## Semantizing Complex 3D Scenes using Constrained Attribute Grammars


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slight variant of the material presented at SGP 2013

## Motivation

Semantizing complex objects in 3D scenes


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- Building industry
$\square$ for the renovation market
- point cloud $\rightarrow$ building model


Semantized geometry

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$\square$ for architects
- building sketch $\rightarrow$ rendering


Semantized geometry (rendered)

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- building sketch $\rightarrow$ rendering
- Game industry
$\square$ for graphic designers
- basic level design $\rightarrow$ rendering


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$\square$ for the renovation market
- point cloud $\rightarrow$ building model
$\square$ for architects
- building sketch $\rightarrow$ rendering
- Game industry
$\square$ for graphic designers
- basic level design $\rightarrow$ rendering
- Object mining in shape databases
$\square$ for semantic queries
- 3D object $\rightarrow$ semantic labeling


Semantized geometry

## Outline

Constrained attribute grammars

Scene interpretation

Bottom-up parsing

Experiments

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## Grammars to express hierarchical decomposition



## Complex, non-hierarchic relations between components



## Constrained attribute grammars

$G=(N, T, P, S)$

- $N$ : nonterminals ( $\leftrightarrow$ complex forms)
e.g., window, wall
- $T$ : terminals ( $\leftrightarrow$ geometric primitives) e.g., polygon, cylinder
- P: production rules ( $\leftrightarrow$ hierarchical decomposition and constraints)
- S: start symbols ( $\leftrightarrow$ root shapes) e.g., building


## Basic rules

Decomposition of a complex object $y$ of type $Y$ into its constituents $x_{i}$ of type $X_{i}$ :

$$
Y y \longrightarrow X_{1} x_{1}, \ldots, X_{n} x_{n}
$$

Example:

$$
\text { step } s \longrightarrow \text { riser } r \text {, tread } t
$$

Rule application:

- top-down view:
$y$ decomposes into $x_{1}, \ldots, x_{n}$

- bottom-up view:
given some $x_{1}, \ldots, x_{n}$, create a new object $y$


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## Constraints

Conditional rule application (conjonction of predicates):

$$
Y y \longrightarrow X_{1} x_{1}, X_{2} x_{2}, \ldots\left\langle\operatorname{cstr}_{1}\left(x_{1}\right), \operatorname{cstr}_{2}\left(x_{1}, x_{2}\right), \ldots\right\rangle
$$

## Example:

$$
\begin{aligned}
\text { riser } r \longrightarrow & \text { polygon } p\langle\operatorname{vertical}(p)\rangle \\
\text { tread } t \longrightarrow & \text { polygon } p\langle\text { horizontal }(p)\rangle \\
\text { step } s \longrightarrow & \text { riser } r, \text { tread } t \\
& \langle\operatorname{edgeAdj}(r, t), \text { above }(t, r)\rangle
\end{aligned}
$$



## Attributes

Features attached to each grammar element:

- at creation time (primitives)
- at rule application (synthetized attributes)

Examples:

- length, width
- bounding box
- ...



## Predicates

Predicates on grammar elements:

- adj, edgeAdj
- orthogonal, parallel
- vertical, horizontal

Predicates on attributes:
$\square \geq,>, \leq, \ldots$

- $=, \neq$
- ...

Example: r.length $==$ t.length

## Collections of similar elements

Grouping elements via recursion ( $Y$ as set of $X$ s):

$$
\begin{aligned}
Y y & \longrightarrow X x \\
Y y & \longrightarrow X x, Y_{y_{2}}
\end{aligned}
$$

Grouping elements via specific collection operators:

$$
Y y \longrightarrow \operatorname{coll}(X) x s
$$

Useful operators: maximal collections

- maxconn: maximal set of connected components
- maxseq: maximal sequence

Example:

$$
\text { stairway sw } \longrightarrow \text { maxseq(step, adjEdge) ss }
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- ... [see complete stairway grammar]

Example:

$$
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## Scene interpretation: parse tree

Tree representation of a grammatical analysis of the scene:

- leaves: terminals representing primitives
- non-leaf nodes: instanciations of grammar rules



## Scene interpretations: parse forest

Set of parse trees
with systematic sharing (DAG)
Compact representation of all possible interpretations


## Ambiguity and the exclusivity constraint

Example (assuming no height ordering constraint):

$$
\text { step } s \longrightarrow \text { riser } r, \text { tread } t\langle\text { edgeAdj }(r, t)\rangle
$$



Exclusivity constraint:
at most 1 occurrence of a grammar element per interpretation


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## Parse forest computation

Bottom-up parsing:
construction of the parse forest from leaves (terminals) to roots (start symbols)

- create one terminal for each primitives
- iteratively create new grammar elements from existing ones
$\square$ e.g., given grammar rule step $s \longrightarrow$ riser $r$, tread $t$ given existing instances riser $r_{23}$, tread $t_{18}$ create new instance step $\mathrm{S}_{5}$
- merge identical trees on the fly
- stop iterating when no rule applies

Rule application order

- Simple rules: use any order
- Maximal operators: wait for all subelements to ensure maximality


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## Rule application order

- Simple rules: use any order
- Maximal operators: wait for all subelements to ensure maximality
$\square$ reverse topological sort of nonterminal dependency graph



## Mastering the combinatorial explosion

Usual drawback of bottom-up analysis: combinatorial explosion

- all trees
- all sets, all sequences, ...
- all combinations

Our solution:

- tree sharing: construction of a parse forest $\quad$ (exp. $\rightarrow$ lin.)
- maximal operators, with efficient implementation ( $>\exp . \rightarrow$ polyn.)
- constraint propagation: predicate ordering $\Rightarrow$ early pruning

Maximal operators
maxseq


Maximal operators


## Constraint propagation as predicate ordering

## A simple 2D example

pair $p \longrightarrow$ seg $s_{1}$, seg $s_{2},\left\langle\operatorname{orthogonal}\left(s_{1}, s_{2}\right), \operatorname{adj}\left(s_{1}, s_{2}\right), \operatorname{vertical}\left(s_{1}\right)\right\rangle$


## Constraint propagation as predicate ordering

## Example of poor ordering

pair $p \longrightarrow$ seg $s_{1}$, seg $s_{2},\left\langle\underline{\text { orthogonal }\left(s_{1}, s_{2}\right)}, \operatorname{adj}\left(s_{1}, s_{2}\right), \operatorname{vertical}\left(s_{1}\right)\right\rangle$

1. orthogonality

Complexity:
$O\left(\# \operatorname{seg}^{2}\right)$


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satisfied constraints

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1. orthogonality
2. adjacency

Complexity:
$O\left(\# s e g^{2}+\right.$ $\#$ seg $\times$ maxDeg $)$
$=O\left(\# \operatorname{seg}^{2}\right)$


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1. orthogonality
2. adjacency

Complexity:

$$
\begin{aligned}
& O\left(\# \operatorname{seg}^{2}+\right. \\
&\quad \# s e g \times \operatorname{maxDeg}) \\
&= O\left(\# s e g^{2}\right)
\end{aligned}
$$


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1. orthogonality
2. adjacency
3. verticality

Complexity:

$$
\begin{aligned}
& O\left(\# \operatorname{seg}^{2}+\right. \\
& \quad \# \text { seg } \times \operatorname{maxDeg}+ \\
& \quad \# \text { seg }) \\
& =
\end{aligned}
$$


constraints to test

## Constraint propagation as predicate ordering

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& \quad \# \text { seg }) \\
& = \\
& O\left(\# \operatorname{seg}^{2}\right)
\end{aligned}
$$


satisfied constraints

## Constraint propagation as predicate ordering

## Example of good ordering

pair $p \longrightarrow \operatorname{seg} s_{1}$, seg $s_{2},\left\langle\operatorname{orthogonal}\left(s_{1}, s_{2}\right), \operatorname{adj}\left(s_{1}, s_{2}\right), \underline{\left.\operatorname{vertical}\left(s_{1}\right)\right\rangle}\right.$

1. verticality

Complexity :
O(\#seg)

constraints to test

## Constraint propagation as predicate ordering

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pair $p \longrightarrow \operatorname{seg} s_{1}$, seg $s_{2},\left\langle\operatorname{orthogonal}\left(s_{1}, s_{2}\right), \operatorname{adj}\left(s_{1}, s_{2}\right), \underline{\left.\operatorname{vertical}\left(s_{1}\right)\right\rangle}\right.$

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Complexity :
O(\#seg)

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pair $p \longrightarrow \operatorname{seg} s_{1}$, seg $s_{2},\left\langle\operatorname{orthogonal}\left(s_{1}, s_{2}\right), \operatorname{adj}\left(s_{1}, s_{2}\right), \underline{\left.\operatorname{vertical}\left(s_{1}\right)\right\rangle}\right.$

1. verticality
2. adjacency

Complexity :

$$
\begin{aligned}
& O(\# \operatorname{seg}+ \\
&\quad \# \operatorname{seg} \times \operatorname{maxDeg}) \\
&= O(\# \operatorname{seg} \times \operatorname{maxDeg})
\end{aligned}
$$



## Constraint propagation as predicate ordering

## Example of good ordering

pair $p \longrightarrow$ seg $s_{1}$, seg $s_{2},\left\langle\underline{\text { orthogonal }\left(s_{1}, s_{2}\right)}, \underline{\operatorname{adj}\left(s_{1}, s_{2}\right)}, \underline{\left.\operatorname{vertical}\left(s_{1}\right)\right\rangle}\right.$

1. verticality
2. adjacency
3. orthogonality

Complexity :

$$
\begin{aligned}
& O(\# \text { seg }+ \\
& \quad \# \text { seg } \times \operatorname{maxDeg}+ \\
& \quad \# \text { seg } \times \operatorname{maxDeg}) \\
& =O(\# \text { seg } \times \operatorname{maxDeg}) \ll O\left(\# \operatorname{seg}^{2}\right)
\end{aligned}
$$


satisfied constraints

## Constraint propagation as predicate ordering

1. Unary predicates
$=$ constraints implying only 1 element: complexity $O$ (\#element)
Example:

$$
\text { riser } r \longrightarrow \text { polygon } p\langle\operatorname{vertical}(p)\rangle
$$

## Constraint propagation as predicate ordering

1. Unary predicates
2. Invertible predicates that are partially instantiated
$=$ constraints with small cardinality when some arguments are fixed
Example:

$$
\text { step } s \longrightarrow \text { riser } r \text {, tread } t\langle\text { edgeAdj }(r, t)\rangle
$$

## Constraint propagation as predicate ordering

1. Unary predicates
2. Invertible predicates that are partially instantiated
3. General predicates
$=$ remaining relations
Example:

$$
\text { step } s \longrightarrow \text { riser } r \text {, tread } t\langle\text { orthogonal }(r, t)\rangle
$$

## Outline

Constrained attribute grammars<br>Scene interpretation<br>Bottom-up parsing

Experiments

## Semantization pipeline



## CAD models

Preprocessing

- Region growing over triangles for polygon creation
- Computation of exact and approximate adjacency graphs



## CAD models



## CAD models

Detection of walls, roofs and openings
(more examples in supplem. material)


## Real data: photogrammetry

- Preprocessing (point cloud)
$\square$ clustering using RANSAC (or region growing)
$\square$ polygons bounded by alpha shapes
- Problems:
$\square$ missing primitives
$\square$ false primitives
$\square$ wrong adjacencies
- Solution:
$\square$ use of a relaxed grammar
- looser bounds
- 1-2 missing items OK
$\square 22$ openings out of 31



## Quasi-real data: simulated LIDAR



- Planes by region growing in depth image
- Polygons as oriented bounding rectangles
- Adjacency based on pixels in depth image


## Size and parsing time (CAD models)

| Name | \# of triangles | \# of polygons | Parsing time (s) stairs openings |  |
| :---: | :---: | :---: | :---: | :---: |
| LcG | 48332 | 9705 | 5 | 15 |
| LcA | 111979 | 26585 | 14 | 42 |
| LcC | 385541 | 111732 | 33 | 306 |
| LcD | 313012 | 75257 | 25 | 111 |
| LcF | 286996 | 84347 | 39 | 322 |

## Precision and recall (\%, CAD models)

|  | \# of | \# of | Stairs |  | Openings |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Name | stairs | steps | Prec. | Rec. | \# | Prec. | Rec. |
| LcG | 3 | 45 | 100 | 93 | 83 | 100 | 90 |
| LcA | 6 | 84 | 100 | 100 | 62 | 98 | 83 |
| LcC | 30 | 210 | 100 | 100 | 196 | 100 | 98 |
| LcD | 5 | 61 | 93 | 100 | 74 | 100 | 93 |
| LcF | 7 | 98 | 100 | 50 | 99 | 100 | 96 |

## Future work

- Principled way to deal with partial or missing primitives
- Exploitation of occlusion/visibility information
- Scoring of interpretations: pick best tree(s)


## Conclusion

Constrained attribute grammars:

- appropriate to semantize complex objects
- high-level specification language
$\square$ being expert is enough, computer scientist not required
- efficient even on large models

This work:

- well-delimited first step: perfect data
- extensions required for incomplete/noisy data

On the web

- http://imagine.enpc.fr/
- sites.google.com/site/boulchalexandre/

