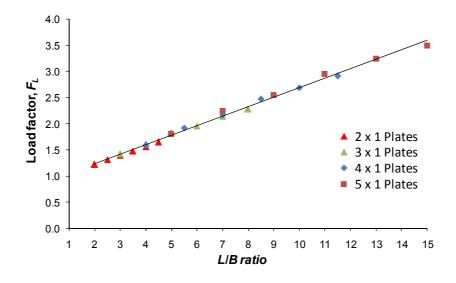


Fig. 11

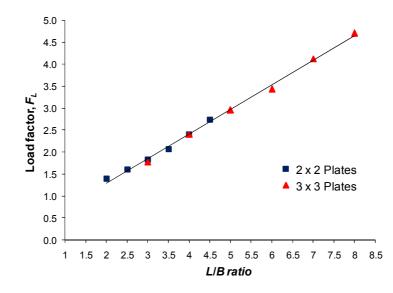


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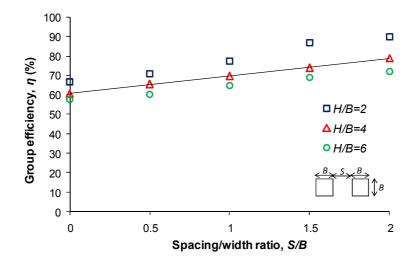


Fig. 13

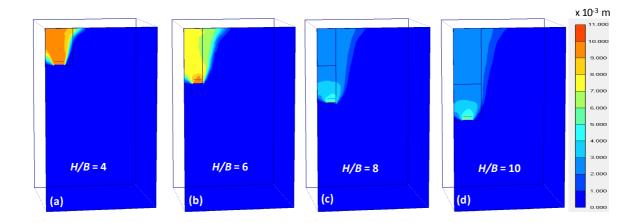


Fig. 14

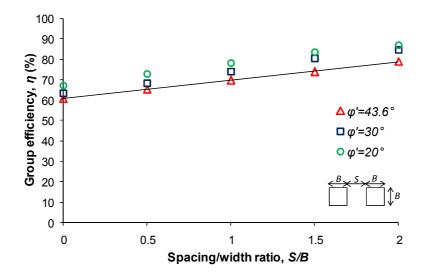


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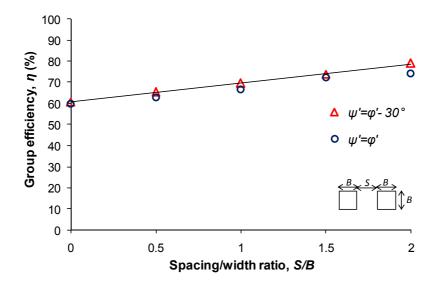


Fig. 16

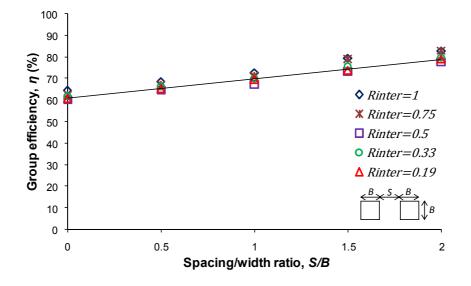


Fig. 17

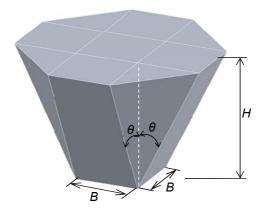


Fig. 18

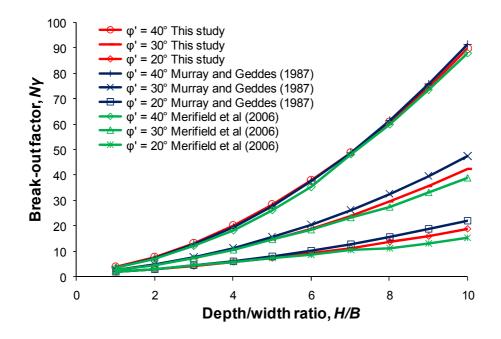


Fig. 19

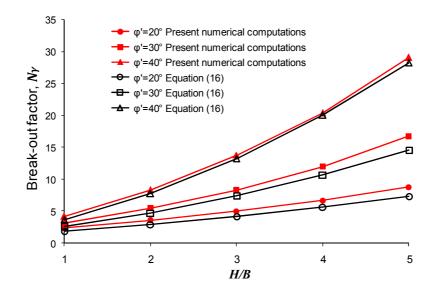


Fig. 20

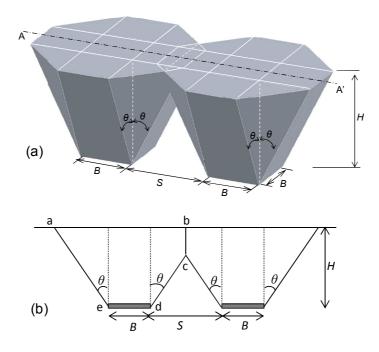


Fig. 21

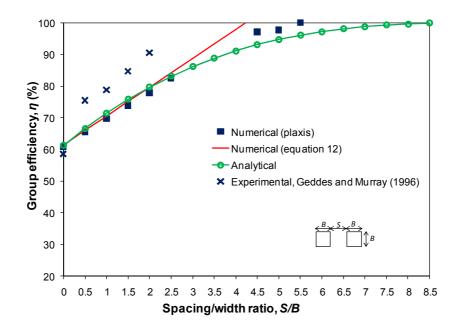


Fig. 22

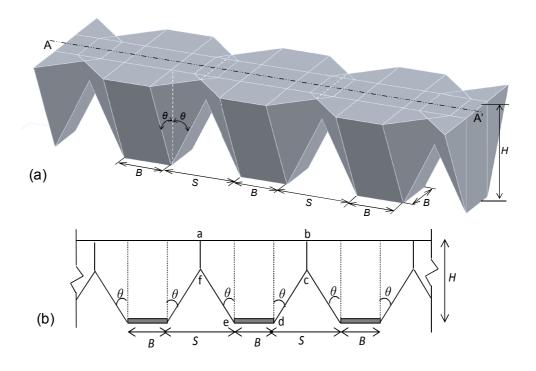


Fig. 23

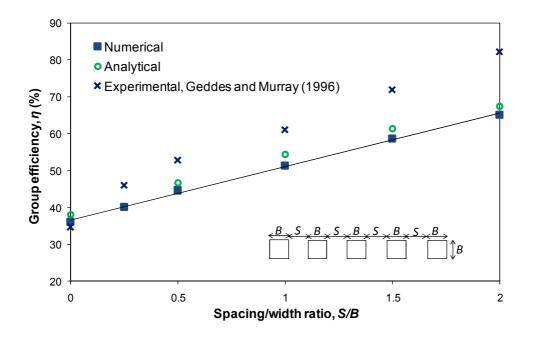


Fig. 24

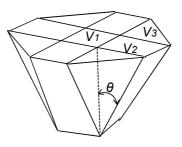


Fig. 25

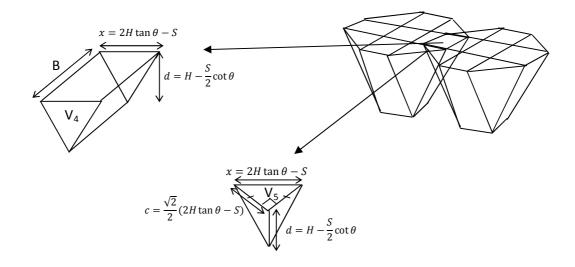


Fig. 26