

A two-surface thermomechanical plasticity model considering thermal cyclic behavior

Wei Cheng, Ren-Peng Chen, Peng-Yun Hong, Yu-Jun Cui, Jean-Michel Pereira

▶ To cite this version:

Wei Cheng, Ren-Peng Chen, Peng-Yun Hong, Yu-Jun Cui, Jean-Michel Pereira. A two-surface thermomechanical plasticity model considering thermal cyclic behavior. Acta Geotechnica, 2020, $10.1007/\mathrm{s}11440$ -020-00999-5 . hal-02874658

HAL Id: hal-02874658 https://enpc.hal.science/hal-02874658v1

Submitted on 19 Jun 2020

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

2	thermal cyclic behavior
3	Wei Cheng ¹ , Ren-peng Chen ² , Peng-yun Hong ³ , Yu-jun Cui ⁴ , Jean-Michel Pereira ⁵
4	
5	¹ Ph.D candidate, Department of Civil Engineering, Zhejiang University, Hangzhou
6	310058, China, wcheng@zju.edu.cn
7	² Professor, Department of Civil Engineering, Zhejiang University, Hangzhou 310058,
8	China; College of Civil Engineering, Hunan University, Changsha 410082, China;
9	chenrp@zju.edu.cn, chenrp@hnu.edu.cn
10	³ Former Ph.D student, Université Paris-Est, Laboratoire Navier (UMR 8205), CNRS,
11	ENPC, IFSTTAR, F-77455 Marne-la-Vallée, France
12	⁴ Professor, Université Paris-Est, Laboratoire Navier (UMR 8205), CNRS, ENPC,
13	IFSTTAR, F-77455 Marne-la-Vallée, France
14	⁵ Professor, Université Paris-Est, Laboratoire Navier (UMR 8205), CNRS, ENPC,
15	IFSTTAR, F-77455 Marne-la-Vallée, France
16	
17	
18	
19	
20	
21	

A two-surface thermo-mechanical plasticity model considering

Abstract

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

In thermal-related engineering such as thermal energy structures and nuclear waste disposal, it is essential to well understand volume change and excess pore water pressure buildup of soils under thermal cycles. However, most existing thermomechanical models can merely simulate one heating-cooling cycle and fail in capturing accumulation phenomenon due to multiple thermal cycles. In this study, a two surface elasto-plastic model considering thermal cyclic behavior is proposed. This model is based on the bounding surface plasticity and progressive plasticity by introducing two yield surfaces and two loading yield limits. A dependency law is proposed by linking two loading yield limits with a thermal accumulation parameter n_c , allowing the thermal cyclic behavior to be taken into account. Parameter n_c controls the evolution rate of the inner loading yield limit approaching the loading yield limit following a thermal loading path. By extending the thermo-hydro-mechanical equations into the elastic-plastic state, the excess pore water pressure buildup of soil due to thermal cycles is also accounted. Then, thermal cycle tests on four fine-grained soils (natural Boom clay, Geneva clay, Bonny silt and reconstituted Pontida clay) under different OCRs and stresses are simulated and compared. The results show that the proposed model can well describe both strain accumulation phenomenon and excess pore water pressure buildup of finegrained soils under the effect of thermal cycles. **Keywords**: fine-grained soils; strain accumulation; thermal cycles; two-surface model; excess pore water pressure buildup

1. Introduction

43

44

45

46

47

48

49

50

51

52

53

54

55

56

57

58

59

60

61

62

63

Around energy piles [1-3], nuclear waste canisters [4], buried tunnels and pipes [5], the soils suffer from temperature effects, especially heating-cooling cycles. Observations of different fine-grained soils in the laboratory and in the field [6-11] showed that heating generally induced non-negligible volume change and excess pore water pressure buildup. Several thermo-mechanical models were proposed to describe this thermo-mechanical behavior of fine-grained soils [13-21]. Some of them extended the Cam-clay or modified Cam-clay model to the temperature effect by introducing a shrinking yield surface [13-17]. These models could describe some basic thermomechanical behavior, but fail to describe the soil behavior in over-consolidated states. In order to well describe the small thermo-mechanical elastic zone and the shear softening behavior, some advanced models consider two yield surfaces based on the bounding surface theory [18-21]. Hong et al. [22] made a comparison among some of these advanced models, and showed that the multiple plastic hardening mechanism were of paramount importance in modeling complex thermal loading behavior. Though numerous efforts were made in thermal mechanical modeling, most existing models can only simulate the case of one thermal cycle and fail in describing the soil behavior under multiple heating-cooling cycles. As more attention has been paid to the long-term performance [11,12,25,26,27,40], the volume change and excess pore water pressure accumulation due to temperature variation can act as a significant factor influencing the safety of energy structures. Demars and Charles [23] reported a series

of drained thermal cycle tests on high plastic marine clays and found that permanent reduction in void ratio (a function of over-consolidation ratio) gradually reduced due to temperature cycles (see Fig. 1). Plum et al. [24] conducted an undrained heating-cooling cycle tests on Newfield clay. After four thermal cycles, the accumulation of excess pore water pressure was still increasing. Pastén et al. [40] experimentally observed the thermally driven displacement accumulation with the number of temperature cycles and developed a thermally induced ratcheting mechanism for a smooth interface. All those observations show that multiple thermal cycles should be considered in thermal mechanical modeling of clays. Zhou et al. [28] recently proposed a bounding surface model with a memory surface to consider the thermal cyclic behavior. However, this imposed memory surface actually has no effect on the accumulation behavior of normally consolidated soil because this memory surface coincides with the bounding surface in this circumstance. Ma et al. [29] proposed a thermal stabilization line in hypoplastic modeling approach. Though three thermal parameters are introduced, the proposed hypoplastic model fails to describe the strain accumulation during relatively small temperature changes because it always simulates an unrealistic elastic behavior before entering the elasto-plastic zone following a thermal loading path. More recently, Zymnis et al. [41] proposed a simple calibration procedure for Tsinghua ThermoSoil (TTS) model and studied the capabilities of simulating the long-term accumulation of strains due to thermal cycles. However, those existing models for thermal cyclic behavior merely considered the strain accumulation behavior under drained conditions

64

65

66

67

68

69

70

71

72

73

74

75

76

77

78

79

80

81

82

83

though the excess pore water pressure buildup due to temperature effects are at least of equal importance from the best of the authors' knowledge.

In the present work, a two surface thermo-plastic model, namely ACC2-T, is proposed to consider the thermal cyclic behavior based on the previous TEAM model by Hong et al. [21]. The proposed model unifies the loading yield limits and the thermal yield limits. To connect the inner loading yield limit and the loading yield limit, a flexible dependency law is incorporated and combined with isotropic and progressive hardening laws to account for multiple thermal cycles. In the dependency law, a parameter n_c is introduced to control accumulation rate through the evolution rate of the inner loading yield limit approaching the loading yield limit. Meanwhile, the proposed model is extended to undrained condition by applying the thermo-hydro-mechanical equations by Coussy [30] into the elastic-plastic state. Then, the rationale of ACC2-T model is discussed in terms of elasto-plasticity and thermodynamic theories. Lastly, the thermal cycle test results of four fine-grained soils (natural Boom clay, Geneva clay, Bonny silt and reconstituted Pontida clay) under different OCRs and stresses are used to verify the proposed model.

101

102

103

104

105

100

85

86

87

88

89

90

91

92

93

94

95

96

97

98

99

2. Model description

In this section, the proposed model (ACC2-T) is presented using typical constitutive variables, namely mean effective stress p', deviator stress q, temperature T and the corresponding increments (dp', dq, dT). The soil behavior is assumed to be isotropic

and the constitutive model is developed and formulated in the conventional triaxial conditions.

108

109

2.1 Thermo-elastic behavior

- In ACC2-T model, the soil deformation can be divided into thermo-elastic and thermo-
- 111 plastic parts.
- In the thermo-elastic part, the elastic law adopted in many other models [31,36,37]
- in isothermal conditions are extended into non-isothermal conditions for its simplicity.
- the total elastic volumetric strain increment associated with mechanical and thermal
- loading and the elastic shear strain assumed purely mechanical are calculated as follows:

116
$$d\varepsilon_{v}^{e} = \frac{\kappa dp'}{\upsilon p'} - \alpha_{1} dT, \ d\varepsilon_{s}^{e} = \frac{dq}{3G}, \ G = \frac{3(1-2v)}{2(1+v)} \frac{\upsilon p'}{\kappa}$$
 (1)

- 117 where $d\varepsilon_{v}^{e}$, $d\varepsilon_{s}^{e}$ is the elastic volumetric strain increment $(d\varepsilon_{v}^{e} = d\varepsilon_{1}^{e} + d\varepsilon_{2}^{e} + d\varepsilon_{3}^{e})$
- and the elastic shear strain increment $(d\varepsilon_s^e = \frac{2}{3}(d\varepsilon_1^e d\varepsilon_3^e))$. κ is the elastic slope in $(v, \frac{1}{3})$
- ln p') plane and v is the specific volume. α_1 is the thermal elastic compressibility index
- which assumed a positive constant because heating induces soil expansion. G is shear
- modulus and v is the Poisson's ratio.

122

123

2.2 Thermo-plastic behavior

- 124 The thermo-plastic mechanism of ACC2-T model consists of two yield surfaces and
- plastic potential surface, the dependency law, the isotropic and progressive hardening

laws and the flow rules.

127

135

136

137

138

140

141

- 128 *2.2.1 Yield surfaces and plastic potential surfaces*
- In ACC2-T model, two yield surfaces, namely loading surface (f_I) and yield surface (f_I),
- with a generalized formulation [31] are implemented to model the yielding of both stiff
- and soft clays.

132 Loading Surface:
$$f_I = q^2 + \frac{M_f^2}{1 - k_f} \left(\frac{p'}{r \overline{p}'_{cT}} \right)^{\frac{2}{k_f}} \left(r \overline{p}'_{cT} \right)^2 - \frac{M_f^2 p'^2}{1 - k_f} = 0$$
 (2)

133 Yield Surface:
$$f_Y = q^2 + \frac{M_f^2}{1 - k_f} \left(\frac{p'}{\overline{p}'_{cT}}\right)^{\frac{2}{k_f}} \overline{p}'_{cT}^2 - \frac{M_f^2 p'^2}{1 - k_f} = 0$$
 (3)

where M_f is the stress ratio at the apex of two surfaces, k_f is a parameter specifying the

shape of yield surfaces, \overline{p}'_{cT} is the pre-consolidation pressure at current temperature T

and r is the inverse of over-consolidation ratio (OCR) at current temperature T. The

conceptual plot of two yield surfaces at various temperature is given in Fig. 2(a). To

consider the thermo-mechanical behavior, the two surfaces are extended into three-

dimensional plot (p', q, T) with two loading yield limits. The two loading yield limits,

namely the inner loading yield limit (ILY) and the loading yield limit (LY) are linked by

the proposed dependency law which is discussed in Yield limits and dependency law

section.

The plastic potential surface g_I takes the same form as for loading surface, but with

144 different parameters M_g and k_g :

145
$$g_I = q^2 + \frac{M_g^2}{1 - k_g} \left(\frac{p'}{r\beta}\right)^{\frac{2}{k_g}} (r\beta)^2 - \frac{M_g^2 p'^2}{1 - k_g} = 0$$
 (4)

and it leads to a dilatancy equation in the case of triaxial compression:

147
$$\frac{d\varepsilon_{v}^{p}}{d\varepsilon_{s}^{p}} = \frac{\frac{\partial g_{I}}{\partial p'}}{\frac{\partial g_{I}}{\partial q}} = \frac{M_{g}^{2} - \eta^{2}}{k_{g}\eta}$$
 (5)

where $d\varepsilon_v^p$ is the plastic volumetric strain increment, $d\varepsilon_s^p$ is the plastic shear strain increment, η denotes the stress ratio q/p', M_g defines the critical stress ratio at failure where no further volumetric strain increment develops, k_g is a constant parameter which controls the ratio of plastic volumetric strain increment and plastic shear strain increment and β is the size parameter. Typically, an unassociated flow rule is adopted for modeling complex mechanical behaviors. However, when $M_g = M_f$ and $k_g = k_f$, an associated flow rule would be recovered. When $k_g = k_f = 2$, elliptical surfaces like modified Cam-clay model are recovered.

156

155

148

149

150

151

152

153

- 157 2.2.2 Hardening laws
- In ACC2-T model, two plastic hardening mechanisms fixed to reference temperature
- T_0 are adopted to control the evolution of yield surface and loading surface.
- In the isotropic hardening rule, as same as in Modified Cam-clay model, the
- evolution of pre-consolidation pressure \overline{p}'_{c0} at reference temperature T_0 is linked to the
- plastic volumetric strain increment:

163
$$d\overline{p}'_{c0} = \frac{\upsilon}{\lambda - \kappa} \overline{p}'_{c0} d\varepsilon_{\nu}^{p} \tag{6}$$

where λ is the normal consolidation slope in (v, ln p') plane and $d\bar{p}'_{c0}$ is the increment of pre-consolidation pressure. It means the evolution of yield surface is dominated by the plastic volumetric strain.

The progressive hardening variable dr_0 , at reference temperature T_0 , is defined with a combined volumetric and shear plastic strain as follows:

where r_0 is the inverse of over-consolidation ratio (OCR) at current temperature T_0 and dr_0 is the increment. s is a material constant which controls the hardening rate of loading surface in approaching yield surface. A_d is a material constant which controls the contribution of shear plastic strain.

In this progressive hardening rule, parameter r_0 is always less than or equal to 1 (0 <

In this progressive hardening rule, parameter r_0 is always less than or equal to 1 (0 < $r_0 \le 1$). When the loading surface is completely inside the yield surface (0 < $r_0 < 1$), it means the soil is over-consolidated. Within the hardening process, plastic strain increases and the loading surface begins to move towards the yield surface ($dr_0 > 0$). When $r_0 = 1$, the loading surface and the yield surface coincide. The soil turns into normally consolidated state as the same case of MCC model. Note that the loading surface could not run out of the yield surface ($r_0 > 1$) for the fact that if $r_0 > 1$, $dr_0 < 0$ holds. With such a combined volumetric-deviatoric hardening law, the inclusion of shear hardening part ($d\varepsilon_s^p > 0$) would lead to a positive plastic modulus (h > 0) even when the effective stress state ($d\varepsilon_v^p = 0$) reach the critical state line (CSL). As a consequence, the stress point lying on the loading surface can cross the CSL,

hardening continues to a stress point $(d\varepsilon_v^p < 0, d\varepsilon_s^p > 0, h = 0)$ and then the stress point $(d\varepsilon_v^p < 0, d\varepsilon_s^p > 0, h < 0)$ would move back to the CSL. This approach allows to predict shear softening behavior and it is often the case of highly over-consolidated states of soil.

With these isotropic and progressive hardening rules, the plastic modulus and increment stress-strain relationship of ACC2-T model are obtained in Appendix A.

Under loading and heating processes, two hardening variables \overline{p}'_{c0} and r_0 are activated with the evolution of plastic strain. However, under unloading and cooling processes, pure elastic strain develops with a fixed value of \overline{p}'_{c0} . Due to ACC2-T model strictly adhering to the principle that the stress point is always lying on the loading surface, the value of r_0 could be re-calculated by a simple Newton-Raphson Method with unconditional stability.

2.2.3 Yield limits and dependency law

In the two surface models, the loading surface and the yield surface are geometrically similar in (p', q) plane with a corresponding radial mapping rule. In previous TEAM model [21], two yield limit mechanisms, namely thermal yield limits (ITY, TY) and loading yield limits (ILY, LY) are adopted to model the thermal behavior. These yield limit mechanisms in TEAM model (see Fig.3(a)) enable the thermal elastic response in reloading path to occur before entering the elasto-plastic zone. Therefore, the TEAM model could not simulate the strain accumulation phenomenon due to temperature

- variations. In order to overcome this shortcoming and extend the model to the case of
- 207 multiple thermal cycles, the loading yield limits (ILY, LY) are unified to consider both
- 208 the thermal yield and loading yield mechanisms. Meanwhile, a new dependency law is
- proposed to connect *ILY* and *LY*.
- In the dependency law, the pre-consolidation pressure \overline{p}'_{cT} at current temperature T
- takes the original form and it would decrease with the increase of temperature:

212
$$\bar{p}'_{cT} = \bar{p}'_{c0} \exp[-\alpha_0 (T - T_0)]$$
 (8)

- where \overline{p}'_{c0} is pre-consolidation pressure at reference temperature T_0 ; α_0 is a material
- 214 constant controlling the thermal plastic behavior.
- The other part of the dependency law r is defined as below:

216
$$r = \frac{1}{OCR} = \frac{p'}{\bar{p}'} = \frac{q}{\bar{q}} = \frac{p'_{cT}}{\bar{p}'_{cT}}$$
 (9)

- where (p', q), (\bar{p}', \bar{q}) is the corresponding stress point in loading surface and yield
- surface at current temperature *T*, respectively.
- Unlike TEAM model with the assumption that $r = r_0$, ACC2-T model takes the form
- 220 that would make *ILY* not necessarily homologous to *LY* any longer (see Fig. 3(b)):

221
$$r = r_0 \exp \left[-\alpha_0 (r_0^{n_c} - 1)(T - T_0) \right]$$
 (10)

- where n_c is a thermal parameter which controls the strain accumulation rate under
- 223 multiple thermal cycles.
- The combined dependency law made up by \bar{p}'_{cT} and r then is expressed by:

225
$$r\bar{p}'_{cT} = r_0\bar{p}'_{c0} \exp\left[-\alpha_0 r_0^{n_c} (T - T_0)\right]$$
 (11)

In the proposed law, the shape of *ILY* is governed by the key thermal accumulation

parameter n_c . Parameter n_c controls the evolution rate of ILY approaching LY by the two isotropic and progressive hardening rules. In order to illustrate the plastic mechanism under the thermal path, two cases in the isotropic states, namely $n_c < 0$ and $n_c = 0$, are compared in Fig.4. Both two cases are at initial stress state A, then heated up to stress state B and finally cooled down to stress state A. Under the heating path from A to B, the ILY without n_c ($n_c = 0$) would induce a increment of Δr_1 . For the case of $n_c < 0$, it would induce a increment of $\Delta r_1 + \Delta r_2 + \Delta r_3$ if the shape of *ILY* is fixed. However, with the effect of n_c , the original ILY (see Fig.4(b), dotted line I) would gradually turn into solid line II with a actual increment of $\Delta r_1 + \Delta r_2$. The larger increment $\Delta r_1 + \Delta r_2$ in hardening variable dr_0 would mean larger plastic volumetric strain increments than the case of $n_c = 0$. Under the cooling path from B to A, the mechanical response is purely elastic and the shape of ILY would turn from II into I. For the case of $n_c > 0$, the increment in hardening variable dr_0 would induce smaller strain increments than $n_c = 0$. Under multiple thermal cycles, the value of r_0 would be smaller and smaller. Under such a unique dependency law, the evolution rate of ILY is actually the evolution rate of strain accumulation. With a proper selection of parameter n_c in the dependency law, ACC2-T model allows the strain accumulation under the effect of multiple thermal cycles to be modelled. Some important features about the dependency law and parameter n_c are summarized below: 1. When the current temperature T is equal to the reference temperature T_0 , r becomes equal to r_0 . It means that n_c would have no effect on the stress-strain relationship at

227

228

229

230

231

232

233

234

235

236

237

238

239

240

241

242

243

244

245

246

- reference temperature T_0 .
- 249 2. When soil turns into the normal consolidated state $(r_0 = 1)$, r is also equal to 1. In that
- case, ILY would coincide with LY. It means that n_c would have no effect on the behavior
- of normal consolidated soils under either isothermal or non-isothermal condition.
- 3. When n_c is equal to zero (bold line in Fig. 3(b)), r becomes equal to r_0 . In that case,
- a similarity between *ILY* and *LY* would be recovered. This is just the case of *ILY* and *LY*
- used in TEAM model [21].
- 4. Theoretically, the value of n_c can be chosen from negative infinity to positive infinity.
- When n_c tends to positive infinity, *ILY* would tend to be the dotted line in Fig. 3(b).
- When n_c tends to negative infinity, *ILY* would tend to approach the temperature axis T
- in Fig. 3(b). A larger n_c represents a quicker strain accumulation rate which would
- induce smaller total volumetric strain accumulation under the effect of thermal cycles.
- 260 5. Any possible r is smaller than 1. During the heating process, the hardening
- mechanism enables r_0 to approach 1. Thus, r would also have its limit value of 1 which
- implies that the over-consolidation ratio of soil is always larger than or equal to 1.

263

264

3. Loading path independence

- 265 After the description of the proposed model extended to thermal cyclic behavior, it is
- essential to discuss the rationale of ACC2-T model in terms of elasto-plastic theory and
- thermodynamic theory as Hong et al. [22] did on three existing thermo-mechanical
- models [19,20,25,28,29]. The verification of loading path independence is made up by

both the thermo-elastic and thermo-plastic part. The schematic plot is given in Fig.5. Heating is treated as a special isotropic loading. Therefore, merely isotropic condition (q=0) is considered during the derivation. The thermo-elastic part is discussed as below and the derivation in thermo-plastic regime is attached in Appendix B. In the thermo-elastic mechanism (Eq.3) of ACC2-T model, the bulk modulus $K = \frac{\upsilon p'}{\iota}$ is independent of temperature, and thermal elastic compressibility index α_1 is also independent of mean effective stress. Such elastic volumetric strain in ACC2-T model is surely loading path independent in (p', T) plane. Note that the thermo-elastic mechanism leads to loading path dependent in (p', q) plane since the Maxwell symmetry relations are not satisfied. A possible way is to extend a hyperelastic law [39] into non-isothermal conditions. For simplicity of parameter calibration, merely this thermo-

4. Analysis and determination of model parameters

elastic mechanism is considered here.

The proposed ACC2-T model contain fifteen parameters $(\lambda, \kappa, \overline{p}'_{c0}, v, M_f, k_f, M_g, k_g, s, r_0, A_d, \alpha_0, \alpha_1, T_0, n_c)$. Five of them $(\lambda, \kappa, \overline{p}'_{c0}, v, M_g)$ are commonly defined in MCC model. (M_f, k_f) , (M_g, k_g) control the shapes of yield surfaces and plastic potential surfaces, respectively. Three parameters (s, r_0, A_d) are used to consider a progressive yielding of two surfaces. Four parameters $(\alpha_0, \alpha_1, T_0, n_c)$ are defined to consider the thermal influence on the soil behavior. The procedure for determining these parameters is described and key parameters $(\lambda, \kappa, \overline{p}'_{c0}, s, r_0, \alpha_0, \alpha_1, T_0, n_c)$ related to thermal

- accumulation behavior are discussed on the set of model parameters for natural Boom
- 291 clay in Fig. 6.
- 1. By an isotropic compression test or oedometer test under reference temperature T_0 ,
- 293 κ , λ , the initial $r_{0,0}$ and $\overline{p}'_{c_{0,0}}$ are determined in $(v, \ln p')$ plane in Fig.6(1). Note that
- 294 parameter s controls the hardening rate of loading surface in approaching yield surface.
- 295 It can be determined by fitting nonlinearity from over-consolidated states to normal
- consolidated state in $(v, \ln p')$ plane.
- 297 2. By an isotropic heating-cooling test at normally consolidated states, α_1 is
- determined by fitting data of cooling stage and α_0 is determined by the heating test in
- 299 $(T, \Delta \varepsilon_v)$ plane in Fig.6(2).
- 3. By a continuous thermal cycle test, the volumetric strain increment by each thermal
- 301 cycle $\Delta \varepsilon_{\nu,st}$ can be obtained ($\Delta \varepsilon_{\nu,st}$, n) plane in Fig.6(3). The thermal accumulation
- n_c parameter n_c , which controls the strain accumulation rate, is then determined by
- 303 calibrating the strain accumulation under each thermal cycle.
- 304 4. M_f , k_f . M_f denotes the apex of yield surface and k_f controls the shape of yield surface.
- 305 They are calibrated by fitting the converntional yield points of various stress paths.
- 306 5. M_g is the critical state stress ratio and it is calibrated by the effective stress ratio at
- 307 critical state.
- 308 6. k_g controls plastic flow direction. It is determined by fitting the values of $d\varepsilon_v^p/d\varepsilon_s^p$
- in drained triaxial shear tests.
- 7. The poisson's ratio v is determined by a triaxial tests at low strain level in the $(\varepsilon_v \varepsilon_l)$

311 plane: $v = (\varepsilon_v - \varepsilon_I)/2$.

 $8. A_d$ represents the contribution of the plastic shear strain in the hardening process. It is calibrated by fitting the results of triaxial compression tests at over-consolidated

states in (q, ε_l) or $(\varepsilon_v, \varepsilon_l)$ plane in Fig.6(4).

315

316

318

5. Model Validation and prediction

In this section, four different fine-grained soils, namely natural Boom clay, Geneva clay,

Bonny silt and reconstituted Pontida clay, are adopted to verify the capability of ACC2-

319 T model in modeling the thermal cyclic behavior.

320

321

325

326

327

328

329

330

331

5.1 Natural Boom clay

One heating and cooling test on natural Boom clay ($I_p = 31$) under isotropic stress states performed by Baldi et al. [8] and two groups of triaxial compression tests conducted by Lê [38] are taken into account.

In the heating and cooling test, specimen TBoom-9 taken from Mol at an in-situ depth of 223 m (initial pre-consolidated pressure of 6 MPa) is tested under a mixed mechanical and thermal loading process: the sample was firstly saturated under a constant mean effective stress of 2 MPa at 21.5 °C, loaded up to 4 MPa, unloaded to 1 MPa, heated up to 95 °C and cooled back to 21.5 °C, loaded up to 3 MPa at 21.5 °C and heated up to 95 °C and cooled back, loaded up to 6 MPa and heated up again and finally cooled back. In the loading process, three thermal cycles of temperature

increment of 73.5 °C at different isotropic stress states, namely mean effective stress of 1 MPa, 3 MPa and 6 MPa, are selected for simulation. For better comparison between the computed and measured results, the increments of volumetric strain are reset at the starting point of each heating-cooling cycle. Moreover, Fig. 7 contains an isotropic compression test of natural Boom clay from 2 MPa to 20 MPa, then back to 6 MPa. Basic parameters for natural Boom clay are listed in Tab.1. The TEAM model [21] and the proposed ACC2-T model are both used for simulation in Fig.8. It appears that both models can describe the thermal volume change well for normally consolidated or slightly over-consolidated state (p' = 6 MPa) adopting the same thermal elastic parameter α_1 and thermal plastic parameter α_0 . However, for highly over-consolidated states (p' = 3 MPa, p' = 1 MPa), it is observed that ACC2-T model gives a more consistent simulation than TEAM model. One reason is that TEAM model always shows a linear elastic expansion behavior before entering the elastoplastic zone and has no parameters controlling strain evolution. With this shortcoming, TEAM model would fail to respond to thermal cycles and thus to describe strain accumulation behavior, though complicated multiple plastic mechanisms are adopted. However, in ACC2-T model, the stress point is always lying on the loading surface. Combined with the isotropic and progressive hardening rules, the thermal accumulation parameter n_c in the dependency law allows the ACC2-T model to better describe the nonlinear expansion behavior and strain accumulation under over-consolidated states. Meanwhile, as natural Boom clay is relatively easy to contract under heating, the use

332

333

334

335

336

337

338

339

340

341

342

343

344

345

346

347

348

349

350

351

of a negative value of parameter n_c could facilitate the simulation of such aspect.

In the triaxial compression test, the experimental results of drained triaxial compression tests ($p'_0 = 2.5 \text{ MPa}$, $p'_0 = 4 \text{ MPa}$) at room temperature 25 °C and drained triaxial compression tests ($p'_0 = 2.5 \text{ MPa}$, $p'_0 = 3.8 \text{ MPa}$) at high temperature 76 °C [38] are considered in (q, ε_l) plane and (ε_l , ε_l) plane in Fig.9. In these moderate overconsolidated states, the shear strength at room temperature is a bit higher than high temperature. However, a larger volumetric strain is generated at high temperature than room temperature as shown in (ε_l , ε_l) plane. At the same time, the smooth predictions by ACC2-T model agree well with the experimental observations. Two values of n_c (n_c = -1, n_c = 0) are selected to simulate the behaivor at high temperature 76 °C. It indicates that the value of n_c has a negligible effect on the prediction of triaxial tests.

A numerical case at high over-consolidated state (p'_0 = 0.5 MPa) under both two

A numerical case at high over-consolidated state ($p'_0 = 0.5$ MPa) under both two temperatures (25 °C, 76 °C) are conducted. A slight shear dilatancy is predicted at axial strain of about 5%. However, the post-peak softening phenomenon in (q- ε_1) plane is not very apparent because parameter A_d ($A_d = 0.1$) for natural Boom clay is very small to simulate behaviors at both high, slightly over-consolidated and normal consolidated states.

5.2 Geneva clay

Multiple thermal cycles were applied on Geneva clays ($I_p = 11.1$) in a temperaturecontrolled oedometer cell under drained condition [25]. A normally consolidated soil sample with a vertical effective stress of 125 kPa was tested with four temperature cycles from 5 °C from 60 °C, starting at a room temperature of 20 °C. The one-dimension test results are simulated in Fig.7 and the calibrated model parameters are listed in Tab.1.

374

375

376

377

378

379

380

381

382

383

384

385

386

387

388

389

390

391

392

393

394

Fig.10 shows the measured and computed soil behavior under multiple heating and cooling cycles. The computed result of ACC2-T model (Fig.10(a)) shows a good agreement with the measured one. The irreversible volumetric strain accumulates with increasing thermal cycles, but at a decreasing rate (Fig. 10(c)). The value of 3.5 is shown appropriate for the thermal accumulation parameter n_c to control the strain accumulation rate. For the case of TEAM model, the computed result of first thermal cycle is the same as ACC2-T model. However, the response of TEAM model is purely elastic thereafter and the thermal strain accumulation could not be described. In Fig.10(b), a sensitivity analysis of ACC2-T model is conducted to study the effect of parameter n_c on the strain accumulation. Two other n_c values of 0, 10 are selected for this purpose. In the first thermal cycle, ACC2-T model gives the same results for all the three n_c values because the thermal volumetric strain of normally consolidated soil is only dependent on thermal elastic parameter α_1 and thermal plastic parameter α_0 . From the second thermal cycle, the soil becomes over-consolidated. The thermal accumulation parameter n_c starts to control the strain evolution rate. From Fig. 10(c), it appears that parameter n_c is positively correlated to the strain accumulation rate and a proper selection of parameter n_c is crucial for total strain accumulation.

5.3 Bonny silt

395

396

397

398

399

400

401

402

403

404

405

406

407

408

409

410

411

simulation.

Multiple heating and cooling cycles were applied on compacted Bonny silt $(I_p = 4)$ under different OCRs in a temperature-controlled oedometer cell [27]. Bonny silts were first mechanically consolidated to a vertical effective stress of approximately 1200 kPa at a constant room temperature of 18 °C. Then, they were unloaded to reach five different OCR values of 1.00, 1.28, 1.80, 7.36 and 30.29. Fig. 7 presents the experimental and calibration results of one-dimensional test of Bonny silt. Four heating and cooling cycles were applied under drained condition with different OCRs in a temperature ranging from 18 °C to 93 °C. It can be seen from Fig. 11 that at slightly over-consolidated states (i.e. OCR = 1, 1.28 and 1.8), the measured and computed results show a good consistency. That means the thermal accumulation parameter n_c can properly control the strain evolution rate under various over-consolidated states. However, for highly over-consolidated ones (i.e. OCR = 7.36, 30.29) in the literature [27], the volumetric strain accumulation is guite small or even becomes negative, suggesting that the expansion and the contraction of the oedometer cell can be no longer ignored. These two samples are not considered in the

412

413

414

415

416

5.4 Reconstituted Pontida clay

The excess pore water pressure accumulation due to thermal cycles in validated by a heating and cooling test of reconstituted Pontinda clay. Hueckel et al [12] reported this measured and computed results on reconstituted Pontida clay. The reconstituted silty

- 417 clay sample was firstly loaded to a mean effective stress state of 2.5 MPa. Then it
- 418 underwent a heating-cooling cycle from 22°C to 65°C and back to 22°C, then a
- 419 continuous heating to 95°C in a constant total isotropic stress state.
- 420 Although some previous models [19] consider the undrained behavior by imposing
- a constant volume condition which is imprecise under non-isothermal conditions, the
- 422 undrained computation using ACC2-T model is obtained by extending the energy and
- mass conservation of thermo-poro-elastic media into elasto-plastic states [30].
- In a saturated porous media, the current water mass (m_w) per unit volume can be
- 425 expressed as:

$$426 m_{\scriptscriptstyle W} = \rho_{\scriptscriptstyle W} \phi (12)$$

- where ρ_w is water density and ϕ is the Lagrangian porosity.
- In undrained conditions, water mass is constant and $dm_w = 0$ holds, then

$$429 \qquad \frac{dm_{w}}{\rho_{w}} = d\phi + \phi \frac{d\rho_{w}}{\rho_{w}} = d\phi + \phi \left(C_{w} du - \alpha_{w} dT \right) = 0 \tag{13}$$

- 430 where α_w , C_w , is the water thermal expansion coefficient, water compressibility,
- 431 respectively.
- In isotropic stress state and under non-isothermal condition, total mean stress change
- (dp) and Lagrangian porosity change ($d\phi$) can be expressed with Maxwell's symmetry
- 434 condition:

$$dp = \frac{1}{C_d} d\varepsilon_v + (I - \frac{C_s}{C_d}) du_w + \frac{\alpha_d}{C_d} dT$$
(14)

$$436 d\phi = -(I - \frac{C_s}{C_d})d\varepsilon_v - (\phi - I + \frac{C_s}{C_d})C_s du_w + (\phi - I + \frac{C_s}{C_d})\alpha_s dT (15)$$

- where C_s , C_d , α_s , α_d is the volumetric compressibility coefficient of solid grain, the
- volumetric compressibility of soil skeleton, the thermal expansion coefficient of solid
- grain and the thermal expansion coefficient of soil skeleton. It is often the case that α_s
- $440 = \alpha_d$.
- Thus, the expressions for excess pore water pressure can be obtained, as follows:

$$d\varepsilon_{v} = -(\phi\alpha_{w} + (1 - \phi)\alpha_{s})dT + \phi(C_{w} - C_{s})du_{w} + C_{s}dp$$
(16)

- With infinitesimal transformation and clayey soils, the fact $(C_s \approx 0, n \approx \phi)$ is
- 444 commonly accepted. Thus

$$445 du_w = \frac{d\varepsilon_v + (n\alpha_w + (1-n)\alpha_s)dT}{nC_w} (17)$$

where *n* is Eulerian porosity.

450

451

452

453

454

455

- For reconstituted Pontida clay, α_s is 1×10^{-5} (1/°C) chosen as same as α_I , which is
- calibrated from an undrained cooling process from 65°C to 22°C. α_w and C_w are
- calibrated from a heating test of free water in the literature [35].
 - The computed results of excess pore water pressure by ACC2-T model and TEAM model are compared to the measured data and Hueckel's simulation [12] in Fig.12. It is seen that both predictions of ACC2-T model and TEAM model are more accurate than Hueckel's simulation, especially the existed buildup of pore water pressure in experimental results. During the heating stage from 22°C to 65°C, the mean effective stress will decrease with temperature (equivalent to a mechanical loading under undrained condition) and the effective stress-temperature path (T p') initially enters
- plasticity. With the plastic hardening of *ILY*, excess pore water pressure is increased.
- Then during the cooling stage from 65°C to 22°C, the response is purely elastic with a
- decrease of the pore water pressure. Thereby, an irreversible excess pore water pressure
- is observed after one heating-cooling cycle which is well captured by ACC2-T model
- and TEAM model. Moreover, though the cooling stage is purely elastic, the *ILY* would
- shrink to make the stress-temperature state always lying on it. However, during the re-
- heating process, TEAM model could not build up excess pore water pressure from 22°C
- 65 to 65 C because the response is purely elastic. As for ACC2-T model, the clay sample
- is initially over-consolidated, then began to build up excess pore water pressure with
- the control of thermal accumulation parameter n_c in the whole process from 22°C to
- 467 95 °C.

5.5 Discussion

Four fine-grained soils are selected to verify the capability of ACC2-T model on modelling thermal cyclic behaviors under drained and undrained conditions. A thermal accumulation parameter n_c control the accumulation rate under multiple thermal cycles. Meanwhile, the values of n_c are ranked as: natural Boom clay< reconstituted Pontida clay<Geneva clay<Bonny silt. It means the clays, containing more clay contents, showing larger plastic index I_p , are more likely to accumulate volumatric strain and build up excess pore water pressure. Generally, the larger is the plastic index I_p , the smaller is the value of n_c . A liner regression function is obtained to evaluate the correlation between parameter n_c and plastic index I_p in Fig. 13.

6. Concluding remarks

A two-surface plasticity model (ACC2-T) is proposed to describe the thermomechanical behavior of fine-grained soils under multiple thermal cycles. Compared with TEAM model, two thermal yield limits are removed and the loading yield limits unify the thermal and loading yielding part. A dependency law with thermal accumulation parameter n_c is used to link the inner loading yield limit and the loading yield limit. Parameter n_c controls the evolution rate of the inner loading yield limit approaching the loading yield limit under thermal loading path. With such a unique dependency law and multiple plastic hardening rules, the model could well control the thermal strain accumulation rate under drained conditions and pore water pressure

489	buildup rate under undrained conditions. Tests on four fine-grained soils are considered
490	to verify the proposed model. Comparison between prediction and experiment shows
491	that ACC2-T model can well capture the thermo-mechanical behavior of soils under
492	multiple thermal cycles.
493	
494	
495	Acknowledgements
496	The present work is carried out with the support of National Natural Science Foundation
497	of China (51608188, 758201011). The authors also wish to acknowledge the support of
498	the European Commission by the Marie Skłodowska-Curie Actions HERCULES-
499	Towards Geohazards Resilient Infrastructure Under Changing Climates (H2020-
500	MSCA-RISE-2017, 778360)
501	
502	
503	
504	
505	
506	
507	
508	
509	

510 Notation

- $\alpha_0 =$ parameter controlling thermal plastic behavior;
- $\alpha_1 = \beta_{12}$ $\alpha_1 = \beta_{12}$ parameter controlling thermal elastic behavior;
- 513 β = the size parameter of potential plastic surface;
- λ , κ = slope of isotropic loading, reloading line respectively;
- v, v =current void ratio, Poisson's ratio respectively;
- A_d = parameter controlling the contribution of shear plastic strain;
- $d\varepsilon$, $d\sigma$, dT = total strain, stress, temperature increment respectively;
- $d\mathbf{\varepsilon}_{\sigma}^{e}$, $d\mathbf{\varepsilon}_{T}^{e}$ = stress, thermal induced elastic strain increment respectively;
- 519 $d\varepsilon_{v}$, $d\varepsilon_{v}^{e}$, $d\varepsilon_{s}^{e}$ = total volumetric, elastic volumetric, shear strain increment
- 520 respectively;
- 521 $d\varepsilon^p$, $d\varepsilon^p$, $d\varepsilon^p$ = plastic, plastic volumetric, plastic shear strain increment
- 522 respectively;
- 523 Λ = plastic multiplier;
- f_{I} , f_{Y} = Loading surface, yield surface respectively;
- G, K, h = elastic shear, elastic bulk, plastic modulus respectively;
- 526 k_f , k_g = parameter controlling the shape of yield surface, plastic potential surface
- 527 respectively;
- 528 M_f = stress ratio at the apex of yield surface;
- 529 M_g , M_{g0} = critical stress ratio at current, reference temperature respectively;
- 530 p', \overline{p}' = current, mapping mean effective stress respectively;

- p'_{cT} , p'_{c0} = pre-consolidation pressure in loading surface at current, reference
- 532 temperature respectively;
- \overline{p}'_{cT} , \overline{p}'_{c0} = pre-consolidation pressure at current, reference temperature respectively;
- q, \bar{q} = current, mapping deviator stress respectively;
- r, r_0 = reverse of OCR at current, reference temperature respectively;
- s =parameter controlling the rate of evolution of the slope of the stress--strain
- 537 relation;
- T, T_0 = current, reference temperature respectively;
- \mathbf{D}_{e} , \mathbf{D}_{ep} , \mathbf{D}_{et} = elastic, elasto-plastic, temperature stiffness matrix respectively;
- $\mathbf{m} = \text{unit vector.}$

556 Appendix A

The consistency condition of loading surface in ACC2-T model is adopted herein:

558
$$\left(\frac{\partial f_I}{\partial \mathbf{\sigma}'}\right)^t : d\mathbf{\sigma}' + \frac{\partial f_I}{\partial T}dT + \frac{\partial f_I}{\partial \overline{p}'_{c0}}d\overline{p}'_{c0} + \frac{\partial f_I}{\partial r_0}dr_0 = 0$$
 (A - 1)

- The plastic multiplier Λ and the plastic modulus h are obtained in non-isothermal
- 560 condition:

561
$$d\mathbf{\varepsilon}^p = \Lambda \frac{\partial g_I}{\partial \mathbf{\sigma}'}$$
 (A - 2)

562
$$\Lambda = -\frac{\left(\frac{\partial f_I}{\partial \mathbf{\sigma}'}\right)^t : d\mathbf{\sigma}' + \frac{\partial f_I}{\partial T} dT}{\frac{\partial f_I}{\partial \overline{p}'_{c0}} \frac{\upsilon}{\lambda - k} \overline{p}'_{c0} \frac{\partial g_I}{\partial p'} + \frac{\partial f_I}{\partial r_0} \frac{\upsilon}{\lambda - k} s(1 - r_0) (\frac{\partial g_I}{\partial p'} + A_d \frac{\partial g_I}{\partial q})}$$
 (A - 3)

563
$$h = \frac{\upsilon}{\lambda - k} \left(\frac{\partial f_I}{\partial \overline{p}'_{c0}} \overline{p}'_{c0} \frac{\partial g_I}{\partial p'} + \frac{\partial f_I}{\partial r_0} s(1 - r_0) \left(\frac{\partial g_I}{\partial p'} + A_d \frac{\partial g_I}{\partial q} \right) \right)$$
(A - 4)

- The total strain increment is made up of mechanical elastic strain increment, thermal
- elastic strain increment and plastic strain increment.

$$\delta 66 \qquad d\mathbf{\varepsilon} = d\mathbf{\varepsilon}_{\sigma'}^e + d\mathbf{\varepsilon}_T^e + d\mathbf{\varepsilon}^p \tag{A-5}$$

The thermal elastic strain increment $d\mathbf{\varepsilon}_T^e$ is defined as:

$$568 d\mathbf{\varepsilon}_T^e = -\frac{1}{3}\mathbf{m}\alpha_1 dT (A-6)$$

- where **m** is the column vector with 1 at normal stress entries and 0 at shear stress entries.
- By substituting Eq. A-6 into Eq. A-5, the general incremental stress-strain relation
- can be expressed:

572
$$d\mathbf{\sigma}' = \mathbf{D}_e d\mathbf{\epsilon}_{\sigma'}^e = \mathbf{D}_e (d\mathbf{\epsilon} + \frac{1}{3} \mathbf{m} \alpha_1 dT - d\mathbf{\epsilon}^p)$$
 (A - 7)

573 where \mathbf{D}_e is the mechanical elastic matrix.

- By substituting the plastic multiplier into Eq. A-7, the differential stress-strain
- equations can be obtained:

576
$$d\mathbf{\sigma}' = \mathbf{D}_{ep}d\mathbf{\varepsilon} + \mathbf{D}_{et}dT \tag{A-8}$$

- where \mathbf{D}_{ep} , \mathbf{D}_{et} are the mechanical elasto-plastic matrix and the thermal elasto-plastic
- 578 matrix, respectively.

579
$$\mathbf{D}_{ep} = \mathbf{D}_{e} - \frac{\mathbf{D}_{e} \frac{\partial g_{I}}{\partial \mathbf{\sigma}'} \left(\frac{\partial f_{I}}{\partial \mathbf{\sigma}'} \right)^{t} \mathbf{D}_{e}}{\left(\frac{\partial f_{I}}{\partial \mathbf{\sigma}'} \right)^{t} \mathbf{D}_{e} \frac{\partial g_{I}}{\partial \mathbf{\sigma}'} + h}$$
(A - 9)

580
$$\mathbf{D}_{et} = \frac{\mathbf{D}_{e} \frac{\partial g_{I}}{\partial \mathbf{\sigma}'} \left[-\frac{1}{3} \left(\frac{\partial f_{I}}{\partial \mathbf{\sigma}'} \right)^{t} \mathbf{D}_{e} \mathbf{m} \alpha_{1} - \frac{\partial f_{I}}{\partial T} \right]}{\left(\frac{\partial f_{I}}{\partial \mathbf{\sigma}'} \right)^{t} \mathbf{D}_{e} \frac{\partial g_{I}}{\partial \mathbf{\sigma}'} + h} + \frac{1}{3} \mathbf{D}_{e} \mathbf{m} \alpha_{1}$$
(A - 10)

596 Appendix B

- Assume the soil is loaded and heated from Point A to Point B under two different
- loading paths I($A \rightarrow C \rightarrow B$) and II($A \rightarrow D \rightarrow B$) in Fig.5. The soil is at the initial stress
- state $(p'_0, r_0, p'_{c0}, T_1)$ which automatically satisfies the yield condition:

600
$$f_{I_0} = p'_0 - r_0 p'_{c_0} \exp \left[-\alpha_0 r_0^{n_c} \left(T_1 - T_0 \right) \right] = 0$$
 (B - 1)

- Under loading path I, the soil element is isotropically loaded to stress point C
- 602 $(p'_0 + \Delta p'_1, r_1, p'_{c1}, T_1)$ at constant temperature T_1 .

603
$$f_{I1} = p_0' + \Delta p_1' - r_1 p_{c1}' \exp \left[-\alpha_0 r_1^{n_c} \left(T_1 - T_0 \right) \right] = 0$$
 (B - 2)

$$604 p'_{cl} = p'_{c0} \exp \left[\frac{\upsilon}{\lambda - \kappa} \Delta \varepsilon_{vl}^{p} \right] (B - 3)$$

605
$$r_1 = 1 + (r_0 - 1) \exp \left[-\frac{\upsilon}{\lambda - \kappa} s \Delta \varepsilon_{\nu 1}^{p} \right]$$
 (B - 4)

- Then the soil element is heated up to stress point B ($p'_0 + \Delta p'_1, r_2, p'_{c2}, T_1 + \Delta T_1$) at
- constant mean effective stress $p'_0 + \Delta p'_1$.

608
$$f_{12} = p_0' + \Delta p_1' - r_2 p_{c2}' \exp \left[-\alpha_0 r_2^{n_c} \left(T_1 + \Delta T_1 - T_0 \right) \right] = 0$$
 (B - 5)

609
$$p'_{c2} = p'_{c1} \exp\left[\frac{\upsilon}{\lambda - \kappa} \Delta \varepsilon_{\nu 2}^{p}\right] = p'_{c0} \exp\left[\frac{\upsilon}{\lambda - \kappa} \left(\Delta \varepsilon_{\nu 1}^{p} + \Delta \varepsilon_{\nu 2}^{p}\right)\right]$$
 (B - 6)

610
$$r_2 = 1 + (r_1 - 1) \exp \left[-\frac{\upsilon}{\lambda - \kappa} s \Delta \varepsilon_{\nu 2}^p \right] = 1 + (r_0 - 1) \exp \left[-\frac{\upsilon}{\lambda - \kappa} s \left(\Delta \varepsilon_{\nu 1}^p + \Delta \varepsilon_{\nu 2}^p \right) \right]$$
 (B - 7)

- Under loading path II, the soil element is firstly heated up to stress point D
- 612 $(p'_0, r_3, p'_{c3}, T_1 + \Delta T_1)$ at constant mean effective stress p'_0 .

613
$$f_{I3} = p'_0 - r_3 p'_{c3} \exp\left[-\alpha_0 r_3^{n_c} \left(T_1 + \Delta T_1 - T_0\right)\right] = 0$$
 (B - 8)

614
$$p'_{c3} = p'_{c0} \exp\left[\frac{\upsilon}{\lambda - \kappa} \Delta \varepsilon_{\nu 3}^{p}\right]$$
 (B - 9)

615
$$r_3 = 1 + (r_0 - 1) \exp\left[-\frac{\upsilon}{\lambda - \kappa} s\Delta \varepsilon_{\nu 3}^p\right]$$
 (B - 10)

Then, the soil element is isotropically loaded to stress point $B(p'_0 + \Delta p'_1, r_4, p'_{c4}, T_1 + \Delta T_1)$

at constant temperature $T_1 + \Delta T_1$.

618
$$f_{I4} = p_0' + \Delta p_1' - r_4 p_{c4}' \exp \left[-\alpha_0 r_4^{n_c} \left(T_1 + \Delta T_1 - T_0 \right) \right] = 0$$
 (B - 11)

619
$$p'_{c4} = p'_{c3} \exp\left[\frac{\upsilon}{\lambda - \kappa} \Delta \varepsilon_{v4}^{p}\right] = p'_{c0} \exp\left[\frac{\upsilon}{\lambda - \kappa} \left(\Delta \varepsilon_{v3}^{p} + \Delta \varepsilon_{v4}^{p}\right)\right]$$
 (B - 12)

620
$$r_4 = 1 + (r_3 - 1) \exp\left[-\frac{\upsilon}{\lambda - \kappa} s\Delta\varepsilon_{\nu 4}^{p}\right] = 1 + (r_0 - 1) \exp\left[-\frac{\upsilon}{\lambda - \kappa} s\left(\Delta\varepsilon_{\nu 3}^{p} + \Delta\varepsilon_{\nu 4}^{p}\right)\right]$$
 (B - 13)

- 621 Compare Eqs.B-5, B-6, B-7 and Eqs.B-11, B-12, B-13, it appears clearly that the two
- different loading paths would reach the same final stress state, namely:

623
$$p'_{c2} = p'_{c4}$$
 (B - 14)

624
$$r_2 = r_4$$
 (B - 15)

625
$$\Delta \varepsilon_{v1}^p + \Delta \varepsilon_{v2}^p = \Delta \varepsilon_{v3}^p + \Delta \varepsilon_{v4}^p$$
 (B - 16)

- No matter Path I or Path II is followed, the plastic volumetric strain will be equal, which
- means that plastic volumetric strain in ACC2-T model is also loading path independent.

643 **References**

- [1] Bourne-Webb PJ, Amatya B, Soga K, Amis T, Davidson C, Payne P. Energy pile
- test at Lambeth College, London: geotechnical and thermodynamic aspects of pile
- response to heat cycles. Géotechnique 2009;59:237-48.
- [2] Amatya BL, Soga K, Bourne-Webb PJ, Amis T, Laloui L. Thermo-mechanical
- behaviour of energy piles. Geotechnique 2012;62:503-19.
- [3] Mimouni T, Laloui L. Behaviour of a group of energy piles. Canadian Geotechnical
- 650 Journal 2015;52:1913-29.
- [4] Gens A, Sanchez M, Guimaraes LD, Alonso EE, Lloret A, Olivella S, et al. A full-
- scale in situ heating test for high-level nuclear waste disposal: observations, analysis
- and interpretation. Geotechnique 2009;59:377-99.
- [5] Liu XC, Xiao YM, Inthavong K, Tu JY. A fast and simple numerical model for a
- deeply buried underground tunnel in heating and cooling applications. Applied Thermal
- 656 Engineering 2014;62:545-52.
- [6] Campanella R G, Mitchell J K. Influence of temperature variations on soil behavior.
- Journal of Soil Mechanics & Foundations Div, 1968.
- [7] Eriksson L G. Temperature effects on consolidation properties of sulphide clays.
- International Conference on Soil Mechanics and Foundation Engineering: 13/08/1989-
- 18/08/1989. Balkema Publishers, AA/Taylor & Francis The Netherlands, 1989: 2087-
- 662 2090.
- [8] Baldi G, Hueckel T, Peano A, Pellegrini R. Developments in modelling of
- thermohydro-geomechanical behaviour of Boom clay and clay-based buffer materials
- (volume 2). Commission of the European Communities, 1991.
- [9] Delage P, Sultan N, Cui Y J. On the thermal consolidation of Boom clay. Canadian
- 667 Geotechnical Journal, 2000, 37(2): 343-354.
- [10] Yavari N, Tang AM, Pereira JM, Hassen G. Mechanical behaviour of a small-scale
- energy pile in saturated clay. Géotechnique 2016;66:878-87.
- 670 [11] Ng CWW, Shi C, Gunawan A, Laloui L. Centrifuge modelling of energy piles

- subjected to heating and cooling cycles in clay. Géotechnique Letters 2014;4:310-6.
- [12] Hueckel T, Pellegrini R. Thermoplastic modeling of undrained failure of saturated
- clay due to heating. Soils and Foundations, 1991, 31(3): 1-16.
- 674 [13] Hueckel T, Baldi G. Thermoplasticity Of Saturated Clays Experimental
- 675 Constitutive Study. J Geotech Eng-Asce 1990;116:1778-96.
- 676 [14] Hueckel T, Borsetto M. Thermoplasticity Of Saturated Soils And Shales:
- 677 Constitutive equations. J Geotech Eng-Asce 1990;116:1765-77.
- 678 [15] Robinet JC, Rahbaoui A, Plas F, Lebon P. A constitutive thermomechanical model
- 679 for saturated clays. Engineering Geology 1996;41:145-69.
- 680 [16] Cui Y J, Sultan N, Delage P. A thermomechanical model for saturated clays.
- 681 Canadian Geotechnical Journal, 2000, 37(3): 607-620.
- 682 [17] Graham J, Tanaka N, Crilly T, Alfaro M. Modified Cam-Clay modelling of
- temperature effects in clays. Canadian Geotechnical Journal 2001;38:608-21.
- [18] Abuel-Naga HM, Bergado DT, Bouazza A, Ramana GV. Volume change behaviour
- of saturated clays under drained heating conditions: experimental results and
- constitutive modeling. Canadian Geotechnical Journal 2007;44:942-56.
- [19] Yao YP, Zhou AN. Non-isothermal unified hardening model: a thermo-elasto-
- plastic model for clays. Géotechnique 2013;63:1328-45.
- 689 [20] Laloui L, François B. ACMEG-T: soil thermoplasticity model. Journal of
- 690 engineering mechanics, 2009, 135(9): 932-944.
- [21] Hong PY, Pereira JM, Cui YJ, Tang AM. A two-surface thermomechanical model
- 692 for saturated clays. International Journal for Numerical and Analytical Methods in
- 693 Geomechanics 2016;40:1059-80.
- 694 [22] Hong PY, Pereira JM, Tang AM, Cui YJ. On some advanced thermo-mechanical
- 695 models for saturated clays. International Journal for Numerical and Analytical Methods
- 696 in Geomechanics 2013;37:2952-71.
- [23] Demars K R, Charles R D. Soil volume changes induced by temperature cycling.
- 698 Canadian Geotechnical Journal, 2011, 19(2):188-194.

- 699 [24] Plum R L, Esrig M I. Some temperature effects on soil compressibility and pore
- water pressure. Special Report-Highway Research Board, 1969 (103): 231.
- 701 [25] Di Donna A, Laloui L. Response of soil subjected to thermal cyclic loading:
- Experimental and constitutive study. Engineering Geology 2015;190:65-76.
- 703 [26] Ng CWW, Shi C, Gunawan A, Laloui L, Liu HL. Centrifuge modelling of heating
- effects on energy pile performance in saturated sand. Canadian Geotechnical Journal
- 705 2015;52:1045-57.
- 706 [27] Vega A, McCartney JS. Cyclic heating effects on thermal volume change of silt.
- Environmental Geotechnics 2015, 2: 257-68.
- 708 [28] Zhou C, Fong KY, Ng CWW. A new bounding surface model for thermal cyclic
- 709 behaviour. International Journal for Numerical and Analytical Methods in
- 710 Geomechanics 2017;41:1656-66.
- 711 [29] Ma QJ, Ng CWW, Masin D, Zhou C. An approach for modelling volume change
- of fine-grained soil subjected to thermal cycles. Canadian Geotechnical Journal
- 713 2017;54:896-901.
- 714 [30] Coussy, O. (2004). Poromechanics, John Wiley and Sons, Ltd.
- 715 [31] McDowell GR, Hau KW. A generalised Modified Cam clay model for clay and
- sand incorporating kinematic hardening and bounding surface plasticity. Granular
- 717 Matter 2004;6:11-6.
- 718 [32] Zhang S, Leng W, Zhang F, et al. A simple thermo-elastoplastic model for
- 719 geomaterials. International Journal of Plasticity, 2012, 34: 93-113.
- 720 [33] Collins I F, Houlsby G T. Application of thermomechanical principles to the
- modelling of geotechnical materials. Proceedings of the Royal Society A: Mathematical,
- 722 Physical and Engineering Sciences, 1997, 453(1964):1975-2001.
- 723 [34] Lebon, Georgy, Jou, et al. Understanding non-equilibrium thermodynamics. 2008.
- 724 [35] B. Spang, Excel add-in for properties of water and steam in si-units, available from
- 725 http://www.cheresources.com/ iapwsif97.shtml, 2002 (2002).
- 726 [36] Yao Y P, Sun D A, Matsuoka H. A unified constitutive model for both clay and

- 727 sand with hardening parameter independent on stress path[J]. Computers &
- 728 Geotechnics, 2008, 35(2):210-222.
- 729 [37] Yao Y P, Sun D A, Luo T. A critical state model for sands dependent on stress
- 730 and density[J]. International Journal for Numerical and Analytical Methods in
- 731 Geomechanics, 2004, 28(4): 323-337.
- 732 [38] Lê T. Comportement thermo-hydro-mécanique de l'argile de boom. PhD Thesis,
- 733 École Nationale des Ponts et Chaussées, France 2008.
- 734 [39] Borja R I, Tamagnini C, Amorosi A. Coupling plasticity and energy-conserving
- elasticity models for clays. Journal of Geotechnical and Geoenvironmentol Engineering,
- 736 1997, 123(10): 948-957.
- 737 [40] Pastén C, Castillo E, Chong S H. Thermo-mechanical ratcheting in soil–structure
- 738 interfaces. Acta Geotechnica, 2019, 14: 1561–1569.
- 739 [41] Zymnis, D M, Whittle A J, Cheng X. Simulation of long-term thermo-mechanical
- response of clay using an advanced constitutive model. Acta Geotechnica. 2019, 14:
- 741 295–31.

742

743

744

745

746

747

748

749

750

751

752

753

755 LIST OF TABLES

756 Table.1 Model parameters of different fine-grained soils

Table.1 Model parameters of different fine-grained soils

Parameters	κ	λ	$\overline{p}'_{c0,0}(ext{kPa})$	$r_{0,0}$	v	α _θ (°C ⁻¹)	$\alpha_I({}^{\mathrm{o}}C^{-1})$	S	$T_0(^{\circ}C)$	n_c	M_{g0}	M_f	A_d	k_f	k_g
Boom clay[8]	0.02	0.18	6000	0.33	-	5×10 ⁻³	5×10 ⁻⁵	8	21.5	-1	0.67	0.67	0.1	0.7	0.9
Geneva clay[25]	0.017	0.062	125	1	0.3	5.2×10 ⁻³	1.5×10 ⁻⁵	12	20	3.5	0.94	0.94	0.1	1.1	1.1
Bonny silt[27]	0.011	0.075	1200	*	0.3	1.6×10 ⁻³	3.5×10 ⁻⁵	10	18	4	1.3	1.3	0.2	1.1	1.1
Pontida clay[12]	0.016	0.103	2500	1	-	3.5×10 ⁻³	5×10 ⁻⁵	10	23	1	-	-	-	-	-

^{&#}x27;-' means the parameters are irrelevant to the simulations in this study.

[&]quot;" means different data are mentioned in this study.

List of Figure Captions

- Fig.1 Permanent reduction in void ratio due to temperature cycles versus overconsolidation ratio (replotted from Demars and Charles[23])
- Fig.2 Yield locus in (a): (p, q) plane at two different temperatures (with $T_1 > T_0$) and (b): two loading yield limits ILY and LY in (p'-T) plane.
- Fig.3 Yield limits in (p', T) plane: (a) TEAM Model (b) ACC2-T Model
- Fig.4 Evolution of yield limits in (p', T) plane during one heating and cooling cycle
- Fig.5 Predicted response of two loading paths in mean effective stress and temperature Plane
- Fig.6 Calibration process of ACC2-T model on set of material parameters for Boom clay: (a) isotropic compression test; (b) one heating-cooling cycle at normal consolidated state; (c) multiple thermal cycles; (d) triaxial compression test at over-consolidated state
- Fig.7 Isotropic/one-dimensional compression tests of Boom clay, Geneva clay and Bonny silt
- Fig.8 Volumetric strain change of Boom clay due to one heating and cooling cycle with different mean effective stresses under drained condition: (a) TEAM model (b) ACC2-T model
- Fig. 9 Triaxial drained behavior of Boom clay at reference temperature 25 °C and high temperature 76 °C: (a) deviatoric stress vs axial strain; (b) volumetric strain vs axial strain;
- Fig.10 Thermal cyclic behaviors of normal consolidated Geneva clay under drained

condition: (a) comparison between ACC2-T model with n_c =3.5 (best fit) and TEAM model; (b) ACC2-T model with n_c =0 and n_c =10; (c) volumetric strain increment due to each thermal cycle by ACC2-T model

- Fig.11 Thermal cyclic behaviors of Bonny silt with different OCRs under drained condition
- Fig.12 Excess pore water pressure accumulation of Pontida clay due to thermal cycles under undrained condition: (a) ACC2-T model; (b) TEAM model
- Fig.13 Correlation between thermal accumulation parameter n_c and plasticity index

 I_p

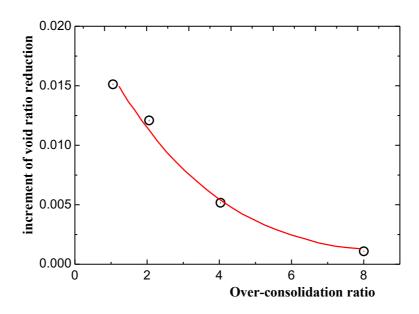


Fig.1 Permanent reduction in void ratio due to temperature cycles versus overconsolidation ratio (replotted from Demars and Charles [23])

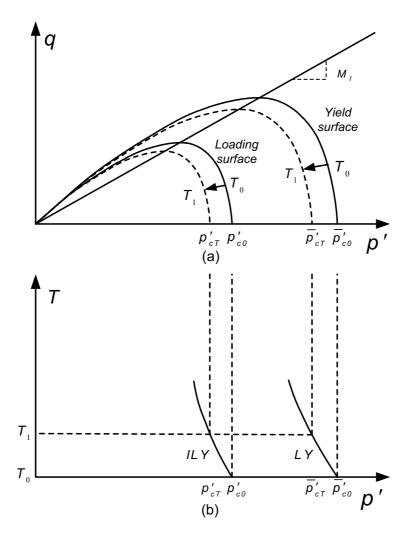


Fig.2 Yield locus in (a): (p', q) plane at two different temperatures (with $T_1 > T_0$) and (b): two loading yield limits ILY and LY in (p'-T) plane.

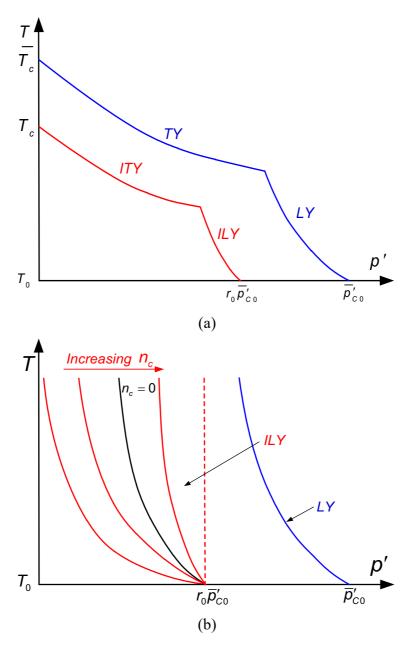


Fig.3 Yield limits in (p', T) plane: (a) TEAM Model (b) ACC2-T Model

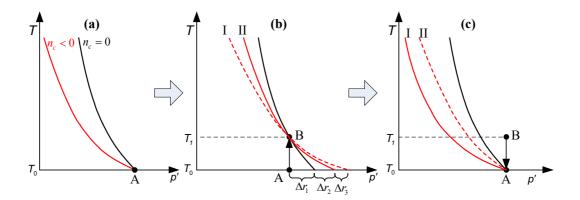


Fig.4 Evolution of yield limits in (p', T) plane during one heating and cooling cycle

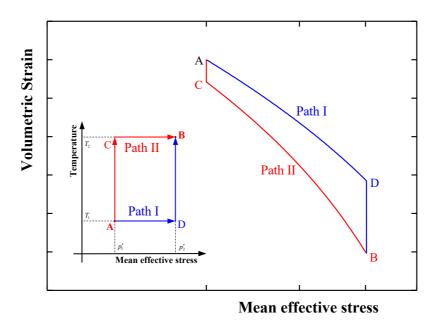
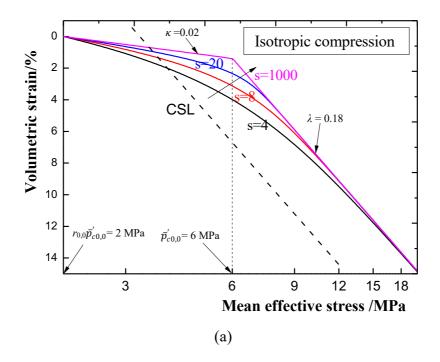
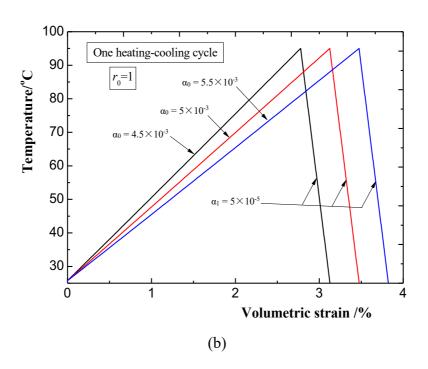


Fig.5 Predicted response of two loading paths in mean effective stress and temperature plane





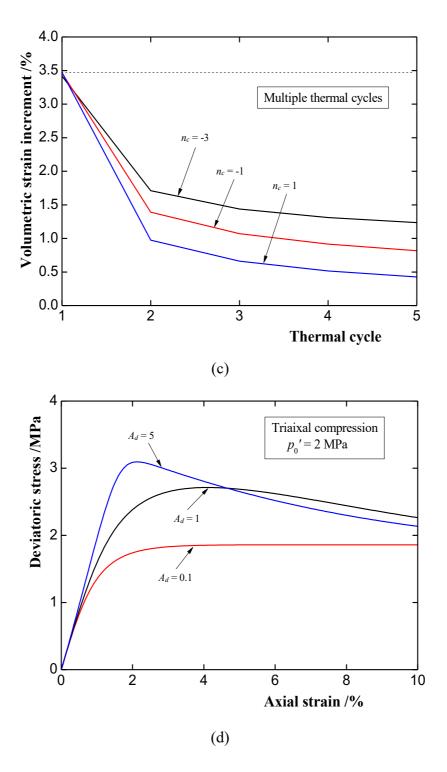


Fig.6 Calibration process of ACC2-T model on set of material parameters for Boom clay: (a) isotropic compression test; (b) one heating-cooling cycle at normal consolidated state; (c) multiple thermal cycles; (d) triaxial compression test at over-consolidated state

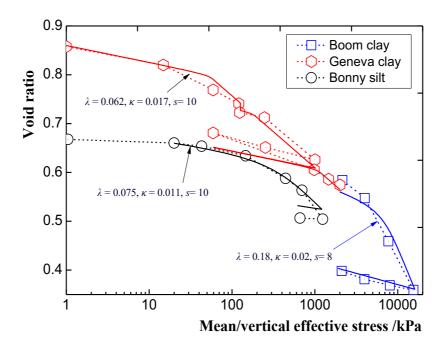


Fig.7 Isotropic/one-dimensional compression tests of Boom clay, Geneva clay and Bonny silt

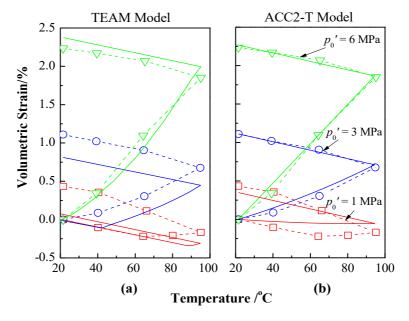


Fig.8 Volumetric strain change of Boom clay due to one heating and cooling cycle with different mean effective stresses: (a) TEAM model (b) ACC2-T model

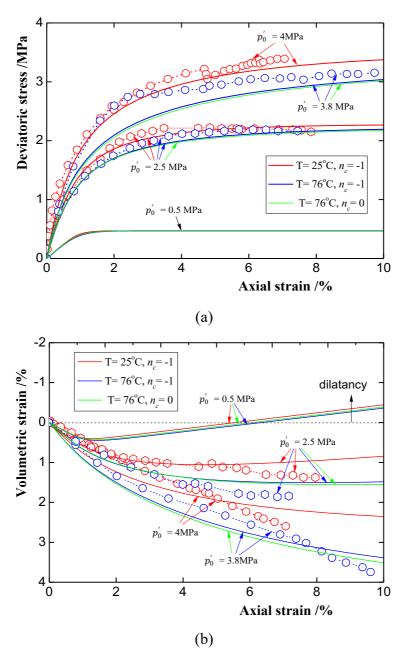
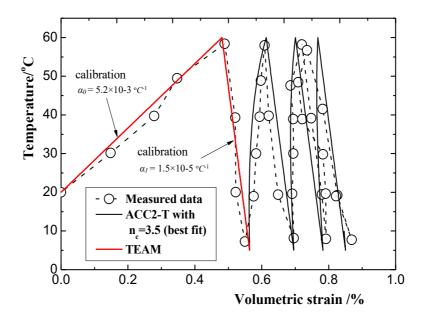
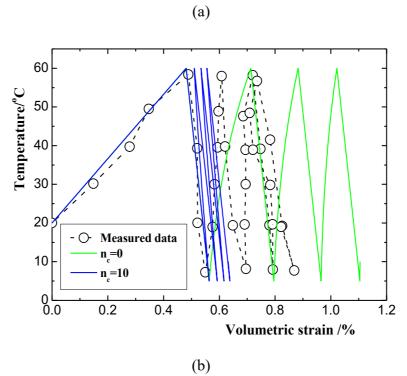


Fig. 9 Triaxial drained behaviors of Boom clay at room temperature 25 °C and high temperature 76 °C: (a) deviatoric stress vs axial strain; (b) volumetric strain vs axial strain;





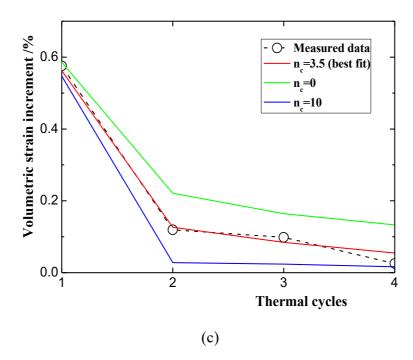


Fig.10 Thermal cyclic behaviors of normal consolidated Geneva clay under drained condition: (a) comparison between ACC2-T model with n_c =3.5 (best fit) and TEAM model; (b) ACC2-T model with n_c =0 and n_c =10; (c) volumetric strain increment due to each thermal cycle by ACC2-T model

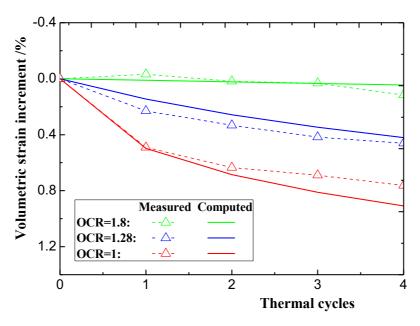


Fig.11 Accumulated strain behavior of Bonny Silt with different OCRs under drained condition

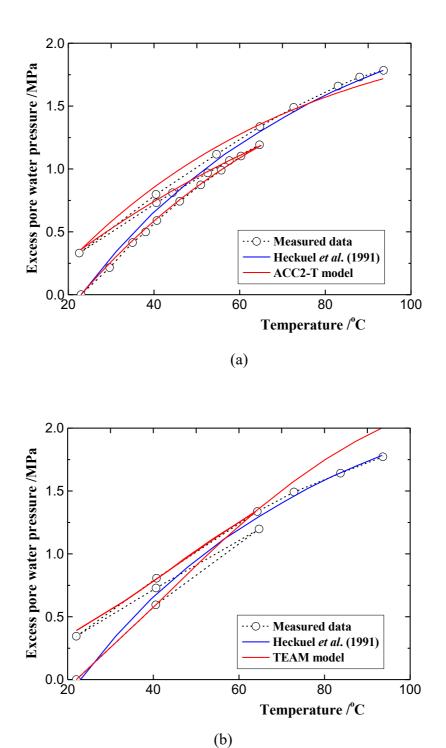


Fig.12 Excess pore water pressure accumulation of Pontida clay due to thermal cycles under undrained condition: (a) ACC2-T model; (b) TEAM model

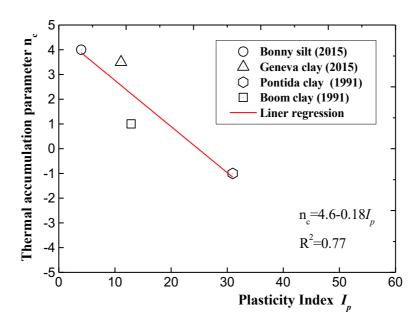


Fig.13 Correlation between thermal accumulation parameter n_c and plasticity index I_p