

Effects of water and fines contents on the resilient modulus of the interlayer soil of railway substructure

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To cite this version:

Trong Vinh Duong, Yu-Jun Cui, Anh Minh A.M. Tang, Jean Claude Dupla, Jean Canou, et al.. Effects of water and fines contents on the resilient modulus of the interlayer soil of railway substructure. Acta Geotechnica, 2016, 11 (1) , pp.51-59. $10.1007/s11440-014-0341-0$. hal-01271097

HAL Id: hal-01271097 <https://enpc.hal.science/hal-01271097v1>

Submitted on 25 Apr 2018

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Abstract

 This paper deals with the resilient behavior of the interlayer soil which is created mainly by the interpenetration of ballast and sub-grade soils. The interlayer soil studied was taken from a site in the South-East of France. Large-scale cyclic triaxial tests were carried out at three water contents ($w = 4$, 6 and 12%) and three fines contents corresponding to 5% sub-grade added to the natural interlayer soil, 10% sub-grade added to the natural interlayer soil and 10% fine particles (< 80 μm) removed from the natural interlayer soil. Soil specimens underwent various deviator stresses, and for each deviator stress a large number of cycles were applied. The effects of deviator stress, number of cycles, water content and fines content on the resilient modulus (*Mr*) were analyzed. It appears that the effects of water content and fines content must be analyzed in a global fashion because the two effects are closely linked. Under unsaturated conditions, the soil containing high fines content has higher resilient modulus due to the contribution of suction. When the soil approaches the saturated state, it loses its mechanical performance with a sharp decrease in resilient modulus.

 Keywords: railway sub-structure; interlayer soil; resilient modulus; fines content; water content; large-scale cyclic triaxial test.

Introduction

 The soils in the sub-structures of highway and railway are subjected to a huge number of traffic loading cycles. In this context, the resilient modulus of sub-structure soils is an important parameter to be considered when designing new tracks or when maintaining under-operation tracks. Indeed, several authors [1, 4, and 28] reported that the resilient modulus of sub-grade can strongly influence the mechanical behavior of sub-structure.

 For the French ancient railway tracks constructed in the 1880s, as ballast was placed directly on the sub-grade during the construction without any separation layers, an interlayer was naturally created over time mainly by the interpenetration of ballast and sub-soil under the traffic effect [5-7, 32]. This interlayer has been kept as part of the sub-structure considering its high mechanical performance related to its high unit mass [33]. As the interlayer is a "component" of the sub-structure overlying the sub-grade, its mechanical behavior appears to be of primary importance for the overall behavior of sub-structure even the overall track structure. However, because this material has been formed naturally, it can present large variability in terms of fines natures and fines contents. Moreover, under the effect of climatic conditions, soil water content changes also constantly. These changes in fines content, fines nature and water content can greatly affect soil mechanical behavior such as soil resilient modulus.

The notion of resilient behavior appeared for the first time in the middle of the $20th$ 70 century [16, 17]. In the railway context, the resilient modulus (M_r) is defined as the secant slope of the curve of deviator stress versus axial strain obtained from cyclic triaxial tests [21, 26-28, 30, and 37]. Previous studies showed that there are several factors that affect the resilient modulus of unbound granular materials, in particular the stress level [14, 22, 24, 26, and 30]. The increase in moisture content appears to decrease the resilient modulus [10, 11, and 14]. For the effect of

 loading cycles, a large disagreement exists in terms of number of cycles required to reach the stabilization of resilient modulus [23, 24, 30, 35, 36]. As far as the effect of fines content is concerned, there is no conclusive observation as mentioned by Lekarp et al. [24]. Thom and Brown [31] and Kamal et al. [20] reported that the resilient modulus generally decreases when the fines content increases. However, Jorenby and Hicks [19] observed that the stiffness of crushed aggregate has an initially increase trend followed by a considerable reduction when clayey fines content increased.

 All these factors (moisture content, fines content, number of cycles) influence the resilient response of materials. However, to the authors' knowledge, their combined effect has rarely investigated especially for the interlayer soil. In the present work, large-scale cyclic triaxial tests were carried out to study the variations of *Mr* of an interlayer soil under the combined effects of stress level, water content, fines content and cyclic loadings.

Materials and methods

 The studied interlayer soil was taken from Sénissiat, near Lyon, France. The grain size distribution curves of the natural interlayer soil (*ITL0*) and the sub-grade soil (SG) are presented in Fig. 1. It can be observed that the interlayer soil has a large fines content (16% of particles are smaller than 80 μm), and its grain size distribution curve is well graded from ballast size (60 mm) to clay size (< 2 μm). Its physical properties (density, plasticity index, blue methylene value and proctor curve) of this material were reported by Trinh et al*.* [33, 34]. For the SG, almost all soil 94 particles are smaller than 80 μ m.

 In order to study the influence of fines content, the fines content of the soil was varied by either removing fine particles smaller than 80 μm from the interlayer soil (-10% for *ITL-10*) or adding sub-grade soil into the interlayer soil (+5% for *ITL⁵* and +10% for *ITL10*). The percentages

 refer to the ratio of dry mass of fine particles to dry mass of interlayer soil. The removal of fine particles for the preparation of *ITL-10* was done by sieving. The grain size distribution curves of *ITL-10, ITL⁵* and *ITL¹⁰* are also shown in Fig. 1.

 For the specimen preparation, water were first added and mixed with the material using a large mixer to reach the target water content. After mixing, the wet materials were stored in hermetic containers for at least 24 h for moisture homogenization. Compaction was performed in 104 6 layers of 0.1 m thick each using a vibratory hammer to a dry unit mass of 2.01 Mg/m³. This is the maximum dry unit mass which can be reached in the adopted conditions without breaking ballast particles.

 Because large particles were involved, a large-scale triaxial apparatus developed by Dupla et al. [8] was used, enabling specimens of 300 mm in diameter and 600 mm in height to be tested. This apparatus can apply large number of loading cycles (up to several millions) at a frequency up to several tens of Hertz.

 The program of tests is presented in Table 1. All the four soils were tested at three water 112 contents ($w = 4\%$; 6% and 12%) corresponding to three initial degrees of saturation ($S_{ri} = 32\%$; 113 49% and 100%), except *ITL*₅ on which only one test at a water content of $w = 6\%$ was conducted owing to lack of material. The tests are named according to the material (*ITL-10, ITL0, ITL5, ITL10*) and water content. For instance, *ITL0w4* corresponds to the test on *ITL⁰* at 4% water content. To overcome the problem related to the limited material quantity, the multi-step loading procedure proposed by Gidel et al. [12] was adopted. This procedure enables several deviator stress levels to be applied before the soil specimen reaches the failure state, thereby reducing the number of tests on one hand and avoiding the effect of variability of soil specimens on the other hand.

120 The cyclic triaxial tests were performed under a constant confining pressure $\sigma_3 = 30$ kPa. This value was chosen by referring to the wheel load generated by train [2], the depth of the interlayer (from 250 mm to 600 mm), the Poisson's ratio (0.3 - 0.4 as proposed by Selig and Waters [28]). The vertical stress at the top of interlayer was found to be 40 to 90 kPa. These values correspond to the Indian railways as reported by Jain and Keshav [18] and American railways as reported by Selig and Waters [28] and Yang et al. [39]. In other countries where heavier wagons are used, the wheel load may reach 30 tons per axle [2], leading to a vertical stress of 120 to 140 kPa on the interlayer [13, 18, 25]. In this study, a maximum deviator stress of 200 kPa was applied. All the tests were performed under drained condition; the valves were open (under unsaturated condition) or connected to a water back pressure source (under saturated condition). During the saturated triaxial test, the back pressure was kept constant and pore water can drain freely. For the loading frequency, a value of 5 Hz was chosen because this is the dominant one among a number of frequencies generated in the French ancient sub-structures at a train speed of 100 km/h [29]. During the tests, the deviator stress was increased in steps from 0 to various target values; in each step, 30 000 cycles were applied and the variations of axial strain were recorded.

Results

 [Fig. 2](#page-23-0) presents typical curves of deviator stress versus axial strain for the first cycles in test *ITL*₅*w6*. It also shows the definition of permanent axial strain (ε _{*p*}), the resilient axial strain (ε _{*r*}) through the first cycle. It can be observed that the minimum deviator stress did not totally reach zero for all cycles. This was probably due to the high loading/unloading speed (frequency of 5 Hz) that caused a delay between the target signal and the real signal. However, it is believed that this problem does not affect the resilient modulus (*Mr*) that corresponds to the secant slope of curves (see Fig. 2).

[Fig. 3](#page-24-0) plots the deviator stress versus the axial strain for the moments where the values of Δq_{max} were increased: during the first 8 cycles (N = 8) under *Δqmax* = 45 kPa [\(Fig. 3](#page-24-0)*a*), from *Δqmax* = 45 kPa (N = 30 000) to *Δqmax* = 90 kPa (N = 30 001 - 30 0004) [\(Fig. 3](#page-24-0)*b*), from *Δqmax* = 90 kPa (N = 60 000) to *Δqmax* = 145 kPa (N = 60 001 - 60 0004) [\(Fig. 3](#page-24-0)*c*) and from *Δqmax* = 145 kPa (N = 90 000) to *Δqmax* =20 kPa (N = 90 001 - 90 0004) [\(Fig. 3](#page-24-0)*d*). It can be observed that when a new deviator stress was applied, the axial strain increased accordingly. During the very first cycles under each stress level, the loading and unloading paths did not form close cycles, suggesting that significant permanent axial strain developed. In this case, the resilient modulus was determined based on the unloading path of a cycle and the loading path of the next cycle. The hysteresis loop was large in the first cycles, and with the increase of number of cycles, this hysteresis became less and less significant. At large number of cycles by the end of each loading level, the material behaved almost in a purely elastic fashion. Werkmeister et al. [38] reported that the change in the loop shape provides information about the different deformation mechanisms. In the beginning, there was probably particles rotation and rearrangement producing the plastic strain. Over time, these particles movements became limited and a purely resilient state is reached where strain is due to the deformation at the contacts of particles. Note that the shape of loading/unloading loops is related to the slope adopted for the determination of the resilient modulus. When two paths formed a close cycle, the straight line between the lowest and highest point of the loading/unloading cycle was used in the determination.

 [Fig. 4](#page-25-0) depicts the evolution of resilient strain with number of cycles for test *ITL2w12*. When the deviator stress increased, the resilient strain increased sharply during the first cycles of each stress level, and decreased afterwards to reach stabilization. The resilient strain was larger under higher deviator stress.

 [Fig. 5](#page-26-0) depicts the variations of *M^r* with the number of cycles (*N*) at three water contents 168 and various deviators stress levels for ITL_{10} . In the case of $ITL_{10}w4$ [\(Fig. 5a](#page-26-0)) at $\Delta q_{max} = 23$ kPa, the data of resilient modulus shows some scatter, but in general an increase trend can be identified. Because of the data scatter, it is difficult to determine the number of cycles at which the stabilization of resilient modulus started. The values in other stress levels are more or less constant around 250 MPa. For *ITL10w6* [\(Fig. 5b](#page-26-0)), the resilient modulus for all stress levels are found to increase significantly in the beginning and then stabilize after around 15 000 cycles. When *Δqmax* was increased from 45 kPa to 90 kpa, the resilient modulus rose up sharply. By contrast, an opposite trend was observed when *Δqmax* was increased from 90 to 140 kPa. It can be seen from Fig. 5c that for each deviator stress level, the resilient modulus decreased during the first cycles. For instance, it decreased from 168 MPa to 144 MPa from cycle 1 to cycle 7. However, this decreasing trend came very quickly to its end and was replaced by an increasing one. Afterwards, the increase rate slowed down and the resilient modulus value tended to stabilize after about 5000 loading cycles. Referring to [Fig. 4,](#page-25-0) the significant variations of resilient modulus in Fig. 5 correspond to the phase characterized by quick development of resilient axial strain just after the change of stress level, and the stabilization states of resilient modulus corresponds to the stabilization of resilient axial strain.

 These observations are confirmed in the case of *ITL5w6* (see [Fig. 6\)](#page-27-0). For all stress levels, the 185 resilient modulus increased with the number of cycles during the first cycles. At $\Delta q_{max} = 45$ kPa 186 about 10 000 cycles were needed for the resilient modulus to become stable while at $\Delta q_{max} = 140$ kPa and 200 kPa, about 5000 cycles were needed. The variation range of *M^r* at all stress levels is about ±10 MPa. On the whole, the effect of deviator stress is not as clear as in the case of *ITL10w6*.

 The results of *ITL⁰* are presented in [Fig. 7.](#page-28-0) The variation of *Mr* with *N* is more pronounced in the case of *ITL0w12* [\(Fig. 7c](#page-28-0)) than in the cases of *ITL0w4* [\(Fig. 7a](#page-28-0)) and *ITL0w6* [\(Fig. 7b](#page-28-0)). After the 192 first variations when the deviator stress Δq_{max} changed, the resilient modulus increased with the number of cycles in the case of *ITL0w12*, while the changes in the two other cases are not clear.

 As regards *ITL-10*, the results with three different water contents are presented in [Fig. 8.](#page-28-1) In the 195 two cases of $w = 4\%$ and 12%, the resilient modulus did not vary much for the deviator stress up to 90 kPa, suggesting an insignificant influence of the number of cycles. Also, the influence of Δq_{max} is insignificant because albeit the variation of Δq_{max} , the resilient modulus remained at a 198 steady value: about 230 MPa for $ITL_{10}W12$ and 250 MPa for $ITL_{10}W4$. In the case of $w = 6\%$ [\(Fig. 8b](#page-28-1)), the variation is clearer as the results show a slight increasing trend of *M^r* with the 200 number of cycles and Δq_{max} . At the stress level of 140 kPa, there was a sharp decrease of M_r , 201 regardless of the water content: for the three tests, when Δq_{max} was increased from 90 kPa to 140 kPa, a reduction of *M^r* of about 50 kPa was produced. Afterwards, the variations of resilient modulus with the number of cycles became much more pronounced than in the cases of other deviator stress levels.

Discussions

 From the test results, it was observed that after a few scattered results at the beginning of each stress level, the resilient modulus became stable with the number of cycles. However, the variations were different for different soils and different water contents. The variations were clear in the case of *ITL¹⁰* [\(Fig. 5b](#page-26-0) and c), insignificant in the first part of test *ITL0w4* [\(Fig. 7a](#page-28-0)) and *ITL-*

 ¹⁰w4 [\(Fig. 8a](#page-28-1)). The stabilization value was reached right after the first cycles in test *ITL0w4* (see [Fig. 7a](#page-28-0)) and after 15 000 cycles in test *ITL10w6* (see [Fig. 5b](#page-26-0)). Therefore, it can be stated that the number of cycles needed for *M^r* to reach stabilization depends on the stress level, water content, and fines content. This can explain the disagreement found in literature regarding the number of cycles required to attain a stable resilient state: Stewart [30] studied the ballast behavior and reported a stabilization after 1000 cycles while Hicks and Monismith [14] and Allen and 216 Thompson [3] (cited by Lekarp et al. [24] and Lackenby [23]) observed that $50 - 100$ cycles are needed for the stabilization for granular materials.

218 The variations of resilient modulus during the scattered phase at the beginning of each Δq_{max} were observed in all tests. This phase corresponds to the stage where the permanent axial strain developed quickly and the loading/unloading path did not form a close cycle in the deviator stress 221 – axial strain plane. This can be explained as follows: when Δq_{max} was increased, the soil behavior became elasto-plastic; thus irreversible strain was produced. However, this phenomenon occurred during the first loading. Afterwards, the cyclic loading led to a progressive stabilization of the particles arrangement, thereby a negligible plastic strain.

 For a better analysis on the effects of deviator stress and water content, the end-level resilient modulus values (after 30 000 cycles for each deviator stress level) are plotted versus deviator stress in Fig. 9. For *ITL¹⁰* (Fig. 9a), the results at 4% and 12 % water contents present a slight decrease of resilient modulus when the deviator stress was increased from 23 to 102 kPa. On the contrary, in the case of 6% water content, the resilient modulus increased and then reached stabilization. The values of 4% and 6% water contents fall in the same range, around 250 MPa and clearly higher than the values of 12% water content. For *ITL⁰* (Fig. 9b), at 4% and 6% water content, the resilient modulus increased with the deviator stress and the values of 4% are higher

233 than those of 6%. The values of $ITL₀$ in near saturated state ($w = 12\%$) are, as opposed to the case of *ITL10*, higher than those of 4% water content. In the case of *ITL-10* (Fig. 9c), the curves have almost the same shape: a stage of slight variations up to 90 kPa of deviator stress followed by a stage of decrease, the decrease being more pronounced in the case of *ITL-10w12*.

 In terms of water content effect, the value of *ITL-10* at 4% water content is the highest; the values of 12% water content are lower than those of 4% water content but higher than those of 6% water content. The relative positions of these curves show that the water content effect is not the same for the three materials. It appears that the increase of water content brings a negative effect to the resilient modulus of the soil that has the highest fines content *(ITL10*). However, for *ITL⁰* and *ITL- ¹⁰*, the resilient modulus decreased when water content changed from 4% to 6% but increased when water content was increased to 12%. Note that only a decreasing trend of resilient modulus with growing saturation level for granular material was observed by Lekarp [24]. More studies are required to clarify this issue.

 For *ITL-10*, a deviator stress of 90 kPa appears to be the critical value for the variations of resilient modulus: all tests showed a decrease of resilient modulus at this stress level, suggesting a significant change in soil behavior. As mentioned previously, after a certain number of cycles, the resilient behavior was mainly governed by the contacts of soil particles. When the imposed deviator stress increased, the stress applied at the inter-particles contact exceeds its limit and 251 particle breakage may occur. As a result, a sharp decrease of M_r is produced. This could be the case for *ITL-10* that has the lowest fines content. For *ITL⁰* and *ITL10,* this phenomenon of particle breakage was probably attenuated, leading to much smaller decrease of *Mr*.

 As far as the effect of water content is concerned, the results show that the relative positions of the curves of three different water contents are not the same for the three materials. This suggests that the soil composition can strongly influence the material resilient modulus. [Fig.](#page-30-0) [10](#page-30-0) presents the results according to the water content: 4%; 6% and 12% in Figs. a, b and c, 258 respectively. The effect of fines content can be observed clearly. In the case of $w = 4\%$, the results of *ITL-10* and *ITL¹⁰* are almost identical for the deviator stress up to 100 kPa. But much lower values are observed for *ITL⁰* for the deviator stress up to 140 kPa. Beyond 140 kPa deviator stress, the values become almost the same for *ITL-10* and *ITL0.* At 6% water content, the resilient modulus of *ITL⁰* is also the smallest, showing that when decreasing the fines content (from *ITL¹⁰* to *ITL0*), a reduction of resilient modulus is produced. However, when the fines content is decreased to a level as low as *ITL-10*, the resilient modulus starts to increase. Under the near 265 saturation conditions ($w = 12\%$ in [Fig. 10c](#page-30-0)), it is observed that the greater the fines content, the lower the resilient modulus.

 Fig. 11 plots the end stage resilient modulus at three stress levels with the variation of water content and fines content. Despite of the scatter, it can be generally observed a clear trend 269 of *M_r* at all water content. It slightly deceases when the fine content added increases from -10% to 270 0%. After that, it can be observed a significant increase of M_r when the fine content added passes to 10%. Adding more fine particles, in one hand, limited the contact between big particles contact (ballast), but in other hand, increase the suction, as the gravimetric water content was kept constant.

 To identify the mechanisms of these phenomena, it appears necessary to consider the combined effects of the fines content and the water content which is linked to the soil suction. It is well known that for unsaturated soils, suction contributes to the soils shear strength, especially for the fine-grained soils. This explains why fine particles show a positive effect on the resilient modulus under unsaturated conditions, but a negative effect under saturated conditions. It can be observed 279 in the case of $\Delta q_{max} = 45$ kPa (Fig. 11a), for the case of 12% of water content, there was no more suction effect, and the resilient modulus decrease with the increase of fine content. This implies that in unsaturated conditions, due to the suction effect the interlayer soil containing high fines content has a better mechanical performance, while in near saturation conditions, higher fines contents leads to a significant degradation of mechanical performance. This is in agreement with the observations of Huang et al. [15], Ebrahimi [9] and Duong et al. [7]. From a practical point of view, these findings are important for the maintenance of railway tracks. If the soil containing high fines content can satisfy the requirements in terms of resilient modulus under unsaturated conditions, measures must be taken to protect it from water infiltration. Very often, it is a good drainage system that should be set up for this purpose.

Conclusions

 The resilient behavior of an interlayer soil taken in a railway sub-structure in France was studied in the laboratory. The effects of deviator stress level, number of cycles, water content and fine content were investigated by performing large-scale cyclic triaxial tests. Four fines contents and 3 water contents were considered.

 At each deviator stress level, after the first scattered results due to the plastic behavior of soil, the resilient modulus tended to stabilize with the number of cycles. It was found that the number of cycles needed to reach stabilization depends on the material nature, water content and stress level.

 The effects of water content and of fines content are linked, and it appeared impossible to distinguish the two effects. Indeed, in unsaturated conditions, due to the suction effect, the soil having high fines content showed higher resilient modulus. On the contrary, when the soil approached the saturated conditions, the fine particles provided a negative effect. This suggests that drainage measures must be taken to protect the interlayer soil when its mechanical performance appears satisfactory under unsaturated conditions but unsatisfactory under saturated conditions.

Acknowledgements

 This study was carried out within the research project RUFEX "Reuse and reinforcement of ancient railway sub-structure and existing foundations". The authors would like to address their deep thanks to Ecole des Ponts ParisTech (ENPC), Railway Network of France (RFF), French Railways Company (SNCF) and French National Research Agency for their supports.

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- [Fig. 3: Deviator stress versus axial strain for test ITL](#page-24-1)₅w6. a) N = 1-8 (Δq_{max} = 45 kPa); b) from
- *Δqmax* = 45 kPa (N = 30 000) to *Δqmax* = 90 kPa (N = 30 001 [30 0004\); c\) from](#page-24-1) *Δqmax* = 90 kPa
- 417 (N = 60 000) to $\Delta q_{max} = 145$ kPa (N = 60 001 60 0004); d) from $\Delta q_{max} = 145$ kPa (N = 90 000)
- 418 to $\Delta q_{\text{max}} = 20 \text{ kPa}$ (N = 90 001 90 0004)
- 419 Fig. 4: Resilient strain versus number of cycles in test $ITL_{10}w12$
- [Fig. 5: Resilient modulus versus number of cycles for ITL](#page-25-1)₁₀. a) $w = 4\%$; b) $w = 6\%$; c) $w = 12\%$
- 421 Fig. 6: Resilient modulus versus number of cycles for $ITL₅$ w6
- [Fig. 7: Resilient modulus versus number of cycles for ITL](#page-27-1)₀. a) $w = 4\%$; b) $w = 6\%$; c) $w = 12\%$
- [Fig. 8: Resilient modulus versus](#page-28-2) number of cycles for ITL₋₁₀. a) $w = 4\%$; b) $w = 6\%$; c) $w = 12\%$
- [Fig. 9: End-stage resilient modulus versus deviator stress -](#page-29-0) Effect of water content. a) *ITL10*; b)
- *ITL0*[; c\)](#page-29-0) *ITL-10*
- 426 [Fig. 10: End-stage resilient modulus versus deviator stress -](#page-30-1) Effect of fines content. a) $w = 4\%$; b) 427 $w = 6\%$ and c) $w = 12\%$
- 428 Figure 11: Resilient modulus in function of water content at different fine contents; a) at $\Delta q_{\text{max}} =$
- 429 45 kPa and b) at $\Delta q_{\text{max}} = 140$ kPa
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433 **Table 1: Test program**

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439 **Fig. 1: Grain size distribution of the studied materials**

443 **Fig. 2: Deviator stress versus axial strain for test ITL5w6 - Determination of resilient** 444 **modulus**

448 Fig. 3: Deviator stress versus axial strain for test ITL₅w6. a) N = 1-8 (Δq_{max} = 45 kPa); b) **from** *Δqmax* **= 45 kPa (N = 30 000) to** *Δqmax* **= 90 kPa (N = 30 001 - 30 0004); c) from** *Δqmax* **= 90 kPa (N = 60 000) to Δqmax = 145 kPa (N = 60 001 - 60 0004); d) from Δqmax = 145 kPa (N** $451 = 90000$ to $\Delta q_{\text{max}} = 20 \text{ kPa}$ (N = 90 001 - 90 0004)

Fig. 4: Resilient strain versus number of cycles in test ITL10w12

458 Fig. 5: Resilient modulus versus number of cycles for ITL₁₀. a) $w = 4\%$ **; b)** $w = 6\%$ **; c)** $w = 459$ **12% 12%**

Fig. 6: Resilient modulus versus number of cycles for ITL5w6

465 Fig. 7: Resilient modulus versus number of cycles for ITL₀. a) $w = 4\%$; b) $w = 6\%$; c) $w = 466$ **12**% **12%**

468

469 **Fig. 8: Resilient modulus versus number of cycles for ITL₋₁₀. a)** $w = 4\%$ **; b)** $w = 6\%$ **; c)** $w =$ 470 **12%**

 Fig. 9: End-stage resilient modulus versus deviator stress - Effect of water content. a) *ITL10***; b)** *ITL0***; c)** *ITL-10*

 Fig. 10: End-stage resilient modulus versus deviator stress - Effect of fines content. a) *w* **=** 478 **4%; b**) $w = 6\%$ and **c**) $w = 12\%$

 $\begin{array}{c} 481 \\ 482 \\ 483 \end{array}$ 482 **Figure 11: Resilient modulus in function of water content at different fine contents; a) at Δqmax = 45 kPa; b) at** $\Delta q_{\text{max}} = 90$ kPa and c) at $\Delta q_{\text{max}} = 140$ kPa