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1	Mesoscopic prediction on the effective thermal conductivity
2	of unsaturated clayey soils with double porosity system
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18 Abstract: The effect of water distribution on heat conduction in unsaturated structural clayey soils 19 with double porosity system is investigated in the present study. A dual-porosity model consisting 20 of intra-aggregate and inter-aggregate pores is developed to describe the water distribution within 21 intra-aggregate and inter-aggregate pores. Heat transfer using this model is then numerically 22 simulated to determine the soil effective thermal conductivity. The obtained values are compared 23 with available experimental data. The results show that the model can predict the accurate soil 24 thermal conductivity values at various water contents and densities. On one hand, the model 25 shows a higher soil thermal conductivity when water content and/or dry density are higher. On the 26 other hand, the model shows an effect of water distribution on the soil thermal conductivity; this 27 later is higher when water is preferentially distributed within aggregates than between aggregates. 28 In addition, the model can give a direct visualization of heat transfer mechanisms in unsaturated 29 clayey soils with double porosity system. In fact, heat conduction is dominant in the wet region of 30 the dual-porosity space. This study provides both a useful predictive model of thermal 31 conductivity and a better understanding on the physical mechanism of heat conduction in 32 unsaturated structural clayey soils or other multiphase media with double porosity system.

33

34 **Keywords:** dual-porosity model; thermal conductivity; water distribution; QSGS method

35

36 **1. Introduction**

Thermal conductivity (λ) is one of the fundamental soil thermal properties. Understandings on soil
 thermal conductivity is particularly important when heat conduction process is taken into account

39	in a large number of geotechnical and geological applications, including energy-saving materials
40	[1], radioactive waste disposal [2, 3], energy foundations [4-6], freezing methods [7] and moisture
41	monitoring [8]. Soil thermal conductivity depends on numerous factors such as mineralogy, dry
42	density, water content, temperature and microstructure, among which water content is found to be
43	the most important factor to consider. In fact, water content is particularly important to consider in
44	many applications because it is more likely to change appreciably in the field under changing
45	atmospheric or boundary conditions unlike other factors (i.e. mineralogy, grain size) which remain
46	relatively constant [9]. The influence of soil water content on thermal conductivity has been
47	investigated extensively [3, 10-12] and a large number of models have been developed to predict
48	soil thermal conductivity from its water content [13-16]. However, the influences of water on heat
49	conduction are twofold: λ depends not only on the water content, but also on water distribution in
50	soil pores [9, 17-19]. Due to the aggregation nature of fine grains, the microstructure of clayey
51	soils is usually described as families of pores: intra-aggregate pores and inter-aggregate pores
52	[20-23]. The presence of double porosity system results in two kinds of water defined as
53	intra-aggregate water and inter-aggregate water. Intra-aggregate water facilitates heat conduction
54	within aggregates by reducing thermal resistance between fine particles inside a single aggregate,
55	while inter-aggregate water expedites heat conduction between aggregates by enhancing thermal
56	contacts between them [21, 24]. It is thus clear that there are some differences between
57	intra-aggregate water and inter-aggregate water in promoting heat conduction process through
58	structural clayey soils with dual-porosity system.

60 The thermal conductivity of these structural soils like compacted clayey soils has been extensively

61 investigated [21, 24, 25], but most researches so far are based on experimental tests, which can 62 only present an empirical relation between thermal conductivity and water contents. Experimental 63 researches are phenomenological in nature, besides, the empirical relations between thermal conductivity and total water contents could not properly relate intra-aggregate water and 64 65 inter-aggregate water to thermal conductivity and distinguish the different effects between intra-aggregate water and inter-aggregate water on heat conduction. Chen et al. [15] investigated 66 the thermal conductivity of compacted bentonite by using Eshelby inclusion theory in mesoscale, 67 68 which has obtained a series of meaningful knowledge. However, the inclusion method is limited in 69 describing the connection between pores [26], which indeed matters in water flow in soils. 70 Simultaneously, it might also affect heat flow process to some extent, especially for structural 71 clayey soils with complex dual-porosity system [27, 28].

72

73 Recently, numerical simulations [29-32] on pore-scale heat conduction in porous media have been 74 performed. Most simulations focused on the effective thermal conductivity of single-porosity 75 media, Wang, Pan [33] developed a prevalent stochastic reconstruction approach, the Quartet 76 Structure Generation Set (QSGS) method, to investigate the effect of particle size and water 77 distribution on soil thermal conductivity. It is well known that clayey soils compacted on the wet side of the Optimum Water Content (OMC), i.e. at a water content higher than OMC, has a 78 79 single-porosity structure [28] while it has a dual-porosity structure [34] when compacted on the dry 80 side of OMC. Therefore, the simulations above based on QSGS method are only suitable for 81 granular sandy soils and clayey soils compacted on the wet side of OMC rather than structural 82 soils with dual-porosity system such as aggregated soils and clayey soils compacted on the dry

83	side of OMC. It is then interesting to apply dual-porosity models to simulate heat conduction
84	when working on a predictive model for soil with dual porosity system.

86 In the present work, the QSGS method proposed by Wang et al. [35] is adapted to structural clayey 87 soils with dual-porosity system. The modified model is then validated with available experimental 88 data. That allows giving a better understanding on the heat transfer process at pore scale.

89 **2. Numerical framework**

90 In the present study, the integration strategy and QSGS approach are combined to investigate the 91 thermal conductivity of structural clayey soils with dual-porosity system. QSGS method usually 92 generates a pore-system with a uniform pore size that is manageable for single-porosity media 93 with a relatively narrow range of pore size. Nevertheless, for dual-porosity media exhibiting 94 different range of pore sizes at dual-scale, the QSGS method would not be appropriate. Integration 95 strategy is quite suitable for dual-porosity media by superimposing one pore-system into another pore-system to form a combined cross-scale pore-system. An example of superposition modelling 96 97 approach can also be seen in the work of Jiang et al.[36]. Hence, in the present study, the 98 dual-porosity structure is generated by using QSGS method twice following the integration 99 strategy. The schematic view of the method is shown in Fig. 1 and the details of this method 100 (including 5 steps) are presented as follows.

101 2.1. Step 1 - Extraction of the statistical information about the pore 102 network

103 To construct stochastically the pore network of dual-porosity soils, the statistical information of 104 both inter-aggregate and intra-aggregate pores is determined in advance. The statistical 105 information of different pores can be obtained based on the pore size distribution (PSD) curve. 106 From the PSD curve, the density distribution of pore size can be interpreted directly by figuring 107 out the area corresponding to the two porosity levels. This approach is easily applicable when the 108 bi-modal shape of PSD curve is apparent [37]. The void ratio and the porosity of intra-aggregate pores are defined as $e_{\rm m}$ and $P_{\rm m}$, while the void ratio and the porosity of inter-aggregate pores are 109 110 defined as e_M and P_M (stage 1 in Fig. 1). Besides, another statistical information is about the 111 number densities of intra-aggregate and inter-aggregate pores as well as solid particles. The 112 physical meaning of the number density for intra-aggregate pores is that the numbers of 113 intra-aggregate pores in a unit volume, and the same for the meaning of the number density for 114 inter-aggregate pores and solid particles. The number densities of intra-aggregate pores, 115 inter-aggregates pores and solid particles are named as n_{dm} , n_{dM} and n_{ds} , respectively. n_{dm} and n_{dM} 116 can be obtained from the PSD curve as well. For a given structural clayey soil with dual-porosity system, the average volume of inter-aggregate pores is set to be $v_{\rm M}$ from the PSD curve. The 117 118 number density of inter-aggregate pores, n_{dM} , can be derived as follows:

119
$$n_{\rm dM} = \frac{P_{\rm M}V}{v_{\rm M}V} = \frac{P_{\rm M}}{v_{\rm M}}$$
 (1)

120 where *V* is the total volume of all pores and solid particles.

121

122 The number density of intra-aggregate pores, n_{dm} , can be defined as follows:

123
$$n_{\rm dm} = \frac{P_{\rm m}V}{v_{\rm m}V} = \frac{P_{\rm m}}{v_{\rm m}}$$
 (2)

124 where $v_{\rm m}$ is the average volume of intra-aggregate pores.

125

126 The number density of solid particles,
$$n_{\rm ds}$$
, can be calculated as follows:

127
$$n_{\rm ds} = \frac{P_{\rm s}V}{v_{\rm s}V} = \frac{P_{\rm s}}{v_{\rm s}}$$
 (3)

128 where P_s and v_s are the fraction of solid particles and the average volume of all solid particles. v_s

129 can be reached from particle size distribution curve directly.

130

131 2.2. Step 2 - Stochastic generation of inter-aggregate pore network

In the present work, a 2D grid-system is employed to generate a pore network from theinformation extracted at Step 1.

134

135 Prior to generate the dual-porosity structure and water distribution by QSGS approach, the four 136 classical parameters in QSGS approach must be introduced in advance. They are core distribution probability (C_d) , directional growth probability (D_i) , volume fraction (P_n) and phase interaction 137 growth probability (I_i^{ab}) . As stated by Wang, Pan [33], the core distribution probability C_d is 138 139 defined as the probability of a cell in a grid system to become a core of the first growing phase. 140 Each grid will generate automatically a random number following a uniform distribution function within (0, 1). If this number is smaller than C_d , then this grid will become the growing phase. The 141 142 directional growth probability D_i is defined as the probability for a neighbor cell to become part of the growing phase in the direction i (i = 1-8; see Fig. 2). The volume fraction P_n is the proportion 143

of the growing phase in the grid system. If the growing phase is air, the volume fraction is usually expressed as the porosity *n*. The phase interaction growth probability I_i^{ab} is defined as the growing probability of a phase on b phase along the direction *i*. In clayey soils, due to the strong interactions between particles and bound water, the growing probability of water phase on solid phase is much larger than that of water phase on water phase along each direction.

149

Although the meaning of each parameter has been introduced, the relation between these parameters and the statistical properties is still unclear especially for the core distribution probabilities of inter-aggregate pores and solid particles. As stated in [38], the core distribution probability of inter-aggregate pores, C_{dM} , indicates the number density of inter-aggregate pores n_{dM} , from which C_{dM} can be defined as follows in consideration of the total number of grids, *N*:

$$155 \qquad C_{dM} = n_{dM} \frac{V}{N} \tag{4}$$

156 where *V/N* corresponds to the resolution of the grid-system.

157

To generate an isotropic structure in a grid system, the main directional probabilities (D_1-D_4) and the diagonal directional growth probabilities (D_5-D_8) are set to be constant: $D_i = 0.0001$ for i = 1-4; and $D_i = 0.00025$ for i = 5-8, which is similar to most applications of QSGS method [33]. The QSGS approach for generating inter-aggregate pore network contains 3 sub-steps as follows (Fig. 1): (*i*) Gas (in inter-aggregate pores) is chosen as the growing phase. The cores of gas phase are

163 (*i*) Gas (in inter-aggregate pores) is chosen as the growing phase. The cores of gas phase are 164 randomly located in a grid system based on the value of $C_{\rm dM}$, which is the core distribution 165 probability of the inter-aggregate pores. Each cell in the grid system is assigned with a random number following a uniform distribution function within (0, 1). Each cell whose random number is smaller than C_{dM} is chosen as a core of gas. Note that a small value of C_{dM} will increase the random fluctuation so that the value of C_{dM} should not be too small. While *V/N* representing grid resolution should be fine enough to guarantee the precision of inter-aggregate pores, as a consequence, C_{dM} should be then small enough. In this study, C_{dM} is set as 0.001, a trade-off between random fluctuation and precise description of inter-aggregate pores.

172 (*ii*) All the elements of gas are enlarged to their neighboring cells in all directions based on each 173 given directional growth probability D_i . Again, new random numbers are assigned to its 174 neighboring cells for each gas element. The neighboring cell in direction *i* becomes a new element 175 of gas if its random number is not greater than D_i .

- 176 (*iii*) The growing process (*ii*) is repeated until the volume fraction of gas reaches the porosity of
- 177 inter-aggregate pores. Thus, the inter-aggregate pore network is constructed (Stage 2 in Fig. 1).
- 178 The domain occupied by the inter-aggregate pores is defined as $\Omega_{\rm M}$, while the rest of the domain
- 179 corresponds to the porous matrix representing aggregates defined as Ω_A .

180 **2.3. Step 3 - Stochastic generation of intra-aggregate pore network**

To obtain a dual-porosity network when inter-aggregate pore-system has been modeled, the intra-aggregate pores are introduced into the porous matrix for aggregates (Ω_A). Similar to the generation procedure of inter-aggregate pores, the core distribution probability of solid particles, C_{ds} , should be determined first. Noted the close relation between C_{ds} and n_{ds} , the core distribution probability of solid particles (C_{ds}) can be defined as below:

186
$$C_{ds} = n_{ds} \frac{V}{N(1-P_M)}$$
 (5)

188 The QSGS approach adopted for generating the intra-aggregate pore network also includes 3189 sub-steps (Fig. 1) as follows.

190 (i) Solid particle is chosen as the growing phase. The cores of solid phase are randomly located in 191 the designed porous matrix region (Ω_A) above based on the value of Cd_S. Each cell in Ω_A is assigned a random number following a uniform distribution function within (0, 1). Each cell 192 193 whose random number is not greater than Cd_{S} is chosen as a core of solid particle. While, in 194 clayey soils, the average size of solid particles is much smaller than that of inter-aggregate pores, 195 so the number density of particles is greater than that of inter-aggregate pores in a unit volume, 196 which results in the core distribution probability of solid particles is always much higher and set as 197 0.1 or 0.2 in the present study.

198 (*ii*) Every element of solid is enlarged to its neighboring cells in all directions. For each solid 199 element, new random numbers are assigned to its neighboring cells. The neighboring cell in 200 direction *i* will become a new element of solid phase if its random number is smaller than D_i .

201 (*iii*) The growing process (*ii*) is repeated until the volume fraction of solid particles reaches the 202 value extracted at Step 1 (Stage 3 in Fig. 1). The domain occupied by the intra-aggregate pores is

203 defined as $\Omega_{\rm m}$, while the rest of the domain corresponds to the solid particles.

204 **2.4 Step 4 - Distribution of water in the pore network**

The water phase grows following the phase interaction growth probability I_i^{ws} and I_i^{ww} ; I_i^{ws} represents the growth probability of the water phase on the solid phase along direction *i*, and I_i^{ww} represents the growth probability of the water phase on the water phase along direction *i*. In this

study, clayey soils are investigated. It is well known that clay particles have a strong water 208 209 adsorption capacity and water would exist in the form of liquid-film on the clay particle surface in 210 spite of intra-aggregate water and inter-aggregate water. Besides, it is very difficult to distinguish 211 the different morphologies of water-film for these two kinds of water, and there has not been a 212 clear data for this issue. Therefore, these two types of water-film are set to be similar to simplify analysis. Then to model such a water-film, I_i^{ws} has been set ten times larger than I_i^{ww} as used by 213 214 Wang et al. [38]. Furthermore, the water growth phase is first started in the domain of 215 intra-aggregate pore $\Omega_{\rm m}$, when the volume of water is higher than the volume of intra-aggregate 216 pore, the inter-aggregate pores start to be filled with water (stage 4 in Fig. 1).

217 **2.5. Step 5 - Determination of the effective thermal conductivity**

Figure 3 shows an example of the three-phase medium generated following the above steps. To determine the effective thermal conductivity of this medium, thermal boundary conditions are imposed as shown in Fig. 3. Constant temperatures are imposed on the left and right sides while adiabatic conditions are imposed on the top and bottom sides.

222

In 1-D heat conduction condition, heat flow between two cell *i* and *j* is calculated as follows:

224
$$q_{ij} = \lambda_{ij} \frac{T_i - T_j}{L_{ij}}$$
(6)

where q_{ij} and L_{ij} are the heat flux density and the distance between the two cells *i* and *j*, and the temperatures in the center of cells *i* and *j* are T_i and T_j , respectively. λ_{ij} denotes the effective thermal conductivity between two neighbor cells. Each cell contains only one phase and λ_{ij} is calculated by the harmonic mean method [39]. 230 When the steady state is reached, the heat flux density through each cell in the computational 231 region keeps balanced, which can be described as below.

$$232 \qquad \sum_{i} q_{ij} = 0 \tag{7}$$

233 Based on the analyses above, the discrete equations about the temperature can be obtained by 234 integrating the governing Eq. (7) over all the cells in the computational region. Consequently, 235 when the number of cells in which the temperature is unknown is X, and there will be an equal number of linear equations to solve the temperature field. As long as the temperature field is 236 237 determined, the effective thermal conductivity can be calculated by the following formula: L× (adx 3)

$$238 \qquad \lambda = \frac{L \times J \, q \, dx}{T_h - T_c} \tag{8}$$

239 where q is the steady heat flux density through each cell along the y direction and L is the distance 240 width of the grid (see Fig. 3).

241 In the present work, a square grid is used with the same number of cells on the x and the y direction. A preliminary work has been done to optimize the grid dimension. In Fig. 4, the thermal 242 243 conductivity of the medium is plotted versus the grid dimension. The results show that the 244 effective thermal conductivity of the medium becomes independent of the grid dimension when 245 the latter is higher than 200 cells. Hence, in the present study, a grid system of 200×200 cells is used for all the simulations. As shown in Fig. 3, this system allows to represent several large pores 246 247 with diameters of approximately 50 cells.

248 **3. Results**

249 **3.1 Validation**

To validate the approach proposed in this study for calculating the effective thermal conductivity of structural clayey soils with dual-porosity system, the numerical results are compared with experimental data [3, 24] from literatures in this section.

253 In the work of Tang et al. [3], MX80 bentonite, containing 92% of montmorillonite, from 254 Wyoming (being considered as a potential reference buffer material for high-level radioactive 255 waste disposal in several countries) was compacted at various water contents (w = 9% for series 256 S1; 11.7% for S2; and 17.9% for S3). Each series includes several specimens compacted at various 257 dry densities. Besides, some compacted specimens of series S2 were dried to obtain a water 258 content of 9.1% (series S2b), and the series S3b corresponds to specimens of series S3 dried to a 259 water content of 10.2%. Tang et al. [3]expected that compacted specimens prepared with direct 260 compaction and with drying after compaction would have different moisture distribution in the 261 pore space. The thermal conductivity of compacted soil specimens was measured by a commercial 262 thermal properties analyser, KD2 (Decagon Devices Inc.) based on the hot wire method.

263

The porosity of intra-aggregate pores is determined as follows for each water content. The soil suction at each water content is estimated from the water retention curve [40], then e_m is determined from the relation between e_m and suction [23]. Noted that e_m increases as water content increases due to the expansion of aggregates and e_M decreases as dry density increases, and the values of void ratio corresponding to these intra-aggregate pores (e_m) are shown in Table 1. The thermal conductivity of water and gas are taken as $\lambda_w = 0.5974 \text{ W/m} \cdot \text{K}$, $\lambda_g = 0.0243 \text{ W/m} \cdot \text{K}$, and the thermal conductivity of solid phase λ_s (which depends on the soil mineralogy) is equal to 2.0825 W/m·K following the study of Tang et al. [3].

272

Figure 5 shows the experimental results of the compacted samples and those obtained by the model. In Fig. 6, the predicted thermal conductivities are plotted versus the measured values for all the samples. The results show that the model can predict the accurate thermal conductivity values of samples subjected to drying path while it overestimates those of samples obtained by direct compaction.

278

279 Different preparation methods may result in different water distribution states. For the samples 280 obtained by compaction, they would contain water both within and between aggregates[41]. However, for samples prepared by drying, both intra-aggregate water content and inter-aggregate 281 water content are unknown, more water would be preferentially stored in intra-aggregate pores. 282 283 Hence, the present model (where water was preferentially distributed in intra-aggregate pores) can 284 predict the accurate thermal conductivity values of samples obtained by drying due to the 285 reasonable model of water distribution. In order to have a deeper analysis on the effect of water, a complementary model (Model 2) is employed where water is distributed preferentially in 286 287 inter-aggregate pores.

288

To evaluate this assumption, the experimental results of all samples obtained by compaction are compared against their corresponding predictions by the two models in Fig. 7. In this figure, the results obtained by the two models are plotted in the form of error bars. The upper bound corresponds to the water distributed preferentially in intra-aggregate pores (Model 1) and the lower bound corresponds to the water distributed preferentially in inter-aggregate pores (Model 2). It can be seen from Fig. 7 that the experimental results of series S1 mainly correspond to the lower bound of the model, while those of the series S2 fall in the range between the lower and the upper bounds. However, only the result of one sample in the series S3 (with lowest dry density) agrees with the model, and those of the two others are over-predicted.

298

In the study of Usowicz et al. [24], a haplic phaeozem at Werbkowice was sieved into six series and each one has different aggregate sizes. The soil aggregates in each series were loosely packed into the cylinders of 100 cm³ volume, 5 cm diameter in five replicates. Some characteristics of the soil were given in Table 2 [42, 43], and the method for measuring thermal conductivity was also taken from Sikoro [43].

305 The influence of volumetric water content on the thermal conductivity in structural clayey soil was 306 also investigated at various aggregate sizes. The pore size distribution of soil samples was not 307 available. The porosity of intra-aggregate pores was then determined following the suggestion of 308 Real et al.[44]. They measured the thermal conductivity of structural lightweight aggregate 309 concrete at various water contents. The results show an inflection point in the relation between 310 thermal conductivity and water content. That point corresponds to the transition from 311 inter-aggregate water to intra-aggregate water at a drying path. Thus, the water content at the 312 inflection point can be used to estimate the porosity of intra-aggregate pores. In the work of

$b_1 b_1 = b_1 b_1 b_1 b_1 b_1 b_1 b_1 b_1 b_1 b_1$	313	Usowicz et al.	[24]	, all curves	presented	an infl	ection	point at	a volumetric	water	content	of 20	0%
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In the present work, the porosity of intra-aggregate pores was then estimated to be 0.20.

315

Figure 8 presents the experimental data and the predicted results of the samples with different aggregate sizes. Figure 9 shows the thermal conductivity predicted by the model versus the experimental data. In Table 3, the summary statistics of measured and predicted thermal conductivities are compared between the present study and the study of Usowicz et al. [24].

320

Figure 8 shows that the model can predict the accurate thermal conductivity values for most of the experimental data except that with aggregate size smaller than 0.25 mm. In fact, the latter corresponds to non-aggregated soil sample, which means it does not have a dual-porosity system. Table 3 shows that the model in the present study can improve the prediction as compared to the one proposed by Usowicz et al. [24]; its coefficient of determination R^2 is higher than that of Usowicz et al. [24] for all the series of soil samples, except that with aggregate size smaller than 0.25 mm.

328 **3.2. Pore-scale heat flow analysis**

A series of typical heat flow density fields are required to give a deep insight into how heat transfers within and between aggregates in structural clayey soils with dual-porosity system. Three typical water distribution model in the dual-porosity space and their corresponding heat flow density fields at different water contents are chosen for comparison to give a visual presentation about the heat flow path and its relation with water distribution. In Fig. 10, the pure structural model of the dual-porosity system without any water ($e_w=0$) is presented in the top, below which its corresponding heat flow density field is shown. The second water content corresponds to the content with saturated intra-aggregate pores ($e_w=e_m$), the structural model of water distribution is shown as the upper half in Fig. 11 and the corresponding heat flow density field as the lower half. As to the third water content, it is set to be twice of the water content of the second one ($e_w=2e_m$). Simultaneously, their water distribution and heat flow density field are shown in Fig. 12 with a similar layout in Figs. 10 and 11.

341

342 From Figs. 10, 11 and 12, we can see that heat flow mainly goes through connected aggregated 343 generally. In addition, it is preferred to the wet region in the dual-porosity space. It is thus clear 344 that heat conduction is closely dependent on the water distribution between intra-aggregate pores 345 and inter-aggregate pores. With the increase of water content, water is mostly retained within aggregates. Heat flow path mainly falls within the region of aggregates and none flow path pass 346 through the areas of inter-aggregate pores. As the water content continues to increase, 347 348 intra-aggregate pores are saturated and water appears in inter-aggregate pores in form of 349 liquid-film along the aggregates region. In this case, heat flow path is getting wider and wider, and 350 the added region for the path just corresponds to the space occupied by the inter-aggregate water 351 in this stage. It can be clearly observed that there is a difference in widening heat flow paths 352 between intra-aggregate water and inter-aggregate water. Intra-aggregate water mainly widens heat flow between fine particles within aggregates, while inter-aggregate water mainly acts on 353 354 broaden heat flow path in the inter-aggregate pores. Except for a correct prediction of effective 355 thermal conductivity, this model can also directly show how heat transfers in soils at pore scale.

The latter can be seen as another promising advantage of the model, especially for the differences in promoting heat conduction between intra-aggregate water and inter-aggregate water from a perspective of heat flow paths.

359

360 **4 Discussions**

361 Microstructural-based quantitative computation of the thermal conductivity in structural clayey 362 soils is always challenging due to the presence of dual-porosity system. As a promising tool to 363 relate structural properties to thermal conductivity in porous media, numerical modelling has been 364 employed in this field. But less effort was made to model heat transfer process in complex dual-porosity media [45] like compacted clayey soils. Dong et al. [46] presented a critical review 365 on the models for predicting soil thermal conductivity and classified the models into three types 366 367 including mixing models, empirical models and mathematical models. For examples, the most 368 popular Johansen model [13] belongs to the empirical models. In most of these models, the effect 369 of water distribution on thermal conductivity is ignored. In the present work, as the water 370 distribution is considered, simulations show clearly that heat transfer is controlled by thermal 371 contacts between aggregates and inside the aggregates. These domains are strongly influenced by 372 the presence of inter-aggregate water and intra-aggregate water.

373

It should be noted that the model could predict the accurate thermal conductivity values when the dual-porosity system of the soil pore network is dominant. In the case of soil compacted at high densities (or compacted on the wet side of OMC), the volume of inter-aggregate pore is negligible.

- 377 In these cases, the accuracy of the predictive model would be adversely affected and it tends to 378 overestimate the values of soil thermal conductivity (see Fig. 7). This problem would be improved 379 by generating a more realistic pore network [47] but it would be more time consuming.
- 380

381 It is thus clear that the proposed model in this paper is still far away from a mature predictive 382 model, and it would be a long way to go as a new predictive one compared with other experienced models. In addition to the accuracy problem, some other limitations are also noteworthy. Soil 383 384 structure is three-dimensional, heat conduction process in real soils is much more complex while 385 the predictive model in our work is a 2-D model and would be somewhat inadequate to provide a 386 more detailed description. Furthermore, as a new predictive model, it still needs to be validated by 387 more experimental data with both thermal conductivity values and pore size distribution curves 388 available. Finally, yet importantly, the determination of the Representative Element Volume (REV) and its mesh need more considerations. The size of the REV should be large enough to avoid 389 390 random fluctuation, at the same time the mesh size should be small enough to guarantee a precise 391 description of the fine pores. The cost for modeling would be extremely high if the above demands 392 are both satisfied, under this circumstance, an in-depth trade-off must be carried out to make 393 minor sacrifices to safeguard the major interests. In the present study, the grid dimension strategy is just a simple case and more work is needed to give more insights into this issue. In addition, it 394 395 should be noted that the present model only describes heat transfer by conduction process in 396 unsaturated soils, and other phenomenon such as latent heat transfer is ignored. It has been 397 experimentally shown [48] that heat transfer is dominant by conduction for unsaturated soils in a 398 low-temperature range (2° C to 30° C), while latent heat transfer turns out to be noticeable when the temperature is high enough (greater than 40°C) in soils. Hence, the present model is then
mostly suitable over a low-temperature range.

401

402 The effect of water distribution on soil properties is usually related to hysteresis effect. For 403 compacted clayey soils as a typical case, Tang et al. [3] found that the thermal conductivity of 404 specimens obtained by drying was higher than that of specimens prepared by direct compaction 405 with the same dry density and water content. This phenomenon was also noted by Farouki [11]. In 406 compacted soils with dual-porosity system, water distribution depends largely on 407 hydro-mechanical history. It is well known that at a given water content the matric suction on a drying path (or a unloading path) is always higher than that on a wetting path (a loading path). 408 409 Indeed, matric suction indicates water distribution state; higher suction means that more water 410 tends to be retained in intra-aggregate pores with small pore size. For this reason, there is more 411 water distributed within aggregates for specimens obtained by drying than that for the specimens 412 obtained by compaction in the study of Tang et al.[3]. This effect of water distribution on soil 413 thermal conductivity is demonstrated by the simulations obtained by the present model. In 414 addition, it should be noted that when the soil pore network is dominated by a monomodal 415 porosity, the hysteresis effect on thermal conductivity would be negligible. Nguyen et al. [49] 416 investigated thermal conductivity of natural loess during wetting-drying paths, whose pore size 417 distribution shows only one pore family, and they found a unique relationship between thermal 418 conductivity and degrees of saturation.

420 **5. Conclusions**

422	In	the present work, the thermal conductivity of structural clayey soils with dual-porosity system
423	is p	predicted based on its microstructure and water distribution. The following conclusions can be
424	dra	wn:
425		
426	1)	A microstructural-based model is proposed to calculate thermal conductivity of structural
427		clayey soils with dual-porosity system. The model was validated with the data obtained from
428		two types of soils. The results show that the model can give appropriate predictions when the
429		dual porosity system is dominant in the soil pore network.
430	2)	Water distribution has a significant effect on soil thermal conductivity. Thermal conductivity
431		is always higher when water is preferentially distributed within aggregates than between
432		aggregates.
433	3)	The model can give a deep insight into heat flow paths at pore scale. Numerical simulations
434		demonstrate that heat conduction mainly goes through aggregate region and is preferred to
435		wet pores of the dual-porosity space.
436		

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564		





567 Fig. 1. Workflow to generate dual-porosity network and water distribution: (1) extraction of $e_{\rm m}$ and

 $e_{\rm M}$; (2) generation of inter-aggregate pores; (3) generation of intra-aggregate pores, (4) water

569	distribution within	aggregates and	between aggregates.
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Fig. 2. Growth directions of each cell to its neighbor cells.

Adiabatic







Fig. 4. Thermal conductivity versus grid dimension.



580 Fig. 5. Thermal conductivity of samples obtained by compaction (a) and obtained by drying (b) for

samples from Tang et al. [3].

581





584 Fig. 6. Predicted thermal conductivity versus measured ones for samples from Tang et al. [3].



586

588

587 Fig. 7. Thermal conductivity versus dry density for samples from Tang et al. [3]: experimental data

and the two models.





Fig. 9. Modelled results by mode 1 versus experimental data in Usowicz et al. [24].





606 Fig. 10. Multi-phase distribution at the first water content ($e_w = 0$) in the upper half and its

corresponding heat flux density field in the lower half.

608



saturated aggregate region





611 Fig. 11. Multi-phase distribution at the second water content $(e_w=e_m)$ in the upper half and its

corresponding heat flux density field in the lower half.



616 Fig. 12. Multi-phase distribution at the third water content ($e_w=2e_m$) in the upper half and its

617

corresponding heat flux density field in the lower half.

Table 1 Detailed $e_{\rm m}$ and $e_{\rm w}$ information at each water content in [3].

w (%)	9.0(S1)	9.1(S2b)	10.2(S3b)	11.7(82)	17.9(S3)
e_m	0.43	0.43	0.46	0.50	0.58
e_w	0.25	0.25	0.28	0.32	0.49

Table 2 Characteristics of the Haplic Phaeozem at Werbkowice.

Aggregate	Particle size (mm) distribution (%,w/w)			Organic matter contents (%)	Bulk density(Mg cm ⁻³)	Porosity(m ⁻³ m ⁻³)
size (mm)	1.0-0.10	0.1-0.02	<0.02			
All	3	57	40	2.18	1.09	0.59
<0.25	3	61	36	3.38	1.18	0.55
0.25-0.5	4	52	44	4.61	0.98	0.64
0.5-1	4	53	43	4.37	0.89	0.66
1-3	3	55	42	4.55	0.94	0.65
3-5	5	52	43	4.37	0.83	0.69
5-10	3	53	44	4.13	0.84	0.68

629	Table 3 Comparison of statistics between this study (left) and [24](right).													
	Aggregate size (mm)	5-10		3-5		1-3		0.5-1		0.25-0.5		<0.25		
	Linear regression coefficient	0.823	1.458	0.783	1.394	0.794	1.560	0.741	1.520	0.834	1.561	0.580	1.088	
	Intercept	0.053	-0.158	0.053	-0.145	0.082	-0.198	0.117	-0.209	0.093	-0.232	0.208	-0.043	
	Coefficient of determination R ²	0.976	0.859	0.937	0.810	0.950	0.938	0.964	0.932	0.978	0.925	0.911	0.978	